

Final Exam, ECE 137A

Wednesday March 20, 2019, Noon - 3 p.m.

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Closed Book Exam:

Class Crib-Sheet and 2 pages (4 surfaces) of student notes permitted

Do not open this exam until instructed to do so. Use any and all reasonable approximations (5% accuracy), *after stating & justifying them*.

Show your work:

Full credit will not be given for correct answers if supporting work is missing.

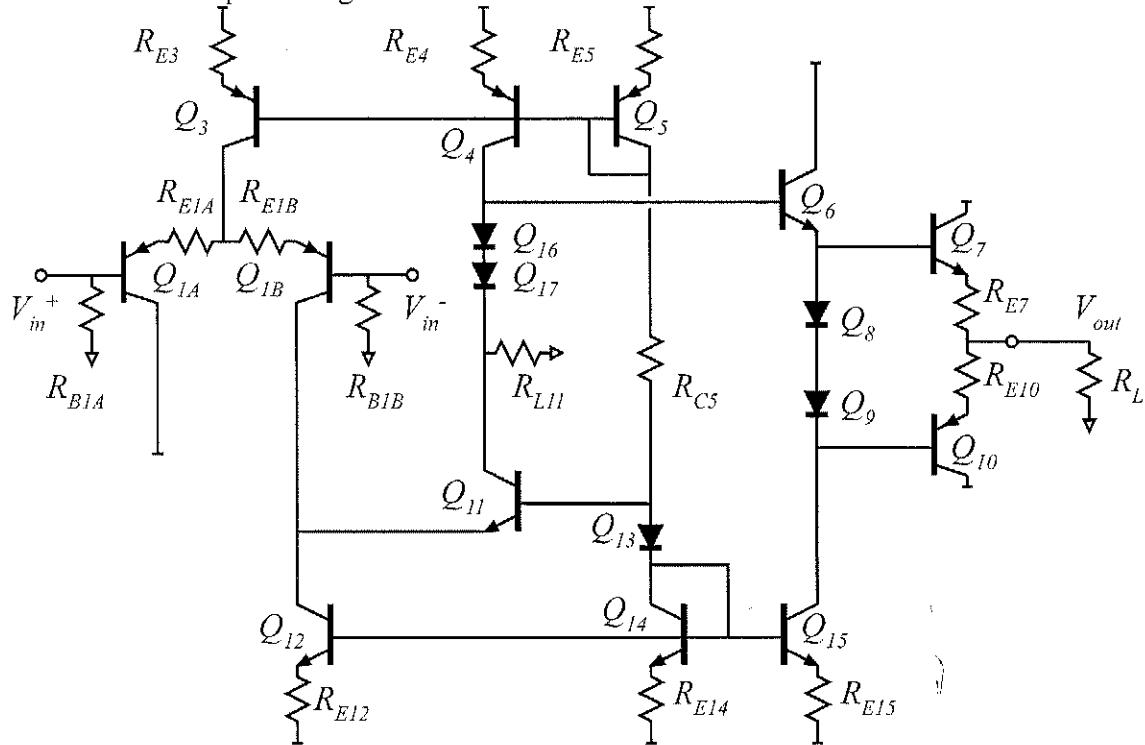
Good luck

Time function	LaPlace Transform
$\delta(t)$ impulse	1
$U(t)$ unit step-function	$1/s$
$e^{-\alpha t} U(t)$	$\frac{1}{s + \alpha} = \frac{1/\alpha}{1 + s/\alpha}$
$e^{-\alpha t} \cos(\omega_d t) U(t)$	$\frac{s + \alpha}{(s + \alpha)^2 + \omega_d^2}$
$e^{-\alpha t} \sin(\omega_d t) U(t)$	$\frac{\omega_d}{(s + \alpha)^2 + \omega_d^2}$

Part	Points Received	Points Possible	Part	Points Received	Points Possible
1a		6	2c		15
1b		5	2d		10
1c		4	3a		7
1d		10	3b		8
1e		10	3c		7
2a		10	3d		8
2b		10			
total		100			

Problem 1, 35 points

This is an NOT an Op-Amp: Analyze under the assumption that the differential and common mode input voltages are at zero volts



All the transistors have the same (matched) I_S , have $\beta = 100$, and $V_A = \infty$ Volts.

$$V_{CE(sat)} = 0.5 \text{ V}.$$

V_{be} is approximately 0.7 V,

but use $V_{be} = (kT/q) \ln(I_E/I_S)$ when necessary or appropriate.

The supplies are +4 Volts and -4 Volts.

All transistors (and diodes) have the same I_S

Q1A,1B,5,11 are biased at 10mA collector current.

Q6 is biased at 25mA collector current.

Q7 and Q10 are biased at 3mA collector current.

The DC voltage drops across RE5 and RE14 are both 400mV.

RB1A=RB1B=2kOhm. RE1A=RE1B=44.8Ohm. RL11=1.1kOhm.

RL=1kOhm.

Part a, 6 points

DC bias---to simplify ,assume $\beta = \infty$ for the DC analysis only.

Find the value of the following resistors:

$$\begin{aligned} R_{E5} &= 40\Omega & R_{E14} &= 40\Omega & R_E4 &= 40\Omega \\ R_{E15} &= 18\Omega & R_{E12} &= 20\Omega & R_E3 &= 20\Omega \\ R_E7 &= 18.4\Omega & R_E10 &= 18.4\Omega \end{aligned}$$

$$1 \quad [R_{E3} = \frac{400mV}{20mA} = 20\Omega = R_{E12}]$$

$$1 \quad [R_{E4} = \frac{400mV}{10mA} = 40\Omega = R_{E5} = R_{E14} = R_{E4}]$$

$$1 \quad [R_{E6} = \frac{400mV}{25mA} = 16\Omega]$$

$$3 \quad [R_E7 = R_{E10} = \frac{V_T \ln \left(\frac{25mA}{20mA} \right)}{3mA} = 18.4\Omega]$$

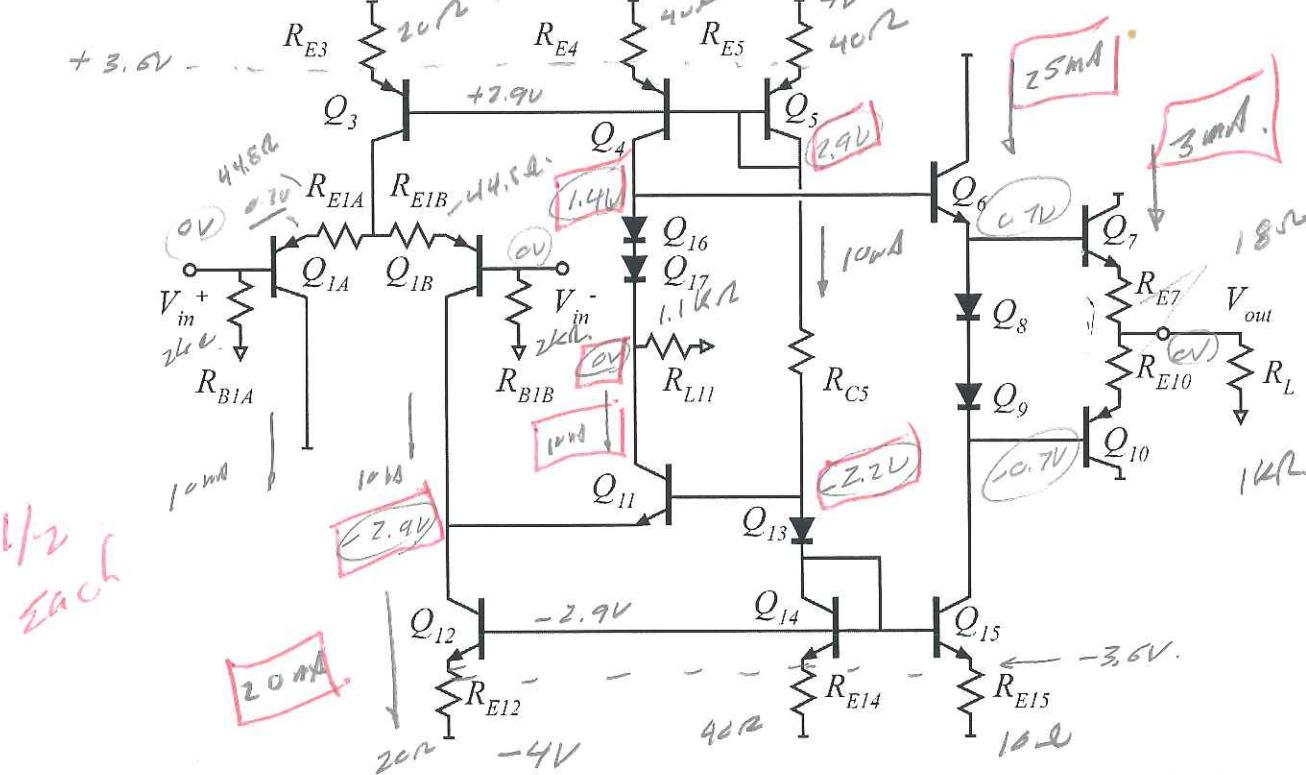
$$\beta = 100$$

$$V_A = \infty V$$

$$V_{CE,5ab} = 1.2 V$$

Part b, 5 points

DC bias---to simplify ,assume $\beta = \infty$ for the DC analysis only.



On the circuit diagram above, label the DC voltages at ALL nodes, and the DC collector currents of all transistors. Label the values of all resistors (except RC5).

$$R_{C6} = \frac{2.9V + 2.2V}{10k\Omega} = \frac{5.1V}{10k\Omega} = 510\Omega$$

Part c, 4 points

find the following

device	Q1AB	11	12	4	6	15	7	10
gm, mS	385	385	769	385	960	960	115	115

Q1A, 1B, 11, 4

$$I_C = 10mA \Rightarrow g_m = \frac{10mA}{26\Omega} = \frac{1}{2.6\Omega} = 385mS$$

Q12, 3,

$$I_C = 20mA \Rightarrow g_m = \frac{1}{1.3\Omega} = 769mS$$

Q6/15

$$I_C = 25mA \quad g_m = \frac{25mA}{26\Omega} = \frac{1}{1.04\Omega} = 0.965 = 960mS$$

Q7/10

$$I_C = 3mA \quad g_m = \frac{1}{26\Omega/13mA} = \frac{1}{8.67\Omega} = 115mS$$

Part d, 10 points.

Find the following, *using the actual value of β , i.e. $\beta=100$*

	Voltage Gain	Input impedance
Q1AB	0.4316	1.4 k Ω
Q11	392.66	3.0 M Ω
Q6	1	10 M Ω
Q7	0.97 to 1.0	100 k Ω
Overall differential Vout/Vin	11.6	1.4 k Ω

Note: with some insight, you can find the combined gain of Q1AB/11 in a single step. If you would like to do so, omit the separate answers for Q1AB and Q11 in the table above, and instead fill in the table below,

	Voltage Gain	Input impedance
Q1AB/ Q11 combination.	11.6	1.4 k Ω

Note: $R_E = \alpha R_L$!

We can treat Q7/Q10 as both on, or on one at a time.
 To: wide range of acceptable assumptions here.

Treat Q7 as on 1/10 as off:

$$\underline{Q7: \text{off}}; \quad \text{From } \downarrow \quad \left[A_{v7} = \frac{1k\Omega}{1k\Omega + 18\Omega + 9\Omega} = 0.97 \right]$$

$$R_{in7} = \beta(14\Omega + 18\Omega + 9\Omega) \approx \beta(14\Omega) = 100k\Omega \text{ (range ok)}$$

Q6. EF

$$R_{\text{leg}} = R_{\text{in}7} = 100 \text{ k}\Omega.$$

$$A_v = \frac{100 \text{ k}\Omega}{100 \text{ k}\Omega + 1/g_m} = \frac{100 \text{ k}\Omega}{100 \text{ k}\Omega + 1.04 \text{ }\mu\text{A}} \approx 0.999 \approx 1$$

$$R_{\text{in}6} = \beta(100 \text{ k}\Omega + 1/g_m) \approx \beta(100 \text{ k}\Omega) \\ = 10 \text{ M}\Omega \quad (!)$$

Q11 - common base

The impedance presented to Q11's base is

$$+R_{\text{es}}. \\ R_{\text{base}} = (1/g_{m3} + 1/g_{m4} + R_{E4}) \parallel (1/g_{m5} + R_{E5}) \\ = (2.6 \Omega + 2.6 \Omega + 40 \Omega) \parallel (2.6 \Omega + 40 \Omega + 510 \Omega) \\ = 41.7 \Omega \quad (-\text{pt for using } R_S = 0 \Omega)$$

$$R_{\text{in}11} = 1/g_m + R_{\text{dec}}/\beta = 2.6 \Omega + \frac{41.7}{100} = 3.0 \Omega$$

$$R_{\text{leg}11} = R_{11} \parallel R_{\text{in}6} = 1.1 \text{ k}\Omega \parallel 10 \text{ M}\Omega \\ \approx 1.1 \text{ k}\Omega \quad (\text{all } R_{\text{ce}} \text{ are infinite}).$$

$$A_{v11} = \frac{1.1 \text{ k}\Omega}{3.0 \Omega} = 366.66 \Omega$$

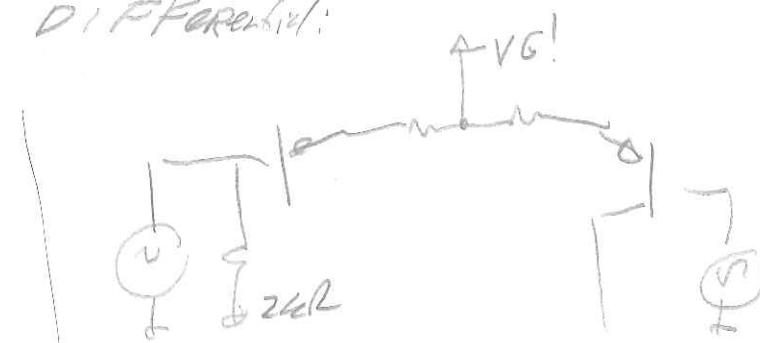
Q11A/Q13

$$R_{\text{leg}} = R_{11} \parallel 3.0 \Omega$$

$$A_v = \frac{R_{\text{leg}}}{2(1/g_m + R_A)} = \frac{3.0 \Omega}{2(2.6 \Omega + 44.8 \Omega)} \\ = \frac{3.0}{2(47.4 \Omega)} = 0.0316$$

Input impedance - depends upon DRIVE signal

For DIFFerential:



$$Z_{in} = 2k\Omega \parallel \beta(1/g_m + R_{out})$$

$$\Rightarrow 2k\Omega \parallel 100(47.4\Omega) = 2k\Omega / 4.74k\Omega$$

$$= 1.4k\Omega$$

or the α_{AB}/β combination:

$\text{Av} = \frac{\text{Av}_{\text{eq}}}{2(1/g_m + R_{out})} = \frac{1.1k\Omega}{2(2.6\Omega + 44.8\Omega)}$

$\frac{1.1k\Omega}{2(47.4\Omega)} = 11.6 \approx$

Part e, 10 points

Maximum peak-peak output voltage (**show all your work**)

For this, you must use the full circuit diagram, not the half circuit diagram.

	magnitude and sign of maximum output signal swing due to <i>cutoff</i>	magnitude and sign of maximum output signal swing due to <i>saturation</i>
Transistor Q7	not relevant	+ 3.5V
Transistor Q10	not relevant	- 3.5V
Transistor Q6	- 2.450V (1)	+ 3V
Transistor Q15	not relevant - no signal	- 3.04V
Transistor Q4	not relevant - no signal	+ 1.67V
Transistor Q11	+ 10.8V	- 2.36V
Transistor Q1A	+ 10.8V	(omit)
Transistor Q1B	- 10.8V	(omit)

Be warned: In some cases a limit is not relevant at all. Mark those answers "not relevant". But, give a 1-sentence statement below as to why it is not relevant. Q7/10 form a push pull stage, so be careful about your answer there..

[Q7 cutoff - not relevant push-pull]

[Q7 saturation: $V_{out} = V_{cc} - V_{CE(sat)} = 6V - 1/2V = 3.5V$

[Q10] same as Q7, but negative voltage.

Q6 saturation $V_{out} = (V_{cc} - V_{CE(sat)6} - V_{CE(sat)7}) \cdot \frac{1k\Omega}{1k\Omega + 18\Omega}$

$$\approx (6V - 4V - 1/2V) = 3V.$$

Q6 cutoff: $\Delta V_{out} = -I_{CQ6} \cdot R_{load} \cdot A_{v7} = 25mA \cdot 100k\Omega \cdot 0.98$
 $\approx -2.450V$

Q15 saturation $V_{out} = (-3.6V + V_{CE(sat)}) \frac{1k\Omega}{1k\Omega + 18\Omega}$
 $\approx (-3.6V + 1/2V)(0.98) = -3.04V.$

Q1 saturation

$$V_{out} = (+3.6V - V_{CE, sat} - V_{be6} - V_{be7}) (0.982)$$

$$= (3.6V - 1.2V - 1.4V) (0.982) = (1.7V) (0.982) = 1.67V.$$

Q1' saturation

$$V_{out} = (-2.9V + V_{CE, sat} + V_{be16} + V_{be17} - V_{be6} - V_{be7}) (0.982)$$

$$= (-2.9V + V_{CE, sat}) 0.982 = (-2.4V) (0.982) = -2.33V.$$

α_{1A} cut off If $I_{C1A} \rightarrow 0mA$, then $I_{C1B} = 2mA$

and $I_{C11} = 0mA$

$$\Rightarrow \Delta V_{C11} = 10mA \cdot 1.1k\Omega = +11V$$

$$\Delta V_{out} = (11V) (0.982) = +10.8V.$$

α_{1B} cut off - same as above, w/ll signs reversed

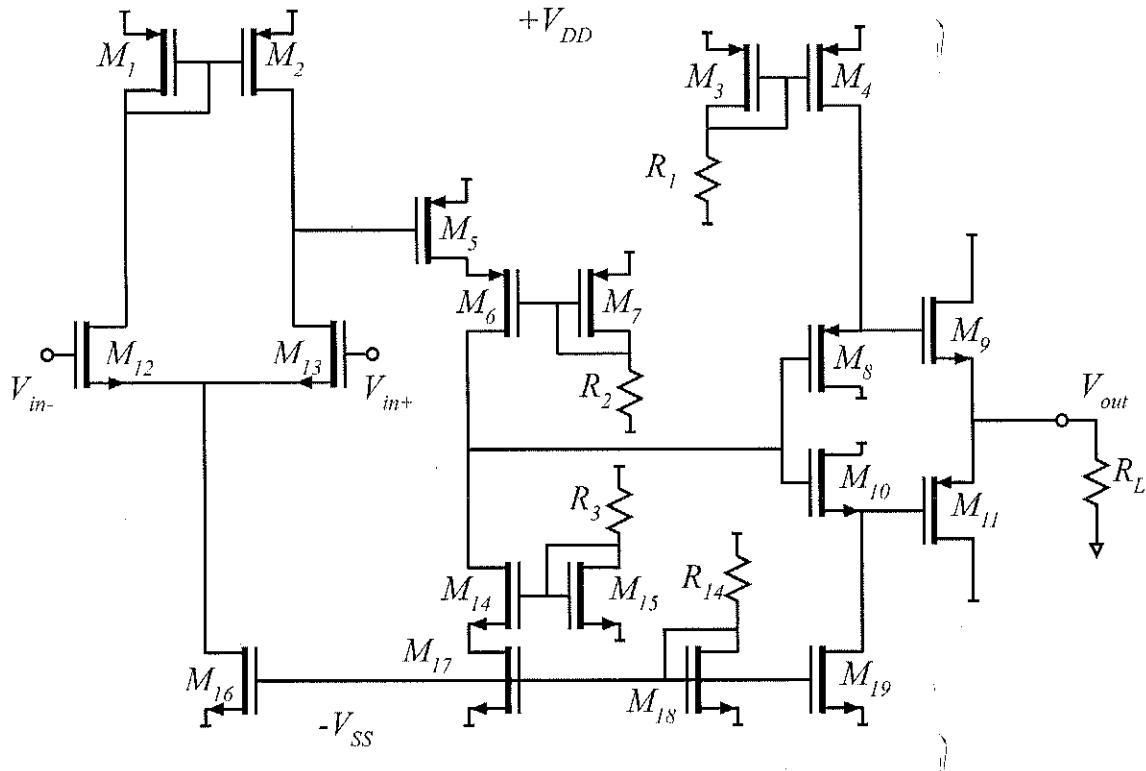
$$\Delta V_{out} = -10.8V$$

α_{11} cut off: $\Delta I_C = 10mA \rightarrow \Delta V_{C11} = 1/1k\Omega \cdot 10mA = +11V$

$$\Delta V_{out} = 11V \cdot (0.982) = +10.8V$$

Problem 2, 35 points

This is an Op-Amp---analyze the bias under the assumption that DC output voltage is zero volts, that the positive input V_{in+} is zero volts, and that we must determine the DC value of the negative input voltage (V_{in-}) necessary to obtain this.



The NMOSFETs have $K_\mu = \mu c_{gs} W_g / 2L_g = 0.55 \text{ mA/V}^2 \cdot (W_g / 1\mu\text{m})$

$K_v = c_{gs} v_{inj} W_g = 0.69 \text{ mA/V} \cdot (W_g / 1\mu\text{m})$, $\Delta V = v_{inj} L_g / \mu = 0.625 \text{ V}$, $V_{th} = 0.25 \text{ V}$,

$1/\lambda = 20 \text{ V}$

The PMOS have identical parameters, except, of course, V_{th} is negative.

$V_{DD} = +1 \text{ V}$, $-V_{SS} = -1 \text{ V}$, $R_L = 50 \text{ kOhm}$

All transistors have $|V_{gs}| = 0.35 \text{ V}$, *except for M7 and M15*, which have $|V_{gs}| = 0.45 \text{ V}$, *and except for M8,9,10,11*, which have $|V_{gs}| = 0.30 \text{ V}$

M12,13 are biased at $I_D = 25 \mu\text{A}$.

M5,7,15 are biased at $I_D = 50 \mu\text{A}$.

M8,9,10,11 are biased at $I_D = 50 \mu\text{A}$.

Ignore $(1 + k_{BS})$ term!

Part a, 10 points

DC bias.

Analyze the bias under the assumption that DC output voltage is zero volts, that the positive input V_{i+} is zero volts, and that we must determine the DC value of the negative input voltage (V_{i-}) necessary to obtain this.

(Hint, this should give $V_{i-} = 0V$)

Find the following:

Gate widths of M12 and M13 = _____

Gate width of M7 = _____

Gate width of M8 = _____

Gate width of M9 = _____

$$I_D = 0.55 \text{ mA/V}^2 (V_{GS} - V_{BL})^2 (1 + \frac{W_g}{L_m}) \frac{W_g}{L_m}$$

M_{12,13}: $2S_{MS} = 0.55 \text{ mA/V}^2 (0.11V)^2 (1 + \sqrt{\frac{1.3V}{200}}) \frac{W_g}{L_m}$

$$W_g = 4.55 \mu\text{m} = +$$

M₇: $S_{MS} = 0.55 \text{ mA/V}^2 \frac{W_g}{L_m} (0.2V)$

$$V_g = 2.27 \mu\text{m}$$

M_{8,9}: $S_{MS} = 0.55 \text{ mA/V}^2 (0.03V)^2 \frac{W_g}{L_m}$

$$W_g = 36.4 \mu\text{m}$$

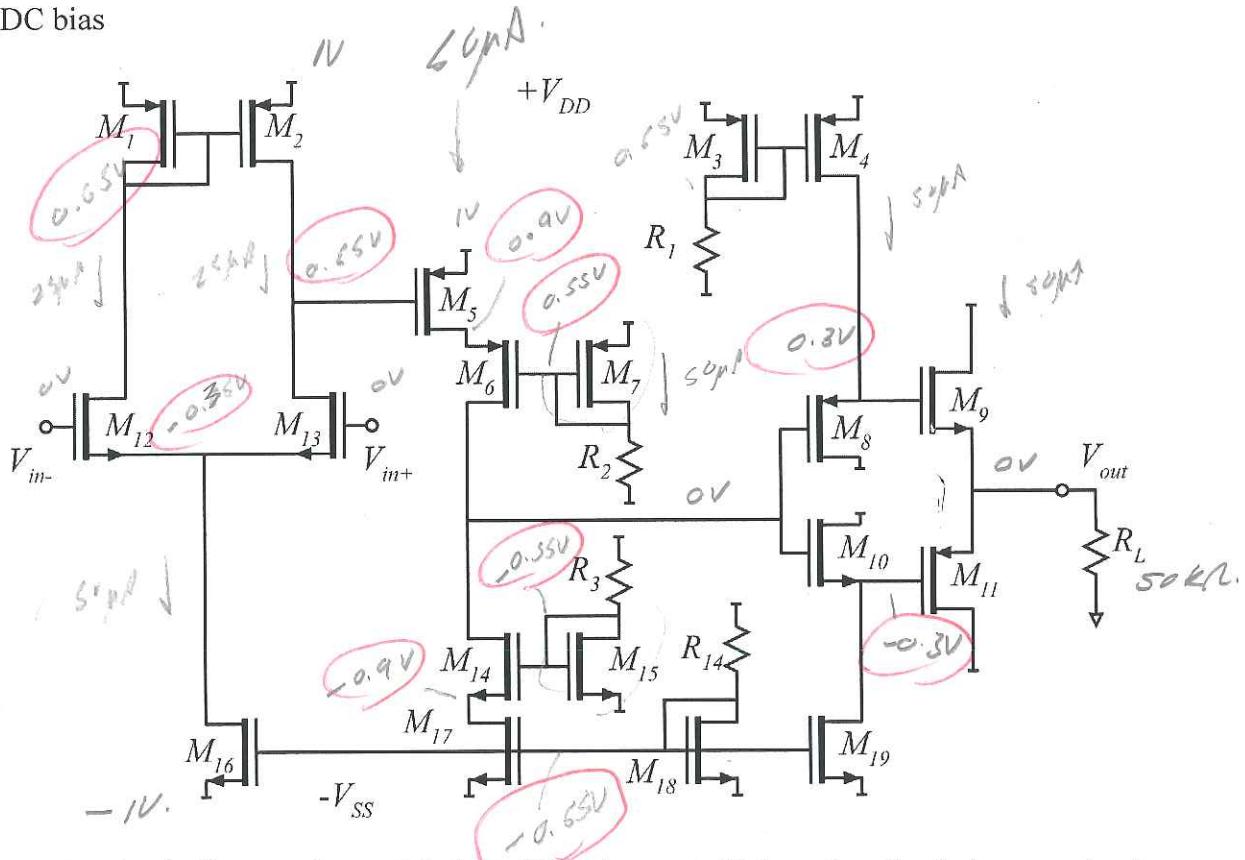
3.33 ohm

$$V_A = 20V, \quad V_{BL} = 0.25V.$$

$$k_m = 0.55mN \cdot \frac{W}{L} \frac{V}{V_{DD}}$$

Part b, 10 points

DC bias



On the circuit diagram above, label the DC voltages at ALL nodes, the drain currents of ALL transistors, and the gate widths of ALL transistors.

1 out

Part c, 15 points.

You will now compute the op-amp differential gain. Find the following

	Voltage Gain	Input impedance
Transistor combination M1,2,13, 13	200.	$\infty \Omega$.
M5,6 combination	50,000	$\infty \Omega$.
Q9 or Q12. M6 or 1000 q	0.9975	0Ω
Q8 or Q15 M9 or 11	0.993	0Ω
Overall differential Vout/Vin	16 million	∞ .

Notes:

1) You can analyze M5 and M6 as separate stages, or as a combined stage using Norton/Thevenin methods. Don't ask for hints as to how to do this.

2) For M8/9 and for M10/11, you can assume that M8 and M9 are on for the positive signal swing and M10 and M11 are on for the negative signal swing. More accurately, you can assume, for the signal swing near zero volts, that all are on. If you take the latter approach (and do it correctly), you will receive a couple of extra credit points. One hint (don't ask for any other hints): use symmetry.

M9 & M11 take both on (signal swing near zero V)
 \Rightarrow each effectively a $\text{div} 2R_L = 100k\Omega$

$$R_{\text{leg}} = R_{\text{leg}} \parallel 100k\Omega = \frac{1}{2 \cdot 100k\Omega} = \frac{20V}{50mA} \parallel 100k\Omega = 80k\Omega$$

[if we take M9 on, M11 off, the R_{leg} will be $R_{\text{leg}} \parallel 100k\Omega - \text{ok}$]

$$\text{Av}_9/11 = \frac{80k\Omega}{80k\Omega + 100k\Omega} \quad \text{but } g_m = \frac{2I_D}{(V_{GS} - V_{TH})} = \frac{2(50mA)}{50mV} = \frac{1}{25} = 25$$

$$= \frac{80k\Omega}{80k\Omega + 500m\Omega} = 0.993$$

$$R_{\text{leg}} = \infty \Omega$$

$$\underline{\text{M8 or M9}} \quad R_{D54} = R_{S8} = \frac{1}{\lambda Z_D} = \frac{20V}{50mV} = 400k\Omega$$

$$R_{L58} = R_{D54} \parallel R_{D58} = 200k\Omega.$$

$$1 \quad g_m = 2 ID / (V_{GS} - V_{th}) = \frac{2(50mA)}{50mV} = 2ms.$$

$$1 \quad A_V = \frac{R_{L58}}{R_{L58} + 1/g_m} = \frac{200k\Omega}{200k\Omega + 500mA} = 0.9975 \approx 1.$$

$$\underline{\text{M6}} \quad R_{D514} = R_{S17} = \frac{1}{\lambda Z_D} = \frac{20V}{50mV} = 400k\Omega.$$

$$1 \quad g_{m4} = g_{m17} = \frac{2(50\mu A)}{100mV} = 1ms.$$

Note that M17 is biased at $V_{DS} = V_{thSS} \rightarrow 0k\Omega$.

$$1 \quad R_{out14} = R_{D514} (1 + g_{m14} R_{S17}) \approx g_m R_{DS}^2 = \\ = 100M\Omega.$$

$$1 \quad A_{L586} = R_{L58} / R_{out14} = 160mA.$$

$$1 \quad R_{L58} = \frac{1}{g_{m6}} \left[1 + \frac{R_{D56}}{R_{DS6}} \right] \approx \frac{1}{g_m} \frac{R_{D56}}{R_{DS6}} = \frac{1}{g_m} \frac{R_{DS6}^2}{R_{DS6}} \\ = R_{DS6} (!) = 400k\Omega.$$

$$1 \quad A_{V6} = R_{D56} / R_{out14} = g_m R_{DS6}^2 / R_{DS6} = g_m R_{DS6}.$$

$$1 \quad \underline{\text{M5}} \quad R_{L585} = R_{DS5} \parallel A_{L586} = R_{DS5} \parallel R_{DS6} = R_{DS5}/2$$

$$1 \quad A_{V5} = -g_m R_{L585} = -g_m R_{DS5}/2$$

$$1 \quad \Rightarrow A_{V5} A_{V6} = (-g_m R_{DS5}/2) (g_m R_{DS6}) = (g_m R_{DS})^2 / 2 \\ = (1ms \cdot 400k\Omega)^2 / 2 = (400)^2 / 2 = \underline{\underline{80,000}}$$

$$\underline{m_{1,2,12,13}} \quad \underline{\text{1}} \quad \underline{\text{2}} \quad \underline{\text{3}} \quad \underline{\text{4}} \quad \underline{\text{5}} \quad g_{m12,13} = \frac{2I_D}{V_{DS}-V_{GS}} = \frac{2(25\mu A)}{0.1V} = 0.5mA$$

$$R_{DS} = \frac{1}{g_m I_D} = 20V/25\mu A = 800k\Omega$$

~~length for R_{ds}~~ $N = g_m R_{ds}$

$$\underline{\text{1}} \quad \underline{\text{2}} \quad \underline{\text{3}} \quad \underline{\text{4}} \quad R_{ds} = R_{ds2} / R_{ds13} = 400k\Omega$$

$$\underline{\text{1}} \quad \underline{\text{2}} \quad \underline{\text{3}} \quad N = 0.5mA \cdot 400k\Omega = 200$$

$$= g_m R_{ds2}$$

overall gain

Part d, 10 points

Maximum peak-peak output voltage at the positive output V_{O+} (**show all your work**)

	magnitude and sign of maximum output signal swing due to <i>cutoff</i>	magnitude and sign of maximum output signal swing due to: <i>knee voltage</i> (saturation)
Transistor M9	NR	0.95V
Transistor M11	NR	-0.95V
Transistor M8	+10V	NR
Transistor M10	-10V	NR
Transistor M4	NR	+0.6V
Transistor M19	NR	-0.6V
Transistor M6	-400mV	+0.8V
Transistor M14	NR	-0.8V

Be warned: in some cases a limit is not relevant. Mark those answers "not relevant".

V_D [M9, M11 cutoff - push pull - not relevant]

All transistors are mostly linear.

[M9 sat.: $V_{GS} = 0.3V$, $V_{TH} = 0.25V \Rightarrow V_{DS,SET} = 0.05V$.

$$V_{out} = V_{O+} - V_{DS,SET} = 1V - 0.05V = 0.95V.$$

\checkmark [M11 - some calculation, - sign]

\checkmark [M8 saturation - Not relevant! as this limits - gate drive to M9

\checkmark [M10 " " " " " " " " + " " " " " " M11.

[M8 cutoff: $R_{LEG} = 200k\Omega$, $\Delta I/\Delta V_{DS} = 5\text{mA/V}$

$$\Delta V = \Delta I \cdot R_{LEG} \cdot \Delta V_{DS} = 5\text{mA} \cdot 200k\Omega \cdot 1 = 10V.$$

\checkmark [M10 cutoff - some calculation, - sign].

\checkmark [M4, M19 cutoff - not relevant, no signal].

[M4 sat.: $V_{GS} = 0.3V$, $V_{TH} = 0.25V \Rightarrow V_{DS,SET} = 0.1V$.

$$\Delta V_{out} = (1V - 0.1V - 0.3V) / 10V \approx 1V - 0.1V - 0.3V = 0.6V.$$

\checkmark [M14 sat.: same as above, - sign].

M6 sat $V_{GS} = 0.35V$, $V_{TH} = 0.25V \Rightarrow V_{OS,SET} = 0.1V$

$$M14, \text{max drain voltage} = 0.9V - 0.1V = 0.8V.$$

$$\Delta V_{out} = 0.8V \cdot A_{v8A_{v9}} \approx 0.8V.$$

M6 cutoff. Throwing impedance at M6 drain:

$$= R_{DS} + R_{DS,14} = g_m R_{DS}^2 / 2$$

$$\text{Max. drain } \Delta I = 50\mu A$$

$$\begin{aligned}\Delta V &= -50\mu A (g_m R_{DS}^2 / 2) \cdot A_{v8} A_{v9} \\ &= -4000V \text{ (c!) }\end{aligned}$$

M14 cutoff not relevant - no signal.

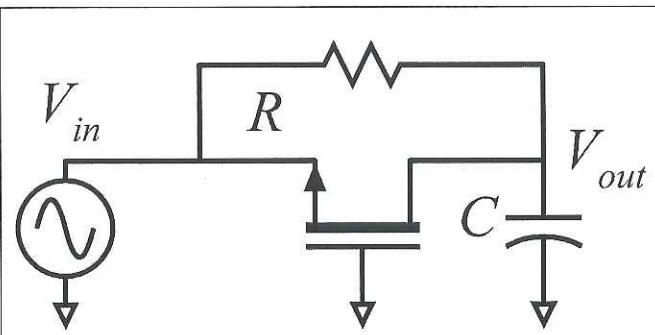
M14 sat

$$V_{OS,SET} = 0.1V$$

$$\begin{aligned}\Delta V_{out} &= (-0.9V + 0.1V) A_{v8} A_{v7} \\ &= -0.8V.\end{aligned}$$

overall, amplifier can drive $\pm 0.8V$
as limited by M4, M14 saturation.

Problem 3, 30 points



You will be working on the circuit to the left

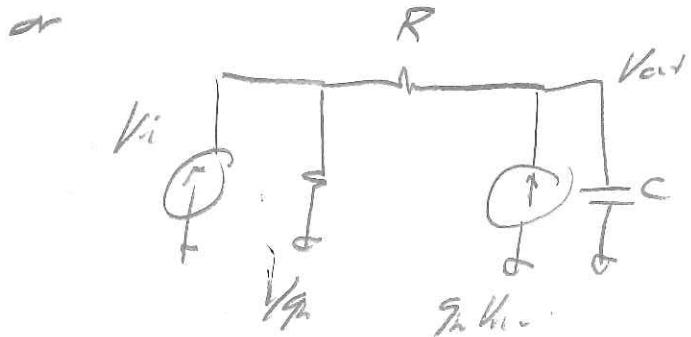
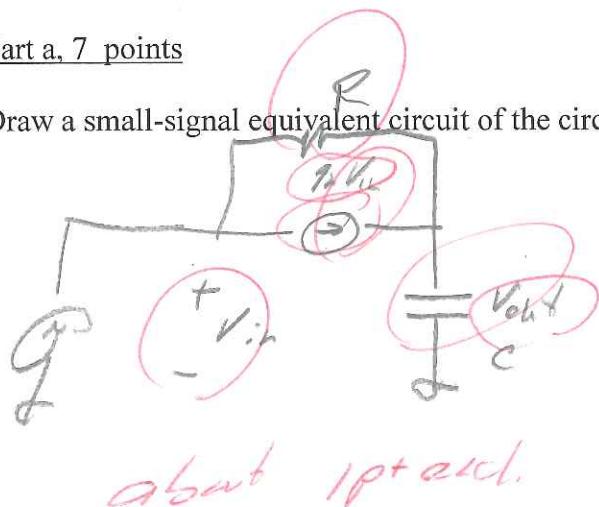
Ignore DC bias analysis. You don't need it.

The transistor has transconductance gm .

Its output resistance R_{ds} is infinity...so you don't need to include this element in the circuit diagram !

Part a, 7 points

Draw a small-signal equivalent circuit of the circuit.



Part b, 8 points

$g_m = 10 \text{ mS}$, $C = 1 \text{ pF}$, $R = 1000 \text{ Ohms}$

Find, by nodal analysis, a small-signal expression for V_{out}/V_{in} . Be sure to give the answer with **correct units** and in ratio-of-polynomials form, i.e.

$$\frac{V_{out}(s)}{V_{gen}(s)} = K \cdot \frac{1 + b_1 s + b_2 s^2 + \dots}{1 + a_1 s + a_2 s^2 + \dots} \text{ or (as appropriate)} \frac{V_{out}(s)}{V_{gen}(s)} = K \cdot (s\tau)^n \cdot \frac{1 + b_1 s + b_2 s^2 + \dots}{1 + a_1 s + a_2 s^2 + \dots}$$

Note that an expression like

$$\frac{V_{out}(s)}{V_{gen}(s)} = \frac{1}{1 + (3 \cdot 10^{-6})s} \text{ is dimensionally wrong; } \frac{1}{1 + (3 \cdot 10^{-6} \text{ seconds})s} \text{ is dimensionally correct}$$

$$V_{out}(s)/V_{in}(s) = \underline{\quad}$$

2 $\boxed{\sum I = 0 \text{ at } V_{out}. \quad (G = 1/R)}$

3 $\boxed{(V_{out} - V_{in})G + dC V_{out} - g_m V_{in} = 0.}$

$$V_{out}(G + dC) = V_{in}(g_m + G)$$

$$\begin{aligned} \frac{V_{out}}{V_{in}} &= \frac{g_m + G}{G + dC} = \frac{g_m + G}{G} \cdot \frac{1}{1 + dCR} \\ &= (1 + g_m R) \cdot \frac{1}{1 + dCR} \end{aligned}$$

3 $\boxed{\frac{V_{out}}{V_{in}} = " \cdot \frac{1}{1 + dCR(s)} "}$

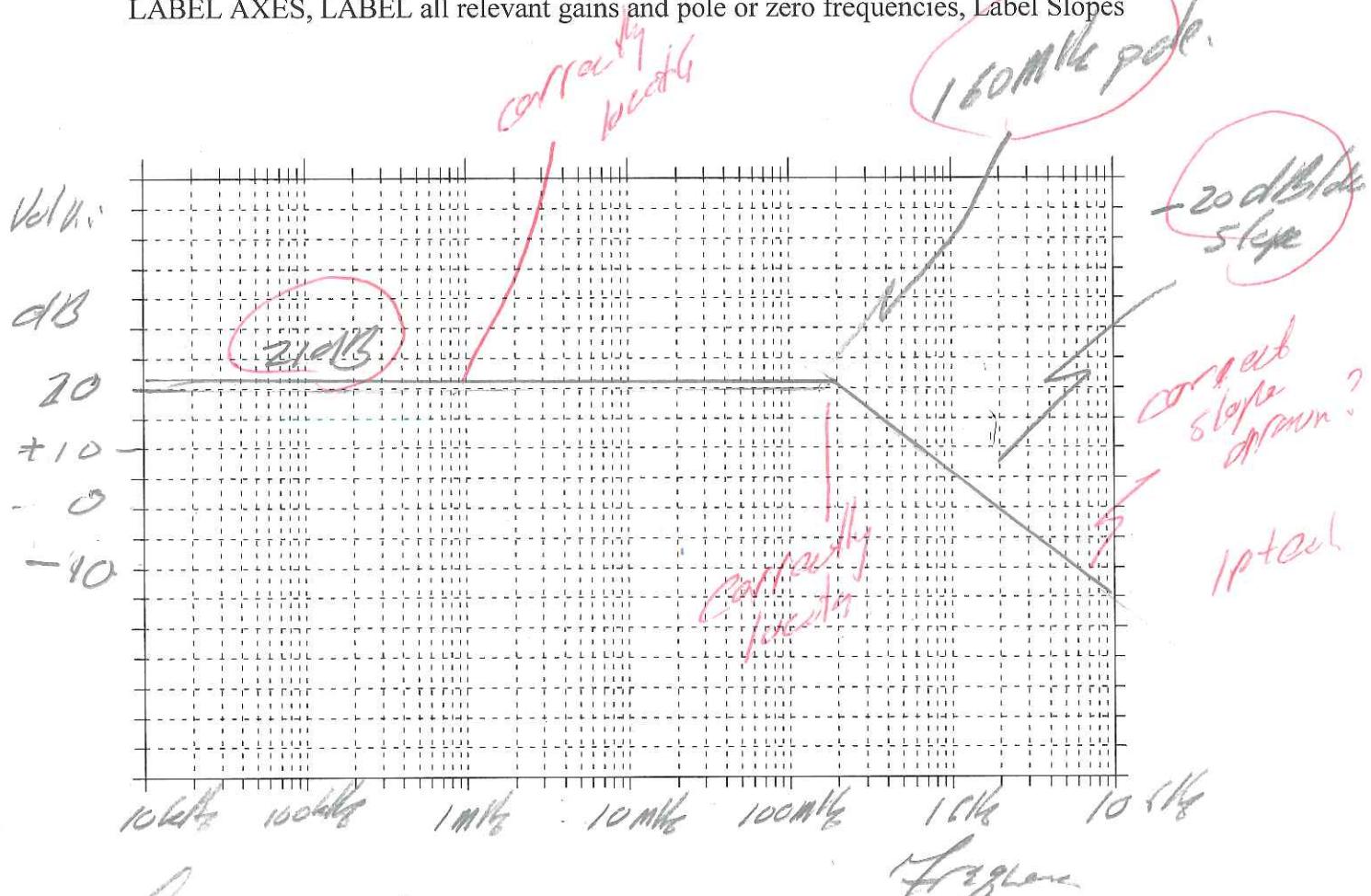
Part c, 7 points

Find any/all pole and zero frequencies of the transfer function, in Hz:

160 MHz pole

Draw a clean Bode Plot of Vout/Vin,

LABEL AXES, LABEL all relevant gains and pole or zero frequencies, Label Slopes



$$f_{pole} = \frac{1}{2\pi(1\text{ns})} = \underline{\underline{159 \text{MHz}}}$$

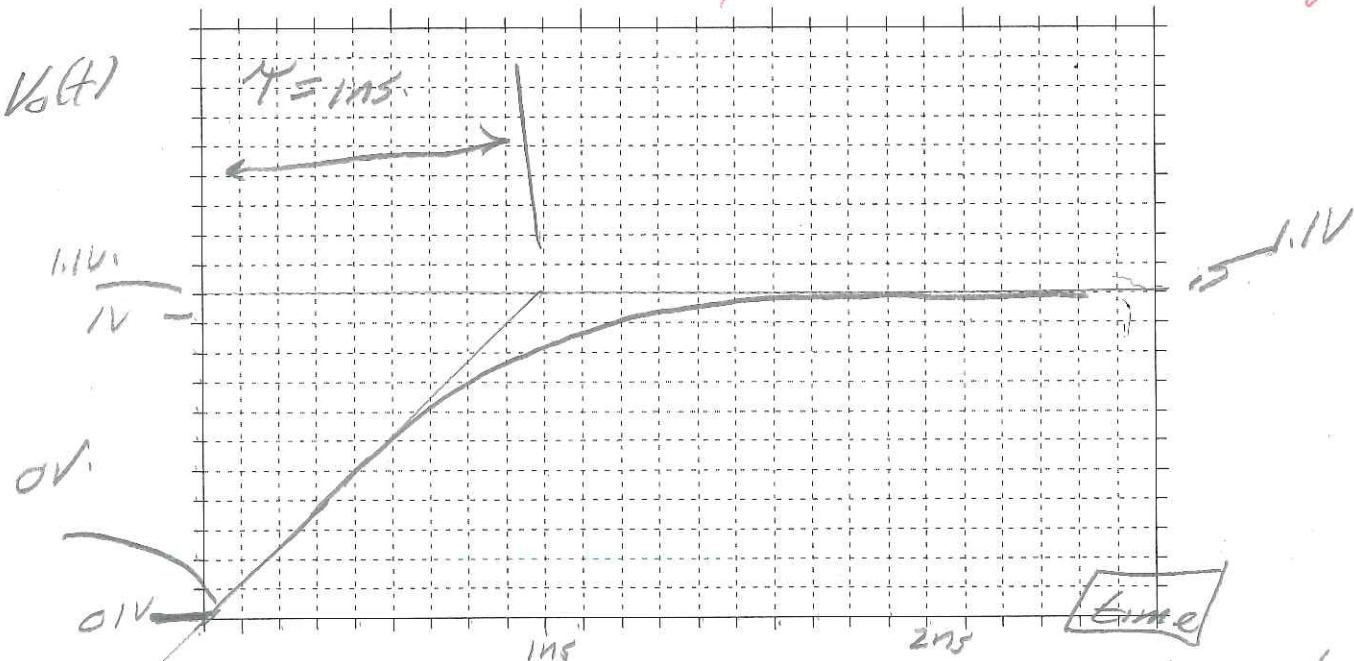
Part d, 8 points

$V_{in}(t)$ is a 0.1 V amplitude step-function.

$$V_{out}(t) = 1.1V \cdot u(t) \cdot [1 - e^{-t/1ms}]$$

Plot it below. Label axes, show initial and final values, show time constants.

-49pt for correct accept graph



$$V_{out}(s) = \frac{1}{1 + s(1ms)} \cdot \frac{0.1V}{s} = 1.1V \int \frac{1}{1 + sc(1ms)}$$

$$\boxed{V_{out}(t) = 1.1V \cdot u(t) [1 - e^{-t/1ms}]}$$