## ECE ECE145A (undergrad) and ECE218A (graduate)

## Final Exam. Tuesday, December 10, 12-3 p.m.

Do not open exam until instructed to.
Open notes, open books, etc. You have 3 hrs.
Use all reasonable approximations (5\% accuracy is fine. ),
AFTER STATING and justifiying THEM.
Think before doing complex calculations. Sometimes there is an easier way.

| Problem | Points Received | Points Possible |
| :--- | :--- | :--- |
| 1a |  | 5 |
| 1b |  | 5 |
| 1c |  | 5 |
| 1d |  | 5 |
| 1e |  | 5 |
| 1f |  | 5 |
| 2 |  | 10 |
| 3 |  | 10 |
| 4 a | 5 |  |
| 4 b |  | 5 |
| 5 a |  | 5 |
| 5 b | 5 |  |
| 5 c |  | 10 |
| 6a |  | 10 |
| 6b |  | 10 |
| total |  | 100 |

Name: $\qquad$
$G_{T}=\frac{\left|S_{21}\right|^{2}\left(1-\left|\Gamma_{s}\right|^{2}\right)\left(1-\left|\Gamma_{L}\right|^{2}\right)}{\left|\left(1-\Gamma_{s} S_{11}\right)\left(1-\Gamma_{L} S_{22}\right)-S_{21} S_{12} \Gamma_{s} \Gamma_{L}\right|^{2}} \quad G_{P}=\frac{1}{1-\left\|\Gamma_{i n}\right\|^{2}} \cdot\left|S_{21}\right|^{2} \cdot \frac{1-\left|\Gamma_{L}\right|^{2}}{\left|1-\Gamma_{L} S_{22}\right|^{2}}$
$G_{a}=\frac{1-\left|\Gamma_{S}\right|^{2}}{\left|1-\Gamma_{S} S_{11}\right|^{2}} \cdot\left|S_{21}\right|^{2} \cdot \frac{1}{1-\left\|\Gamma_{\text {out }}\right\|^{2}} \quad G_{\max }=\frac{\left|S_{21}\right|}{\left|S_{12}\right|} \cdot\left[K-\sqrt{K^{2}-1}\right]$ if $K>1$
$G_{M S}=\frac{\left|S_{21}\right|}{\left|S_{12}\right|}$. if $K<1 \quad K=\frac{1-\left|S_{11}\right|^{2}-\left|S_{22}\right|^{2}+|\Delta|^{2}}{2\left|S_{21} S_{12}\right|} \quad$ where $\Delta=\operatorname{det}[S]$
Unconditionally stable if : (1) $\mathrm{K}>1$ and (2) $\|\operatorname{det}[S]\|<1$

Problem 1, 30 points
gain definitions

| At a signal frequency of 1 GHz , a two-port |
| :--- | :--- |
| has $S_{11}=0.6, S_{12}=1 / 4, S_{21}=2$ and $S_{22}=0$, |
| as defined with a 50 Ohm impedance |
| reference. |

part a, 5 points
If the 2-port were directly connected to 50 Ohm load, and a 50 Ohm generator with 10 mW available power, what would be the power dissipated in the load ?
part b, 5 points
If the load is an open circuit (infinity Ohms), then what is the input impedance ?
part c, 5 points
If you were to first stabilize (if necessary) and then impedance match the input and output to 50 Ohms , and drive the input with generator of 10 mW available power, what would be the power delivered to the load?
part d, 5 points
If you were to load the 2-port, without matching or stabilization elements, with a 150 Ohm load, is it possible to select a generator impedance which would cause the 2-port to oscillate?
part e, 5 points
If you were to load the 2-port, without stabilization elements, in 50 Ohms, and then impedance-match the input to a 50 Ohm generator with 10 mW available source power, what would be the power in the load?

## part f, 5 points

If you were to take the 2-port, without stabilization elements, connect the input directly to a 500 Ohm generator with 10 mW available source power, and then connect the output directly to a 150 Ohm load, what would be the power in the load?

## Problem 2, 10 points

## Stabilization

Source stability circle

| A MOSFET in common-source mode has $\left\\|S_{11}\right\\|$ and $\left\\|S_{22}\right\\|$ both less than 1. . Source and |
| :--- |
| load stability circles are as shown. The Smith charts use 50 Ohms impedance |
| normalization. Draw $* * 2 * * *$ circuit diagrams, giving resistor values, of methods of |
| stabilizing the transistor. Please draw your answers in the 3 boxes to the right and |
| below |
| circuit \#1 |
|  |
|  |

## Problem 3, 10 points

Gain circles


A FET in common-source mode has operating and available gain circles as shown. Find the optimum generator and load impedances (in complex Ohms).
optimum source impedance= $\qquad$
optimum load impedance= $\qquad$

## Problem 4, 10 points

2 -port parameters and gains.


Examining the figure above, we note that network E can be represented as a cascade of networks A-D. Note also that it can be easily shown that $S_{21} / S_{12}=Y_{21} / Y_{12}$ for any 2-port network.
part a, 5 points
Compute $Y_{21}$ and $Y_{12}$ of network C.
$\qquad$ $Y_{12}=$

## part b, 5 points

Find $S_{21} / S_{12}$ of network E.
$S_{21} / S_{12}=$
**State your arguments clearly***. Points will be deducted it steps are not justified.
This analysis explain why transistor maximum stable gain tends to have specific variation with frequency.

## Problem 5, 20 points

Transistor cutoff frequencies and gain relationships.
part a, 5 points

$\mathrm{MAG}=$
part b: 5 points
Give expressions for the optimum generator and load impedances.
The answers must be in clear, simple, and tractable form.
Zgen,opt=
ZL,opt=
part c: 10 points

| Compute, as a function of $R_{b e} C_{b e}, g_{m}$, |
| :--- | :--- |
| $C_{c e}$ and $R_{c e}$ the maximum available power |
| gain as a function of frequency. Find also |
| the $f_{\text {max }}$ of the transistor |
| 1) the answer must be in a clear, simple, <br> and tractable form. |

$\mathrm{MAG}=$ $\qquad$
$f_{\text {max }}=$ $\qquad$
(this answer should give some insight into high-frequency transistor design considerations).

Problem 6, 20 points
Power amplifier design.


A MOSFET has large-signal parameters as given above and small-signal parameters as given below:
$g_{m}=1.0 \mathrm{mS} / \mu m \cdot W_{g} \quad R_{i}=1.0 / g_{m} \quad C_{g d}=0.0 \mathrm{fF} / \mu \mathrm{m} \cdot W_{g} \quad C_{g s}=1.0 \mathrm{fF} / \mu \mathrm{m} \cdot W_{g}$ $C_{d s}=0.5 \mathrm{fF} / \mu \mathrm{m} \cdot \mathrm{W}_{g} G_{d s}=0 \mathrm{mS} / \mu \mathrm{m} \cdot W_{g}$
part a, 10 points
You will use a FET of 50 microns total gate width. The signal frequency is 15.9 GHz . What this the maximum linear RF output power? What is the optimum load (give either load impedance or load admittance) ?

Pout, max $=$ $\qquad$
Yload= $\qquad$
or
Zload= $\qquad$

## part b, 10 points

The amplifier has a properly-designed input matching network. With the output power you calculated above, what available generator power is required?

Available generator power $=$

