## ECE ECE145A (undergrad) and ECE218A (graduate) <br> Mid-Term Exam. October 26, 2015

Do not open exam until instructed to.
Open notes, open books, etc
You have 1 hr and 15 minutes.

Use any and all reasonable approximations (5\% accuracy is fine.) , AFTER STATING THEM.

| Problem | Points Received | Points Possible |
| :--- | :--- | :--- |
| 1 |  | 15 |
| 2 a |  | 10 |
| 2 b |  | 15 |
| 3 a |  | 10 |
| 3 b |  | 10 |
| 3 c |  | 10 |
| 4 |  | 15 |
| 5 |  | 15 |
| total |  | 100 |

Name: $\qquad$

## Problem 1, 15 points

The Smith Chart and Frequency-Dependent Impedances.
HINT: use the scales on the figures to measure distances as needed.




First match each Smith Chart with each circuit. Then determine as many component values as is possible (RLC values, transmission line delays and characteristic impedances)...note that some values cannot be determined with the information given. The charts all use 50 Ohm normalization:

| Smith chart (a). Circuit= | Component values= |
| :---: | :---: |
| Smith chart (b). Circuit= | Component values= |
| Smith chart (c). Circuit= | Component values= |
| Smith chart (d). Circuit= | Component values= |
| Smith chart (e). Circuit= | Component values= |
| Smith chart (f). Circuit= | Component values= |

## Problem 2, 25 points

2 -port parameters and Transistor models

Part a, 10 points
For the network at the right, give algebraic expressions for the four S-parameters.

Assume a normalization to impedance Zo for the $S$ parameters.


Part b, 15 points
For the network at the right, give algebraic expressions for the four Y-parameters.


## Problem 3, 30 points

Transmission-line theory
Hint: we are testing here your understanding of transmission-lines and their relationships to lumped elements. If the calculation appears to be extremely difficult, you may possibly be missing some key insight.

Part a, 7.5 points
You have a microstrip line of 10 cm length, and 5 mm width. The substrate is 2 mm thick and has a dielectric constant of 2.0. Treat fringing fields approximately by assuming that the effective conductor width is the physical conductor width plus twice the substrate thickness

Find the characteristic impedance of the line, the velocity, the total line inductance, and the total line capacitance.

Part b, 7.5 points
We now load port 2 with a resistance of 10 kOhm. Give an approximate expression for the frequency-dependent input impedance, measured at port 1. The approximation need be valid only over a $\mathrm{DC}-100 \mathrm{MHz}$ signal frequency range.


Part c, 7.5 points
We now load port 2 with a resistance of 2
Ohms. Give an approximate expression for the frequency-dependent input impedance, measured at port 1. The approximation need be valid only over a $\mathrm{DC}-100 \mathrm{MHz}$ signal frequency range.


## Part d, 7.5 points

At what frequency is the line one quarterwavelength in length? If we load port 2 with a 30 Ohm resistance, what would be the input impedance at port 1 at this frequency?


## Problem 4, 15 points

Impedance-matching exercise.
The ( 50 Ohm normalization) Smith chart gives the input impedance of a circuit at 1 GHz signal frequency. Design a lumped-element matching network which converts this impedance to $* * 500 \mathrm{hms} * *$ at 1 GHz . Give all element values.


## Problem 5, 15 points

Transmission-line parasitics.

Part a, 7.5 points
You have a microstrip line of 10 cm length, and 5 mm width. The substrate is 2 mm thick and has a dielectric constant of 2.0.
**Neglect** the fringing fields.
The conductivity of gold is
$44.2 * 10^{6}$ Siemens/meter and
$\mu_{0}=4 \pi * 10^{-7} \mathrm{H} / \mathrm{m}$. Find (i) the skin
 (iii) the total line attenuation at 10 GHz signal frequency.
Hint----the skin depth is $\delta=\sqrt{2 / \omega \mu_{0} \sigma}$

Part b, 7.5 points
We are not happy with the line attenuation we calculated above. So, we choose to make the circuit board thicker, while adjusting the conductor width to keep the same characteristic impedance. (i) If we increase the board thickness by 5:1, what is the total line attenuation now? (ii) At what frequency might we expect to see lateral modes on the transmission-line?


