ECE ECE145A (undergrad) and ECE218A (graduate) Final Exam. Monday December 6, 2021, noon - 3 p.m.

Open book. You have 3 hrs.

Use all reasonable approximations (5% accuracy is fine.),

AFTER STATING and justifying THEM.

Think before doing complex calculations. Sometimes there is an easier way.

Problem	Points Received	Points Possible
1A		5
1B		5
1C		5
1D		5
1D		5
1F		5
1G		10 (218A only)
2		10
3		10
4A		10
4B		10 (218A only)
5A		5
5B		5
total		(145A), 114 (218A)

$$G_{T} = \frac{\mid S_{21} \mid^{2} (1 - \mid \Gamma_{s} \mid^{2}) (1 - \mid \Gamma_{L} \mid^{2})}{\mid (1 - \Gamma_{s} S_{11}) (1 - \Gamma_{L} S_{22}) - S_{21} S_{12} \Gamma_{s} \Gamma_{L} \mid^{2}} \qquad G_{P} = \frac{1}{1 - \|\Gamma_{in} \|^{2}} \cdot |S_{21}|^{2} \cdot \frac{1 - |\Gamma_{L}|^{2}}{\mid 1 - \Gamma_{L} S_{22} \mid^{2}}$$

$$G_{a} = \frac{1 - |\Gamma_{S} \mid^{2}}{\mid 1 - \Gamma_{S} S_{11} \mid^{2}} \cdot |S_{21}|^{2} \cdot \frac{1}{1 - \|\Gamma_{out} \|^{2}} \qquad G_{max} = \frac{|S_{21}|}{|S_{12}|} \cdot \left[K - \sqrt{K^{2} - 1}\right] \text{if } K > 1$$

$$G_{MS} = \frac{|S_{21}|}{|S_{12}|} \cdot \text{if } K < 1 \qquad K = \frac{1 - |S_{11}|^{2} - |S_{22}|^{2} + |\Delta|^{2}}{2 |S_{21} S_{12}|} \quad \text{where } \Delta = \det[S]$$

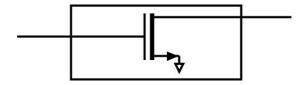
Unconditionally stable if: (1) K>1 and (2) $\|\det[S]\|<1$

Problem 1, 30 points (145A), 40 points (218A)

Power Gain Definitions

part a, 5 points

At 10 GHz, the transistor has S11=-0.5, S21=+2, S12=0, S22=+0.5



The generator has 100 Ohms source impedance and 1 mW available power. The load is 25 Ohms.

If we place impedance-matching networks between the generator and the transistor, and between the transistor and the load, what RF powered will be deliver to the load?

RF power delivered to the load = $64/9 \,\text{mW} \stackrel{6}{=} 71 \,\text{mW}$

Matched on in, out -> MAG

-> MAG = - 1-115,112 1-11522/12

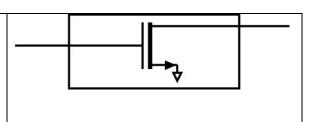
 $= \frac{1}{1 - 1/4} \quad 4 \cdot \frac{1}{1 - 1/4}$ $= \frac{4}{3} \cdot 4 \cdot \frac{4}{3} = \frac{26}{9}$

 $R = MSE \cdot P_{DVg} = 1 \frac{MW \cdot Z}{q}$ $= \frac{64}{9} \frac{MW}{9} = 71.6 \frac{MW}{9}$

part b, 5 points

At 10 GHz, the transistor has S11=-0.5, S21=+2, S12=0, S22=+0.5

The generator has 50 Ohms source impedance and 1 mW available power. The load is 50 Ohms.



If we directly connect the generator and load to the transistor, what RF power will be delivered to the load?

RF power delivered to the load = 4mh

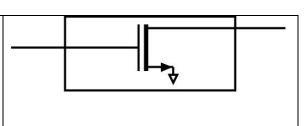
Byen = Ze = Zo; direct Connection

2 -> gain = 1/52/12 = 4

1 Pava 1 = 4 mW part c, 5 points

At 10 GHz, the transistor has S11=-0.5, S21=+2, S12=0, S22=+0.5

The generator has 100 Ohms source impedance and 1 mW available power. The load is 25 Ohms.



If we directly connect the generator and load to the transistor, what RF power will be delivered to the load?

RF power delivered to the load = $\frac{Z}{SSMW}$ NO Metched on Sither gen or load = $\frac{Z}{SSMW}$ $G_T = \frac{|S_{21}|^2 (1-|\Gamma_s|^2)(1-|\Gamma_L|^2)}{|(1-\Gamma_sS_{11})(1-\Gamma_LS_{22})-S_{21}S_{12}\Gamma_s\Gamma_L|^2} \frac{1}{2} \frac{1}{2$

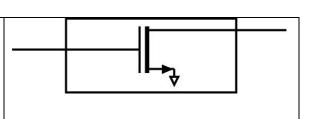
 $\frac{1 - 1/4}{(1 + \frac{1}{3} \frac{1}{2})^{2}} = \frac{1 - 1/9}{(1 + \frac{1}{3} \frac{1}{2})^{2}}$ $\frac{3/4}{(7/6)^{2}} = \frac{8/9}{(7/6)^{2}} = 2.825$

1/2 = 2.825.1mW = 2.825 mW.

part d, 5 points

At 10 GHz, the transistor has S11=-0.5, S21=+2, S12=0, S22=+0.5

The generator has 100 Ohms source impedance and 1 mW available power. The load is 25 Ohms.



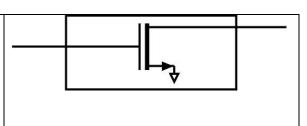
If we impedance-match the generator to the transistor input, but directly connect the load to the transistor output, what RF power will be delivered to the load?

RF power delivered to the load = $\frac{3.48 \text{ MW}}{3.48 \text{ MW}}$ $G_P = \frac{1}{1 - \|\Gamma_{ln}\|^2} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$ The pedente metal on output, not input $IM = \frac{3.48 \text{ MW}}{1 - |\Gamma_L|} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$ $IM = \frac{3.48 \text{ MW}}{1 - |\Gamma_L|} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$ $IM = \frac{1}{3} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$ $IM = \frac{1}{3} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$ $IM = \frac{1}{3} \cdot |S_{21}|^2 \cdot \frac{1 - |\Gamma_L|^2}{|1 - \Gamma_L S_{22}|^2}$ | because sizeo, sine I'm Gp = 1-115/112 1/52/12 1-1/2/12 $\frac{1}{1 - 1/4} \cdot 4 \cdot \frac{1 - 1/q}{(1 + \frac{1}{3} + \frac{1}{5})^2}$ $= \frac{4}{3} \cdot 4 \cdot \frac{8/q}{(7/6)^2}$ = 3.48Pr = 3,48.1mW = 3.48 mW

part e, 5 points

At 10 GHz, the transistor has
S11=-0.5, S21=+2, S12=0, S22=+0.5

The generator has 100 Ohms source impedance and 1 mW available power. The load is 25 Ohms.



If we directly connect the generator to the transistor input, but impedance-match the load to the transistor output, what RF power will be delivered to the load?

RF power delivered to the load = $\frac{2}{938}$ m

| [Load matched, import not -> Go GN

[Int = Szz because Siz 50 1/4 [= 100/50

14 [= 100/50 - [= 1 100/50 + 1 3 14[2] = 25/50 - 1 = 1/2 - 1 25/50 + 1 1/2 + 1 = -1

$$G_{a} = \frac{1 - |\Gamma_{S}|^{2}}{|1 - \Gamma_{S}S_{11}|^{2}} \cdot |S_{21}|^{2} \cdot \frac{1}{1 - ||\Gamma_{out}||^{2}}$$

$$\begin{cases} \frac{1-1/4}{(1+\frac{1}{3}\frac{1}{2})^2} & \frac{24-\frac{1}{1-1/4}}{(1-\frac{1}{3}\frac{1}{2})^2} \\ \frac{3/4}{(7/6)^2} & \frac{4}{3} & \frac{3}{3} & \frac{3}{49} & 4 \end{cases}$$

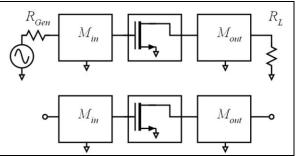
$$G_{4} = 2.939$$

Pe = Ga · Pavg = 2.938 MV.

part f, 5 points

At 10 GHz, the transistor has S11=-0.5, S21=+2, S12=0, S22=+0.5

The generator has 25 Ohms source impedance and 1 mW available power. The load is 100 Ohms.



We first impedance-match the generator to the transistor input and then impedance-match the load to the transistor output (upper diagram). We then disconnect the generator and the load (lower diagram), leaving us with the transistor and its input and output networks, which we can an "amplifier".

Please find the following:

S11 of the "amplifier"=

S22 of the "amplifier"=

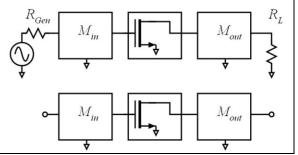
 $\frac{1/4}{I_{s}} = \frac{25 k_{0} - 1}{25 k_{0} + 1} = \frac{1}{1/2 + 1} = -\frac{1}{3}$ $\frac{1/4}{I_{c}} = \frac{100 k_{0} - 1}{100 k_{0} + 1} = \frac{4}{3}$

||S21||orate ||mapping|| = 1After matchin Z.i. mast be 2512, Zect must be 1001 $||S0|| S11 = \frac{25/50-1}{25/50+1} = -1/3$ ||S21||orate ||mapping|| = 1 ||S21|| orate ||mapping|| = 1 $||S0|| S11 = \frac{25/50-1}{25/50+1} = -1/3$ $||S0|| S22 = \frac{100/60-1}{100/80+1} = +1/3$

part g, 10 points (218A only)

At 10 GHz, the transistor has S11=-0.5, S21=+2, S12=0, S22=+0.5

The generator has 25 Ohms source impedance and 1 mW available power. The load is 100 Ohms.



We first impedance-match the generator to the transistor input and then impedance-match the load to the transistor output (upper diagram). We then disconnect the generator and the load (lower diagram), leaving us with the transistor and its input and output networks, which we can an "amplifier".

Please find the following:

16/27 = 0.59 ||S21|| of the "amplifier"=

This will required some hard thinking

Amplifier model:

Reht = 1000

Prova = (Au Vin) 2/4/Rost } MAG = Prova = Au Rout

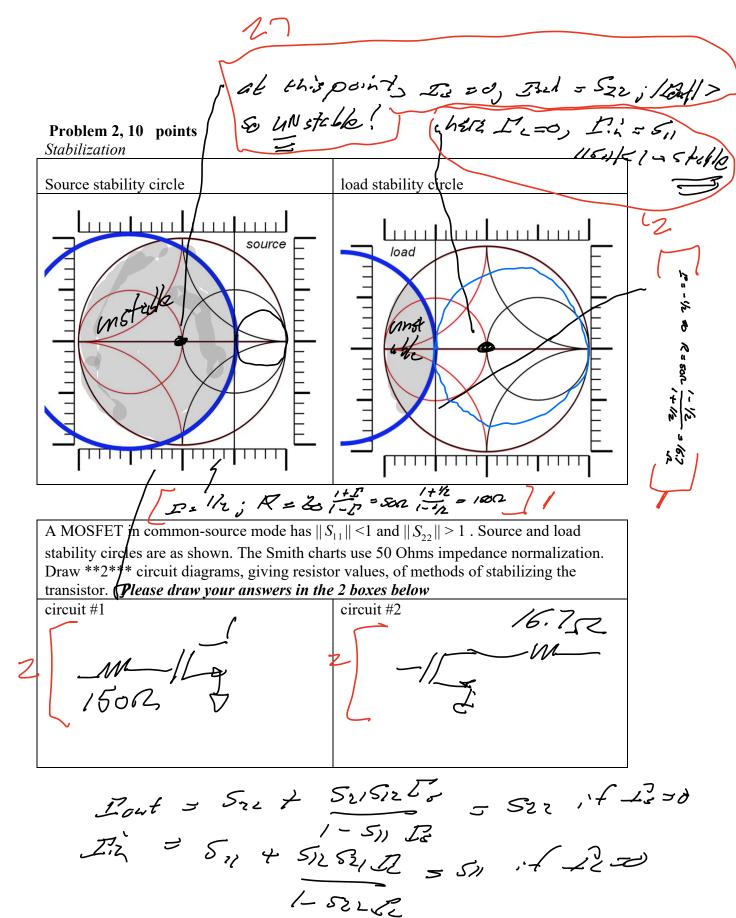
Pri = Vin 2/Rin }

Prins C/Rin _

 $MAG = \frac{1}{1-|S_{11}|^{2}} \frac{15z_{1}|^{2}}{1-|S_{12}|^{2}} \frac{1}{1-|S_{12}|^{2}} \frac{9.000}{1-|S_{12}|^{2}}$ $= \frac{1}{1-1124} \cdot 4 \cdot \frac{1}{1-4} = \frac{4}{3} \cdot 4 \cdot \frac{4}{3}$

64 = | Av | Polet = 1/Av/P 1000 9 4P.2 4.250 $|\mathcal{A}| = \sqrt{\frac{647}{9}} = \frac{8}{3}$ 1152111. [511]= 2 10 / Ex= Eg 520 / = Z · $\frac{250}{750}$ · $\frac{8}{3}$ · $\frac{500}{1520}$ 52. 1. 87. 5 20,59

Can Also acre with spector



$$G_{a} = \frac{1 - |\Gamma_{S}|^{2}}{|1 - \Gamma_{S}S_{11}|^{2}} \cdot |S_{21}|^{2} \cdot \frac{1}{1 - ||\Gamma_{out}||^{2}}$$

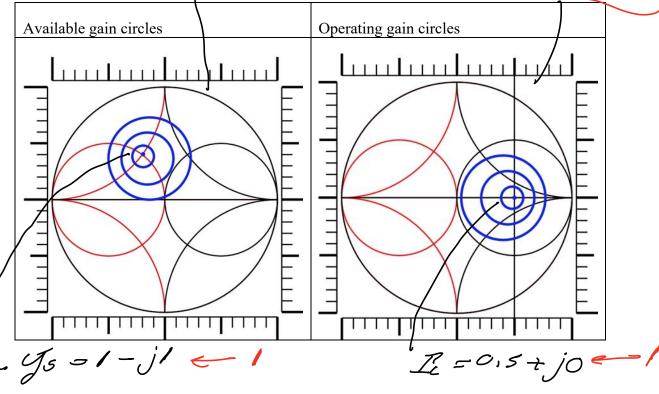
$$Depends on Is$$

$$Depends of$$

 $\frac{|1-\Gamma_L S_{22}|^2}{|Dopendson} II$ Is plane

Problem 3, 10 points Gain circles

IE plans



A FET in common-source mode has operating and available gain circles as shown (50 Ohm impedance normalization). Find the optimum generator and load impedances (in complex Ohms).

optimum source impedance= 250 + 0250

optimum load impedance= 150 R + jO D

 $\frac{(J_{s} \circ pt = 1 - j1)}{=} \frac{1}{S_{s} \circ pt} = \frac{(1 - j1)}{S_{on}} = \frac{(1 - j1)}{S_{on}} = \frac{S_{on}(1 + j1)}{(1 - j1)(1 + j1)} = 25n + j25n$

In, ept = 1/2

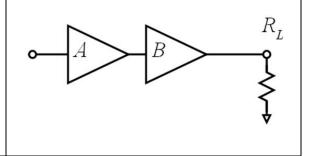
1 -> Eropt = 500 1+1/2 = 1500

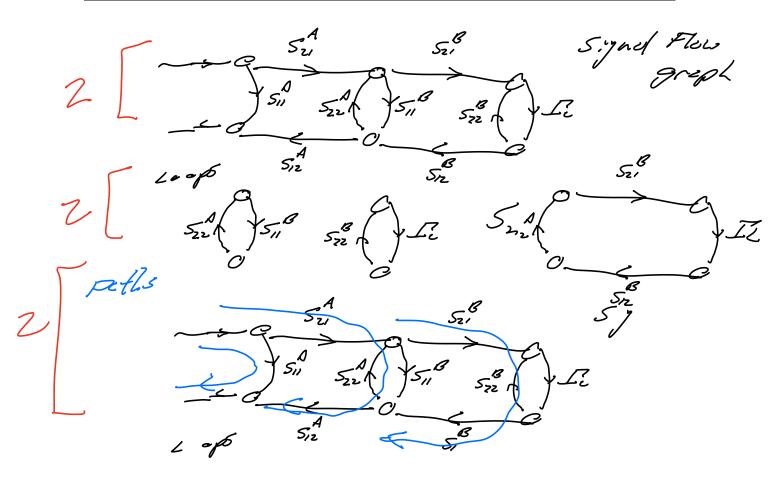
Problem 4, 10 points (145A), 20 points (218A)

2-port parameters and signal flow graphs

Part a, 10 points

Amplifiers A and B have S-parameters S_{ij}^A and S_{ij}^B . The output is connected to a load with reflection coefficient Γ_L . As a function of these given parameters, compute Γ_{in} , the input reflection coefficient.

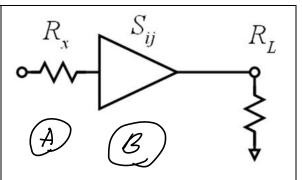


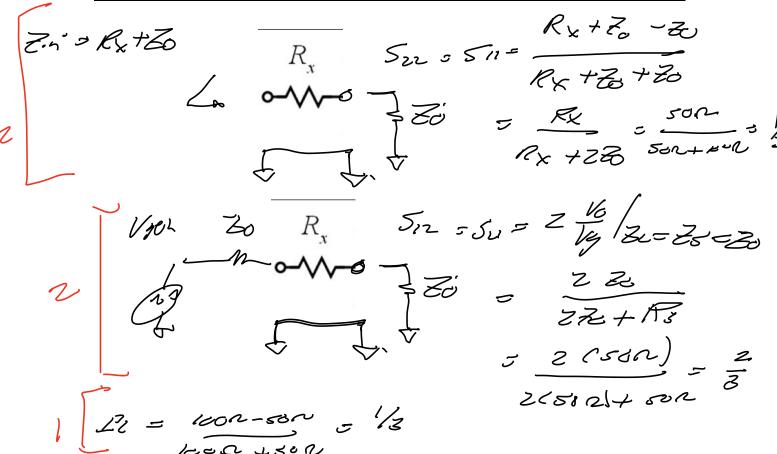


1 - 511 S22 - 522 IL + 51, B52 522 IZ - 52, B512 522 A 511 (1-511852) -522 IZ +51, B522 522 IZ -52, B512 522 AZ + 521 S11 S12 (- IZ 522) or 4 pt. 4 52, 52, BL 5,2 5n Con Sin t or 4pt 52, 511 512 (- IZ522) + 52, 52, IL 512 512 1-5118521-522 IZ +51,85252 IZ-52,8512 522 A In Sit or 4pt 521 511 512 (- IZ522) + 521 521 IL 512 512 (1-5118521)(1-522 IZ) -5218512 522 A [all 3 forms of the answer can be written by inspection for the

Part b, 10 points (218a only)

The amplifier has (50 Ohm normalization) S11=-0.5, S21=+2, S12=1/5, S22=+0.5. The load is 100 Ohms, and a resistor, Rx=50Ohms, is connected to the input. Using properties of S-parameters and signal flow graphs, find Γ_{in} of the resulting network





Problem 5, 10 points

Power amplifier design

part a, 5 points

You are working in some mm-wave CMOS technology. The maximum safe current is 1 mA per micrometer of gate width. For wide bandwidth (high fmax), the maximum gate width is 1.0 micrometers; set the gate width at this value, but use multiple gate fingers to further increase maximum gate current to some desired value.

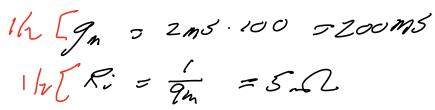
The maximum safe drain-source voltage is 1.2V, and the minimum (knee) voltage is 0.2 Volts.

What is the maximum RF power per 1 micron gate finger? (1/8). mW

If the minimum impedance we could tune to were 10 Ohms, how many parallel gate fingers would we use in the power transistor, so that the required load impedance were 10 Ohms? _______ (please round the answer to the nearest integer)

What output power would that cell produce? 12.5mh/

What would be the drain efficiency? 1/2, & 35.7%,



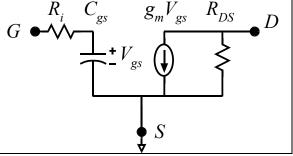
part c, 5 points

The transistor is now modelled by the the equivalent circuit to the right.

 $g_m = 2 \text{ mS*(number gate fingers)}$

 $f_{\tau} = 100 \text{ GHz}$

 $R_{ds} = \text{infinity}, R_i = 1/g_m \text{ Ohms},$



Given a 10 Ohm load, and the number of gate fingers you have found earlier, what input power at 10 GHz is necessary to produce this maximum output power?

12 Note simply:

- may pp of current = 100ml pp.

- qiven fr = 100 Gk & fs = 10 4kg,

TE (I'n = 10). Tin = 10 ml pad-pack Sml peak

1/2 = 5. V27 ml RMS