## ECE ECE145A (undergrad) and ECE218A (graduate)

TAKE HOME Final Exam. Return before Friday December 15, 2017

HONOR SYSTEM: Open book. You have 3 hrs. WORK WITHOUT HELP.
Use all reasonable approximations ( $5 \%$ accuracy is fine. ) ,
AFTER STATING and justifying THEM.
Think before doing complex calculations. Sometimes there is an easier way.

| Problem | Points Received | Points Possible |
| :--- | :--- | :--- |
| 1A |  | 5 |
| 1B |  | 5 |
| 1C |  | 5 |
| 1D |  | 10 |
| 1E |  | 10 |
| 1F |  | 10 (218A only) |
| 2A |  | 10 |
| 2B | 5 |  |
| 2C |  | 5 |
| 2D |  | 5 |
| 3A |  | 10 |
| 3B |  | 10 |
| 4A | 5 |  |
| 4B |  | 10 |
| 4C | 10 (218A only) |  |
| total | 95 (145A), 115 (218A) |  |

## I certify that

1) I have taken no more that 3 hours to work the exam. (or DSP) limits.
2) I have help from no one
3) I did not read the exam until the time I took the exam.

Signed: $\qquad$
$G_{T}=\frac{\left|S_{21}\right|^{2}\left(1-\left|\Gamma_{s}\right|^{2}\right)\left(1-\left|\Gamma_{L}\right|^{2}\right)}{\left|\left(1-\Gamma_{s} S_{11}\right)\left(1-\Gamma_{L} S_{22}\right)-S_{21} S_{12} \Gamma_{s} \Gamma_{L}\right|^{2}}$ $G_{P}=\frac{1}{1-\left\|\Gamma_{i n}\right\|^{2}} \cdot\left|S_{21}\right|^{2} \cdot \frac{1-\left|\Gamma_{L}\right|^{2}}{\left|1-\Gamma_{L} S_{22}\right|^{2}}$
$G_{a}=\frac{1-\left|\Gamma_{S}\right|^{2}}{\left|1-\Gamma_{S} S_{11}\right|^{2}} \cdot\left|S_{21}\right|^{2} \cdot \frac{1}{1-\left\|\Gamma_{\text {out }}\right\|^{2}} \quad G_{\max }=\frac{\left|S_{21}\right|}{\left|S_{12}\right|} \cdot\left[K-\sqrt{K^{2}-1}\right]$ if $K>1$
$G_{M S}=\frac{\left|S_{21}\right|}{\left|S_{12}\right|}$. if $K<1 \quad K=\frac{1-\left|S_{11}\right|^{2}-\left|S_{22}\right|^{2}+|\Delta|^{2}}{2\left|S_{21} S_{12}\right|} \quad$ where $\Delta=\operatorname{det}[S]$
Unconditionally stable if : (1) $\mathrm{K}>1$ and (2) $\|\operatorname{det}[S]\|<1$

Problem 1, 35 points (145A), 45 points (218A)
Two-port properties, Power gain definitions

| At a signal frequency of 10 GHz, a |
| :--- | :--- | :--- |
| transistor has $S_{11}=0, S_{12}=0.2, S_{21}=2$ and |
| $S_{22}=0.8$, as defined with a 50 Ohm |
| impedance reference. |

part a, 5 points
Is the circuit unconditionally stable? Hint: examine the expressions for $\Gamma_{i n}$ and $\Gamma_{\text {out }}$ Yes/No: ?
part b, 5 points
Please draw a SOURCE stability circle

part c, 5 points
The transistor is connected to a 100 Ohm generator with 1 mW available power. The output of the transistor is impedance matched to the load. How much power will be delivered to the load?
load power =

## part d, 10 points

IF necessary, the transistor is stabilized, and is then impedance-matched to a 50 Ohm generator and a 50 Ohm load? If the generator has 1 mW available power, how much power will be delivered to the load?
load power $=$
part e, 10points

In the case of part $D$, above, if we consider the transistor, the possible stabilization network, and the matching networks to be, in combination, an amplifier, what are \|S21\|, $\|\mathrm{S} 11\|,\|\mathrm{S} 22\|,\|\mathrm{S} 12\|$ of the amplifier ?
||S11|| = $\qquad$
||S12|| = $\qquad$
||S21|| = $\qquad$
||S22|| $=$ $\qquad$
part f, 10 points (somewhat tricky, ece218c students only)

I now connect the amplifier of parts D and E to a 100 Ohm generator of 1 mW available power. The load is 25 Ohms. What is the power delivered to the load ?

Pload= $\qquad$

Problem 2, 25 points
Unconditionally stable and Potentially unstable amplifier design, gain circles
part a, 10 points
A MOSFET in common-source mode has $\|$ S11 $\|<1$ and $\mid$ S22 $\|>1$, and has stability circles (50Ohm reference impedance) as below.
In the boxes below, draw circuit diagrams of *two* methods of stabilizing the transistor.



## part b, 5 points

A transistor has available and operating gain circles as below. These are graphed in 1dB gain increments. The transistor MAG is 10 dB , and the transistor is unconditionally stable. (the stability circles have been updated)


What source and load impedances are required for 10 dB gain?
$\mathrm{Zs}=$ $\qquad$ $\mathrm{Zl}=$ $\qquad$
part c, 5 points
We continue with the transistor of part $\mathbf{B}$. If the generator impedance is 50 Ohms , and the load impedance is matched to the transistor output impedance, then what power gain will the transistor have?
Power gain $=$
part d, 5 points
We continue with the transistor of part B. If the load impedance is 500 hms , and the generator impedance is matched to the transistor input impedance, then what power gain will the transistor have?
Power gain $=$

## Problem 3, 20 points

$S$ parameters and Signal flow graphs
part a, 10 points
We have R1=100 Ohms and R2=50
Ohms
Given a 50 Ohm impedance reference, Find the four S-parameters of this network


S11= $\qquad$ S12= $\qquad$ S21= $\qquad$ , $\mathrm{S} 22=$ $\qquad$
part b, 10 points
We have a transistor having $\mathrm{S} 11=0.5, \mathrm{~S} 12=0.1, \mathrm{~S} 21=3, \mathrm{~S} 22=0.5$. We connect the network of part a to the transistor's INPUT. Please find S21 of the combined network

S 21 of the combined network $=$

Problem 4, 15 points (145A), 25 points (218A)
Power amplifier design (the graph is updated)


A FET has the common-source characteristics above, normalize to FET gate width. You can infer gm from the data above. We have $\mathrm{Ri}=1 / \mathrm{gm}$, and $f_{\tau}$ is 200 GHz . The signal frequency is 50 GHz
part a, 5 points
Assuming TEMPORARILY a 1 micron FET width, give the following.
$\mathrm{gm}=$ $\qquad$ , $\mathrm{Cgs}=$ $R i=$ $\qquad$

## part b, 10 points

When we attempt to design impedance-transformation networks, we have found that the minimum load impedance we can synthesize is 10 Ohms .
What FET width should we select ? $\mathrm{Wg}=$
What maximum undistorted output power will we obtain? Pout= What input power does this require ? Pin=
part c, 10 points

## 218A students ONLY

We want to combine the power of 4 such FETs. Draw circuit diagrams, with all element values given, of (1) the output matching network of an individual FET and (2) the output power-combining network.

