

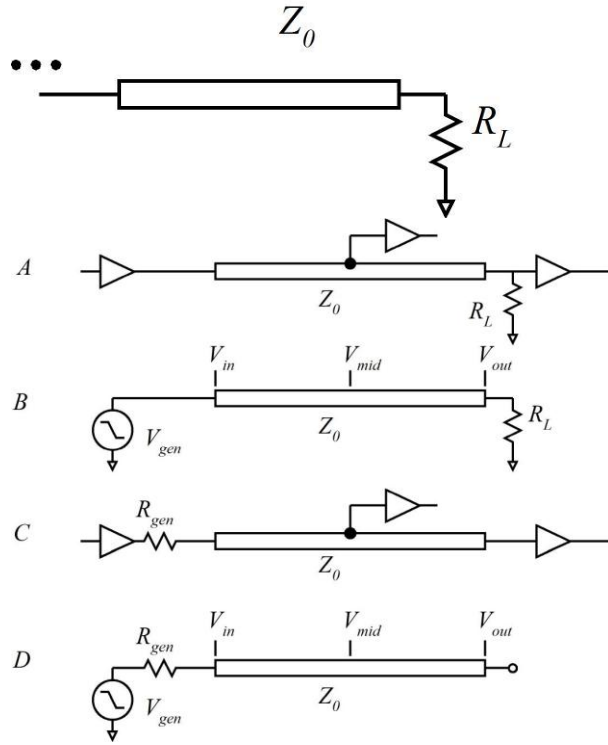
**ECE 145a /218A first problem set (basics of transmission lines and lumped elements)**

Problem 1: A transmission line has 50 Ohms characteristic impedance and a load impedance of (a) 25 Ohms (b) 50 Ohms (c) 100 Ohms. Compute in each case the voltage reflection coefficient.

Problem 2: lattice diagrams:  
Draw lattice diagrams for the 2 cases: (a/b) and (c/d), and draw clean plots of  $V_{in}$ ,  $V_{mid}$ , and  $V_{out}$ .

Case (a/b) logic gate with low (zero ohms) output impedance drives a 75 Ohm line of 5 cm length and  $10^8$  m/s propagation velocity. The equivalent circuit is in (b). The load impedance is 75 Ohms and  $V_{gen}$  is a 500 mV step-function.

Case (c/d) logic gate with 75 ohms output impedance drives the same line. The equivalent circuit is in (d). The load impedance is infinity and  $V_{gen}$  is a 500 mV step-function.



Comment on the relative utility of the 2 schemes for distributing logic signals using a transmission-line bus

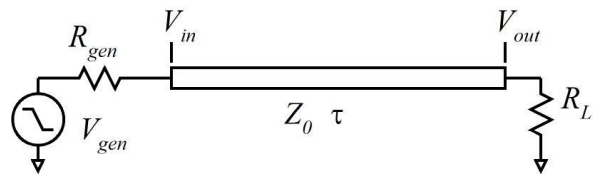
Problem 3: lumped-distributed relationships

In all cases:  $Z_0 = 100$  Ohms,  $\tau = l/v = 1$  ps, and  $V_{gen}$  is a 1 V step-function. For cases (a,b,c), Compute and plot  $V_{in}(t)$  using lattice diagram methods.

Case a:  $R_L = 1000$  Ohms,  $R_{gen} = 1000$  Ohms.

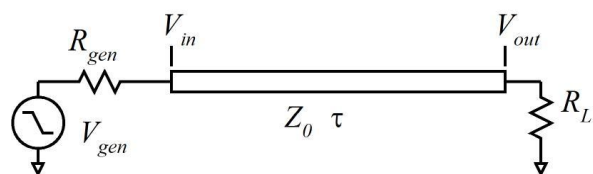
Problem 4: lumped-distributed relationships

In all cases:  $Z_0 = 100$  Ohms,  $\tau = l/v =$



Case b:  $R_L = 10$  Ohms,  $R_{gen} = 10$  Ohms.

Case c:  $R_L = 0$  Ohms,  $R_{gen} = 1000$  Ohms.



1 ps, and  $V_{gen}$  is a 1 V step-function.

For cases (a,b,c), replace the transmission-line with a T or Pi equivalent circuit, compute and plot  $V_{in}(t)$  using basic circuit analysis.

In (a) and (b) first compute L/R and RC time constants, and ignore either L or C if the associated time constant is more than 10:1 less than the dominant time constant.

**Problem 5: lumped-distributed relationships**

A transmission line (image C) has length  $l = 300$  microns and propagation velocity equal to the speed of light in vacuum.  $Z_o = 100$  Ohms. The plate vertical separation is 1 mm. Using approximate microstrip-line formulas, compute the *width* of the conductors.

This leads to the equivalent circuit (a) . From this, compute the line inductance and use this value in (b).

**Problem 6: lumped-distributed relationships**

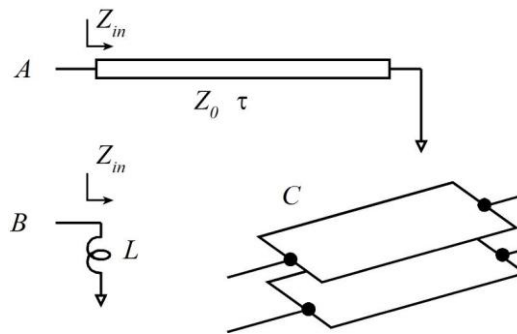
A transmission line (image C) has length  $l = 300$  microns and propagation velocity equal to the speed of light in vacuum.  $Z_o = 100$  Ohms.

This leads to the equivalent circuit (a) . From this, compute the line capacitance and use this value in (b).

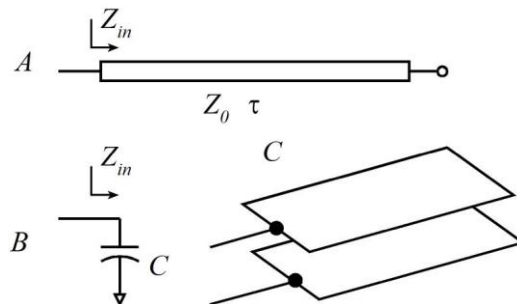
Case a:  $R_L = 1000$  Ohms,  $R_{gen} = 1000$  Ohms.

Case b:  $R_L = 10$  Ohms,  $R_{gen} = 10$  Ohms.

Case c:  $R_L = 0$  Ohms,  $R_{gen} = 1000$  Ohms.



Using the Smith chart, make a quantitative graph comparing  $Z_{in}$  of cases (a) and (b) over a frequency range extending from DC to  $f = 1/\tau = v/l$



Using the Smith chart, make a quantitative graph comparing  $Z_{in}$  of cases (a) and (b) over a frequency range extending from DC to  $f = 1/\tau = v/l$