

ECE 124a/256c



Transmission Lines as Interconnect

Forrest Brewer

Displays from Bakoglu, Addison-Wesley

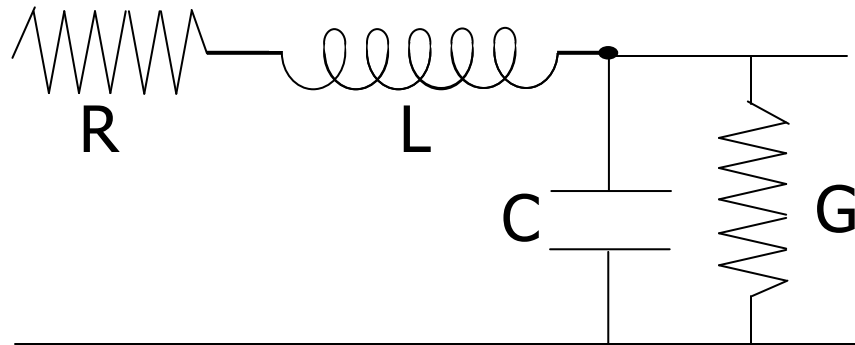


Interconnection

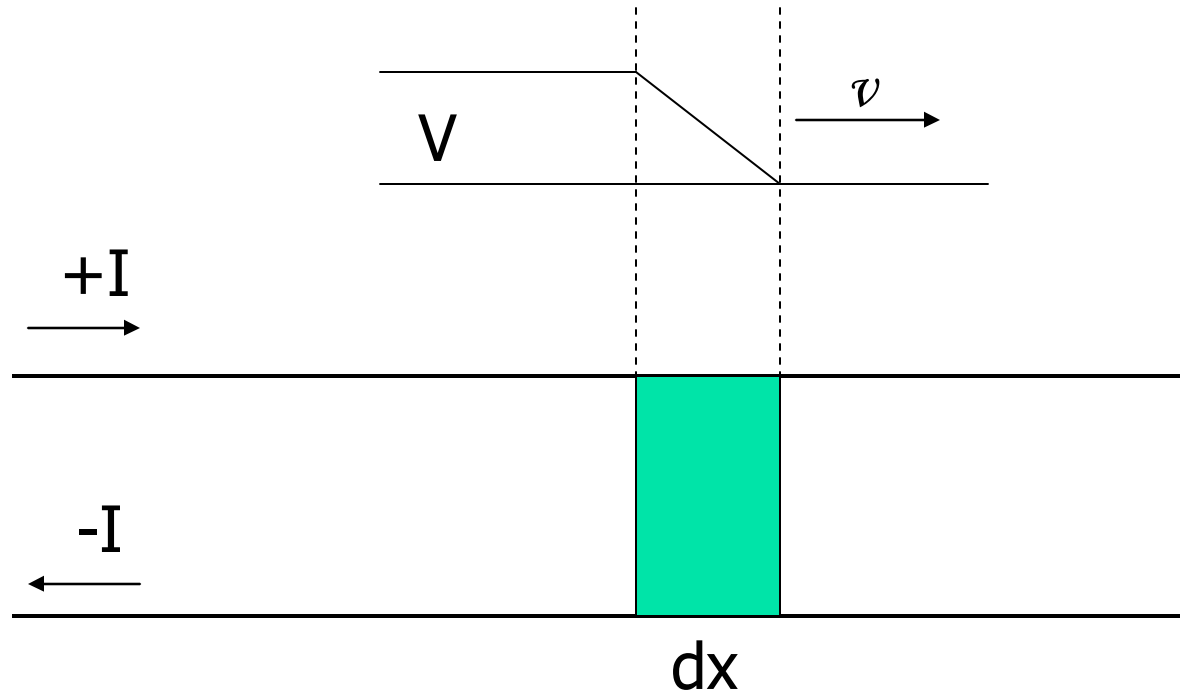
- Circuit rise/fall times approach or exceed speed of light delay through interconnect
- Can no longer model wires as C or RC circuits
- Wire Inductance plays a substantial part
- Speed of light: $1\text{ft/nS} = 300\text{um/pS}$

Fundamentals

- $L \, di/dt = V$ is significant to other effects
- Inductance: limit on the rate of change of the current
- E.g. Larger driver will not cause larger current to flow initially



Lossless Transmission $R=G=0$



- Step of V volts propagating with velocity v
- Initially no current flows – after step passes, current of $+I$
- After Step Voltage V exists between the wires



Lossless Transmission $R=G=0$

- Maxwell's equation: $\Phi = \iint_S B \cdot dS$
- B is field, dS is the normal vector to the surface
- Φ is the flux
- For closed surface Flux and current are proportional

$$L = \frac{\Phi}{I}$$



Lossless Transmission $R=G=0$

- For Transmission Line I and Φ are defined per unit length
- At front of wave: $d\Phi = d(IL) = ILdx$
- Faraday's Law: $V = d\Phi/dt = IL dx/dt = ILv$
- Voltage in line is across a capacitance $Q=CV$
- It must be: $I = \frac{dQ}{dt} = \frac{d(CV)}{dt} = CV \frac{dx}{dt} = CVv$
- Combining, we get: $v = \frac{1}{\sqrt{LC}}$
- Also: $Z = \frac{V}{I} = \sqrt{\frac{L}{C}}$



Units

- The previous derivation assumed $\epsilon = \mu = 1$

- In MKS units:
$$v = \frac{1}{\sqrt{\epsilon\mu}} = \frac{c}{\sqrt{\epsilon_r\mu_r}}$$

- c is the speed of light = 29.972cm/nS

- For typical IC materials $\mu_r = 1$

- So:
$$Z_0 = \frac{\sqrt{\epsilon_r}}{cC} \quad L = \frac{\epsilon_r}{c^2C}$$

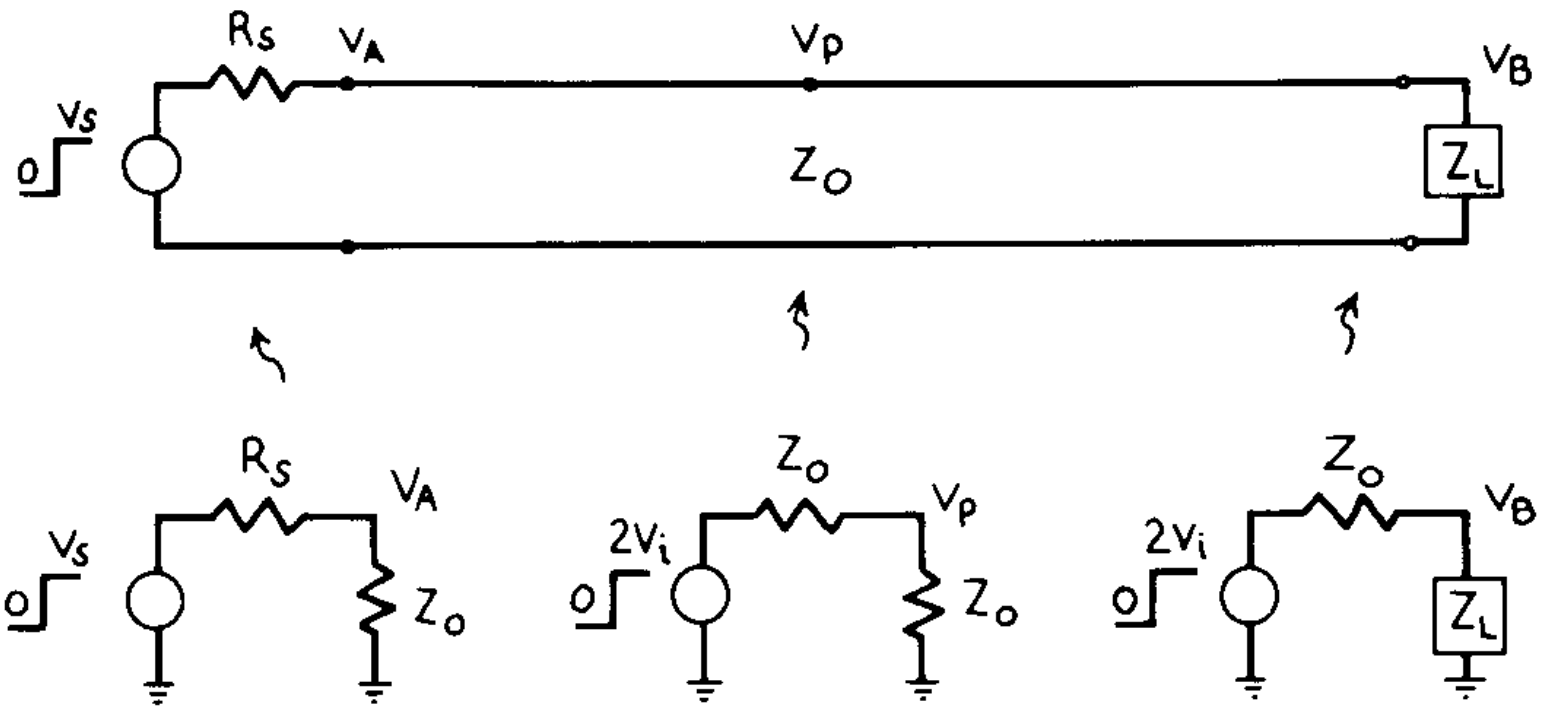


Typical Lines

- We can characterize a lossless line by its Capacitance per unit length and its dielectric constant.

Material	Dielectric Constant	Propagation Velocity
Polymide	2.5-3.5	16-19 cm/nS
SiO ₂	3.9	15
Epoxy PC	5.0	13
Alumina	9.5	10

Circuit Models





Circuit Models II

- Driver End

- TM modeled by resistor of value Z

- Input voltage is function of driver and line impedance: $V_{line} = \frac{Z}{R_s + Z} V_s$

- Inside Line

- Drive modeled by Step of $2V_i$ with source resistance Z

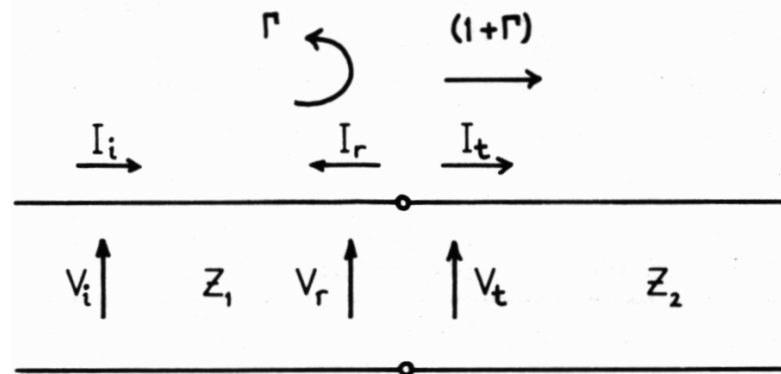
- Remaining TM as above (resistor)

- Load End

- Drive modeled by Step of $2V_i$ with source resistance Z

- Voltage on load of impedance Z_L : $V_L = \frac{Z_L}{Z + Z_L} 2V_i$

Discontinuity in the line (Impedance)



- Abrupt interface of 2 TM-lines

- Incident wave: $V_i = I_i Z_1$ Reflected Wave: $V_r = I_r Z_1$

- Transmitted Wave: $V_t = I_t Z_2$

- Conservation of charge: $I_i = I_r + I_t$

- Voltages across interface: $V_i + V_r = V_t$

- We have: $\frac{V_i}{Z_1} = \frac{V_r}{Z_1} + \frac{V_t}{Z_2}$ $V_r = V_i \frac{Z_2 - Z_1}{Z_2 + Z_1}$ $V_t = V_i \frac{2Z_2}{Z_2 + Z_1}$

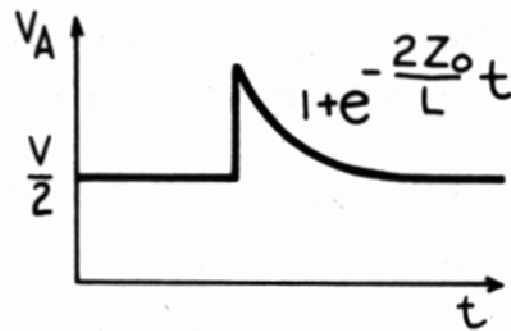
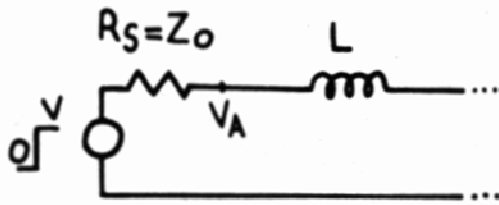


Reflection/Transmission Coefficients

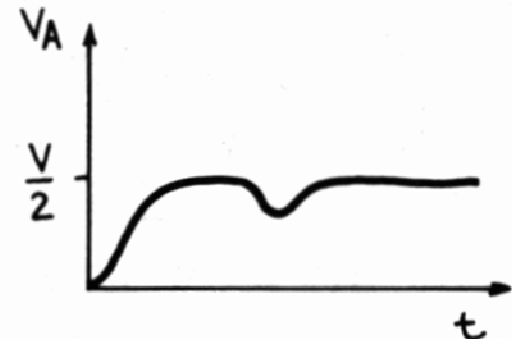
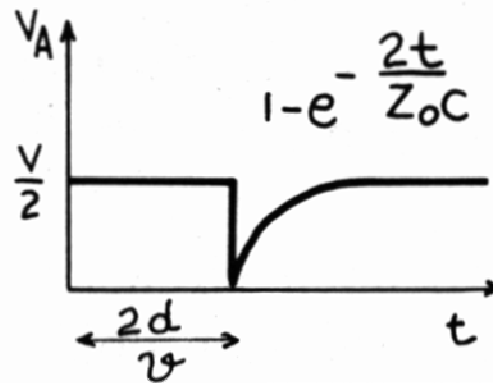
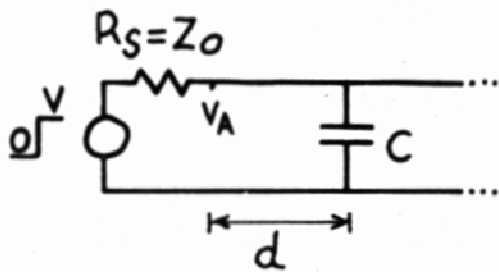
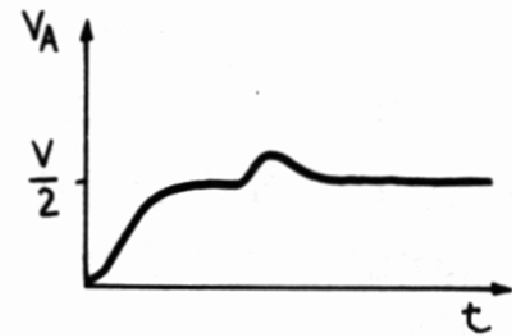
- The Coefficient of Reflection $\Gamma = V_r/V_i = \frac{Z_2 - Z_1}{Z_2 + Z_1}$
- V_i incident from Z_1 into Z_2 has a reflection amplitude Γv_i
- Similarly, the Transmitted Amplitude = $1 + \Gamma = \frac{2Z_2}{Z_1 + Z_2}$

Inductive and Capacitive Discontinuities

DISCONTINUITY



FINITE RISE TIME





Typical Package Pins

Package	Capacitance (pF)	Inductance (nH)
40 pin DIP (plastic)	3.5	28
40 pin DIP (Ceramic)	7	20
68 pin PLCC	2	7
68 pin PGA	2	7
256 pin PGA (with gnd plane)	5	15
Wire bond (per mm)	1	1
Solder Bump	0.5	0.5



Discontinuity Amplitude

- The Amplitude of discontinuity
 - Strength of discontinuity
 - Rise/Fall time of Impinging Wave

- To first order Magnitude is:

- Inductive: $V_{peak} = \frac{L_D V_i}{2Zt_r}$ Capacitive: $V_{peak} = -\frac{C_D Z V_i}{2t_r}$

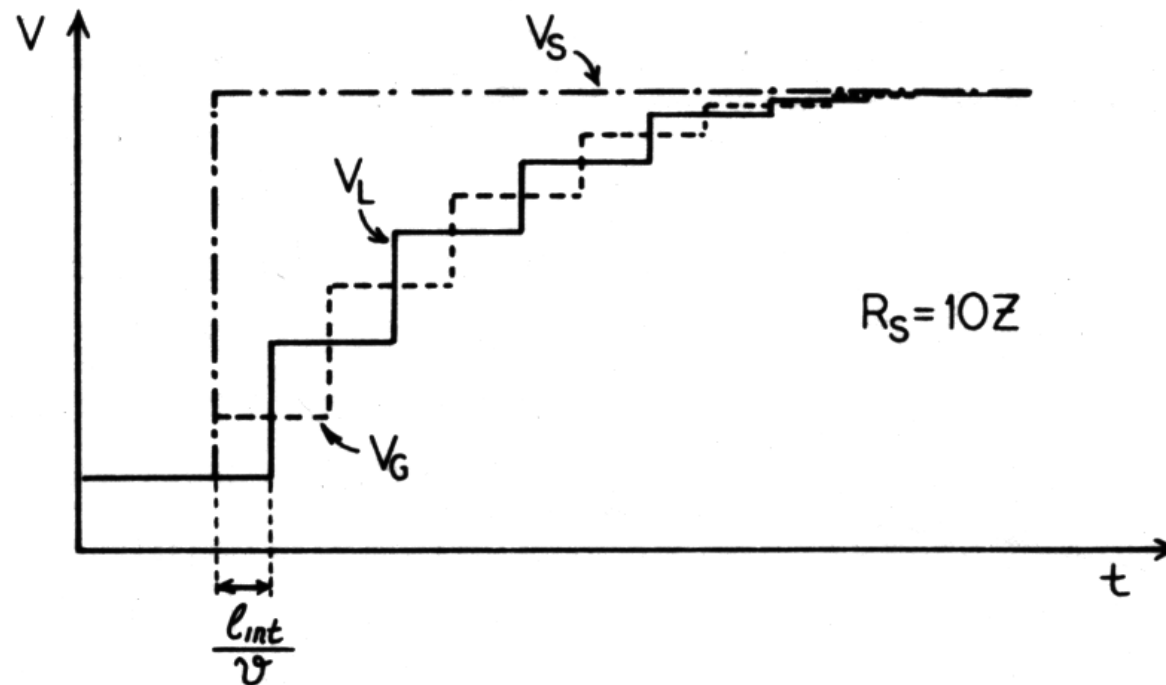
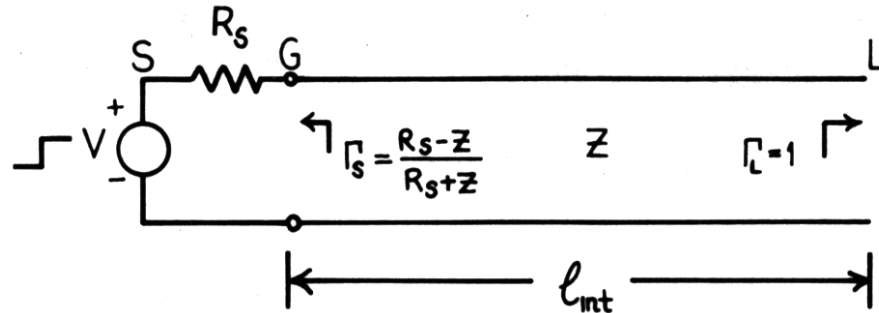
Critical Length (TM-analysis?)

- TM-line effects significant if: $t_r < 2.5 t_f$
- Flight time $t_f = d/v = \frac{d\sqrt{\epsilon_r}}{c}$

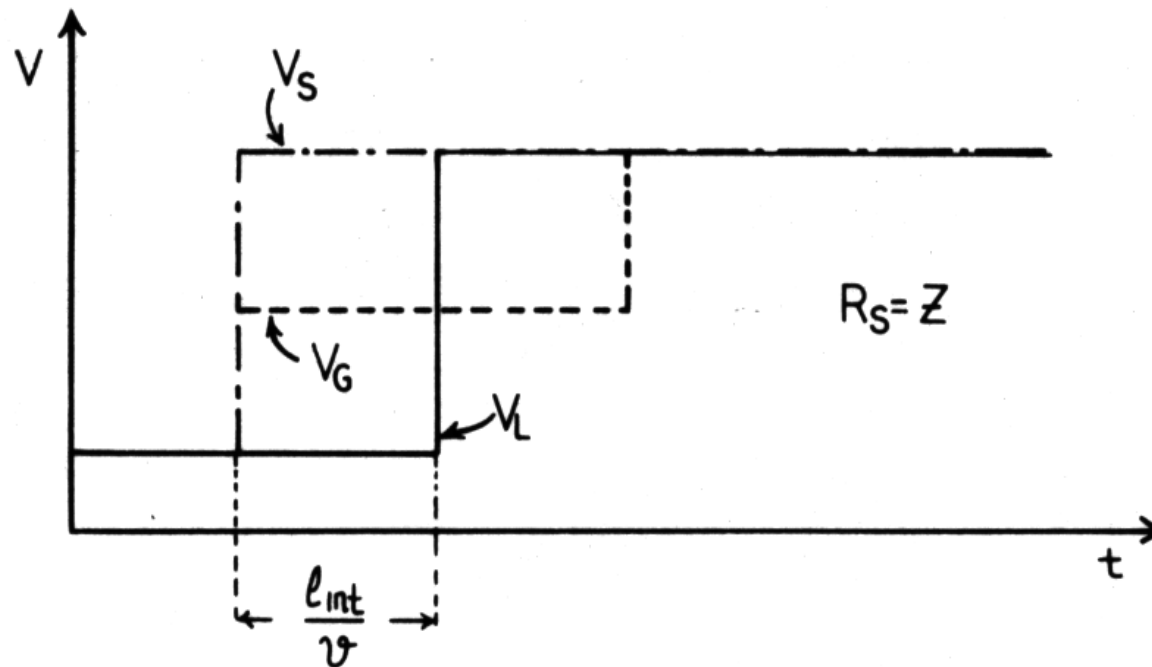
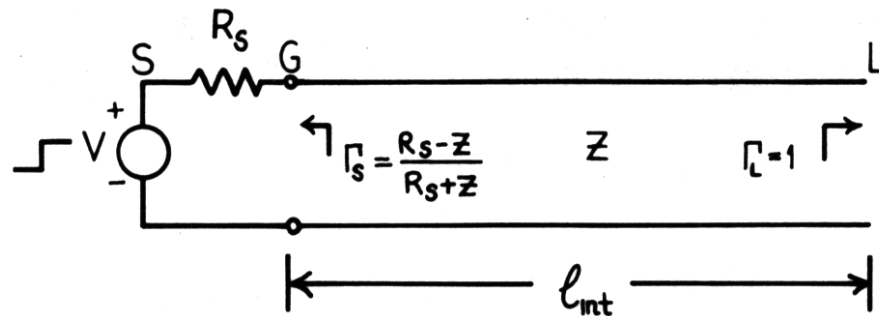
Rise Time (pS)	Critical Length (15 cm/nS)
25	150 μ m
75	0.45
200	1.3
500	3.0
1000	6.0
2000	12.0

Technology	On-Chip Rise time	Off-Chip Rise time
CMOS (0.1)	18-70pS	200-2000pS
GaAs/ SiGe/ (ECL)	2-50pS	8-300pS

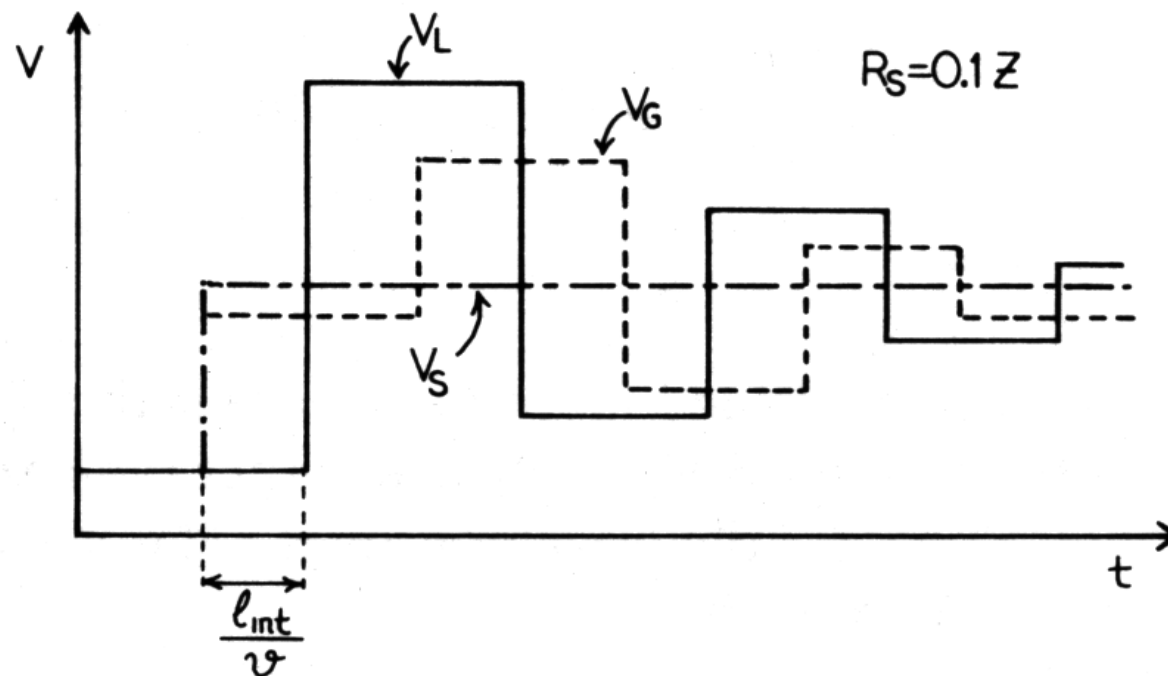
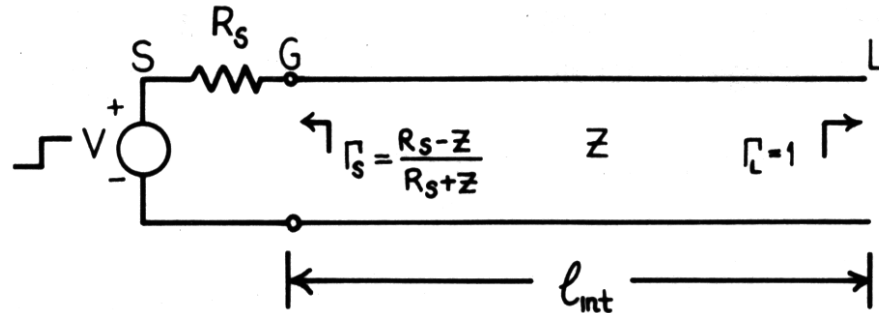
Un-terminated Line $R_s = 10Z$



Un-terminated Line $R_s = Z$

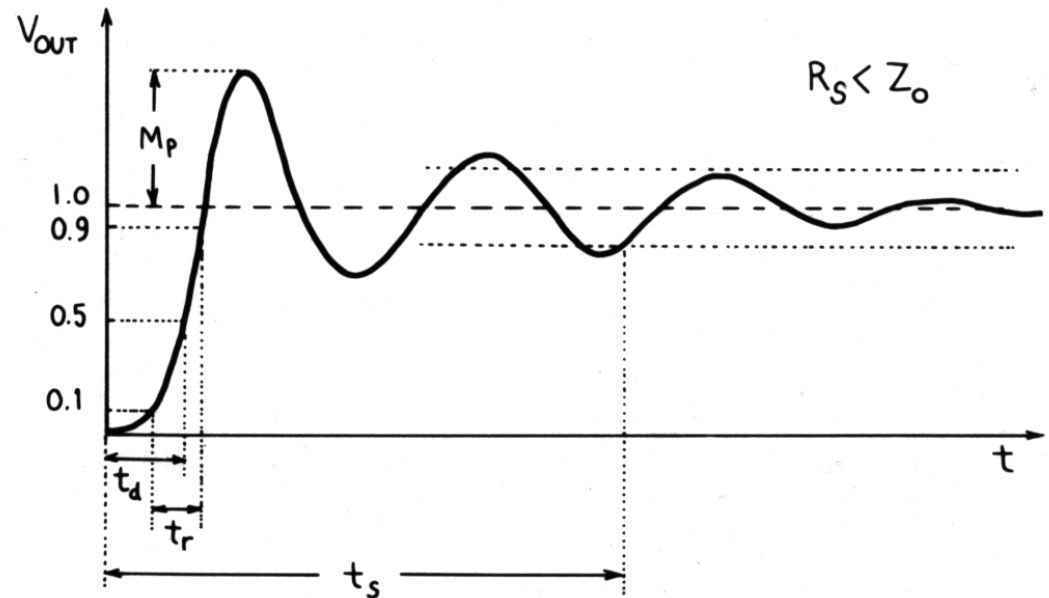
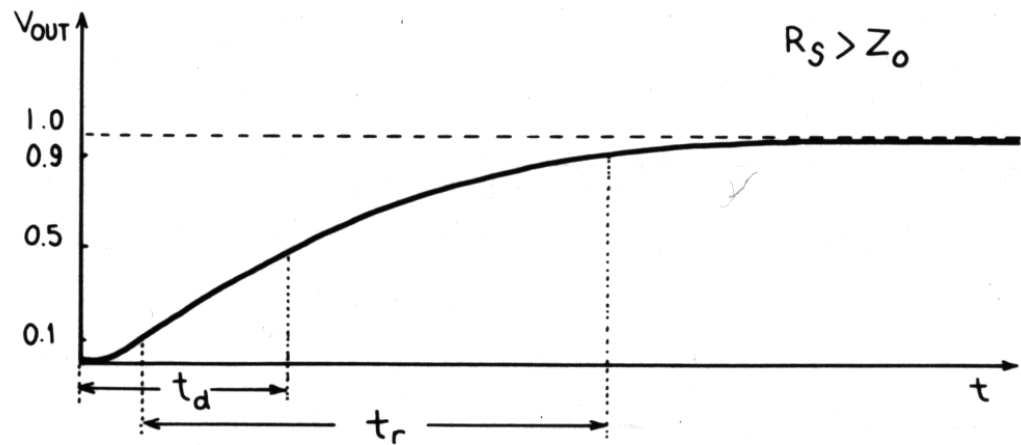


Un-terminated Line $R_s = 0.1Z$

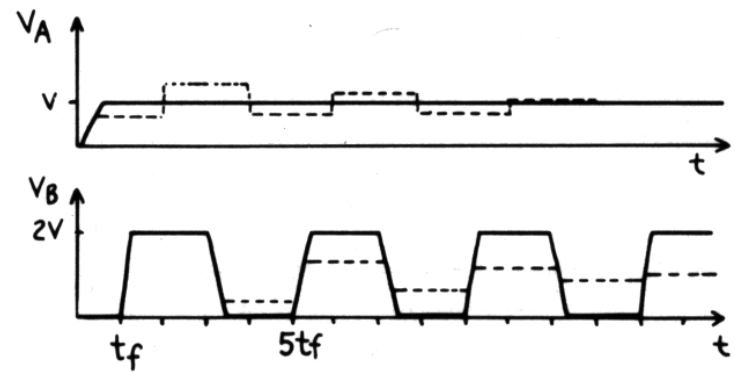
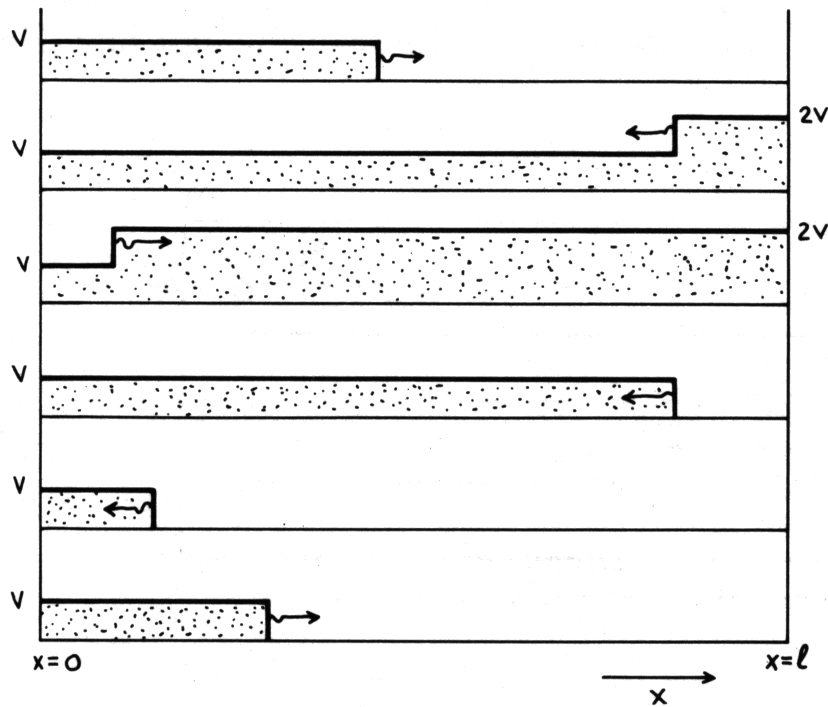
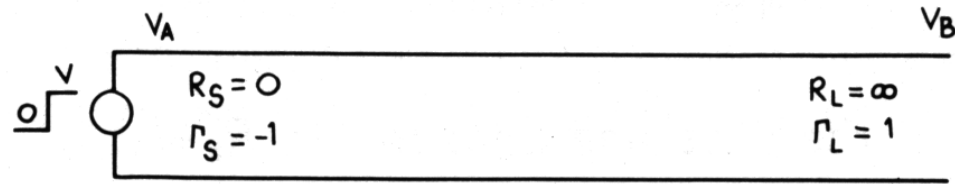


Unterminated Line (finite rise time)

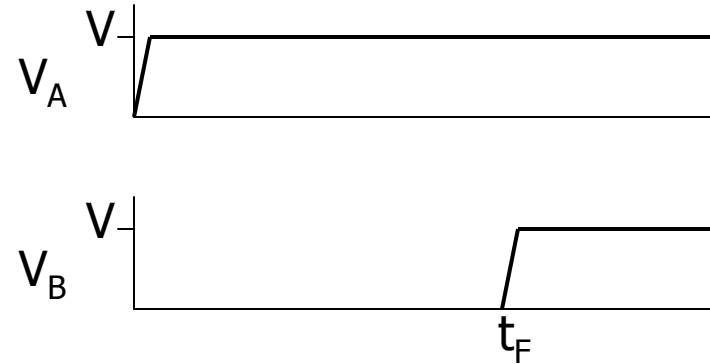
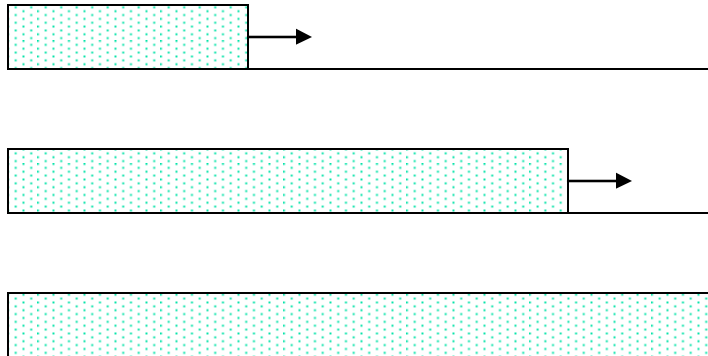
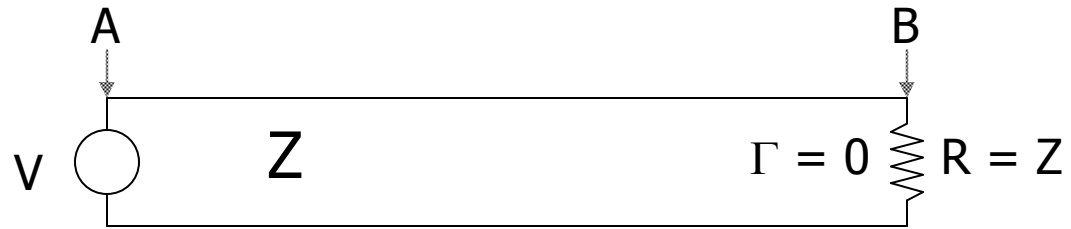
- Rise Time **Never** Zero
- For
- $R_s > Z_0$, $t_r > t_f$
 - Exponential Rise
- $R_s < Z_0$, $t_r \approx t_f = l/v$
 - “Ringing”
 - Settling time can be much longer than t_f .



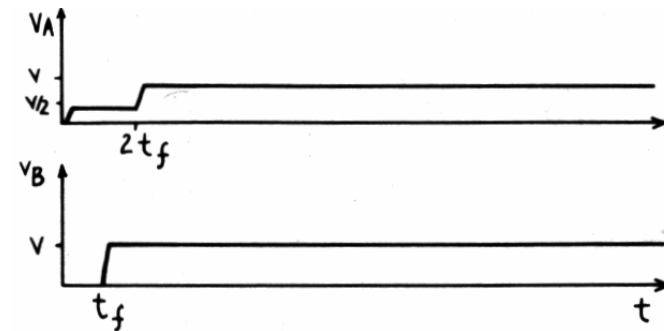
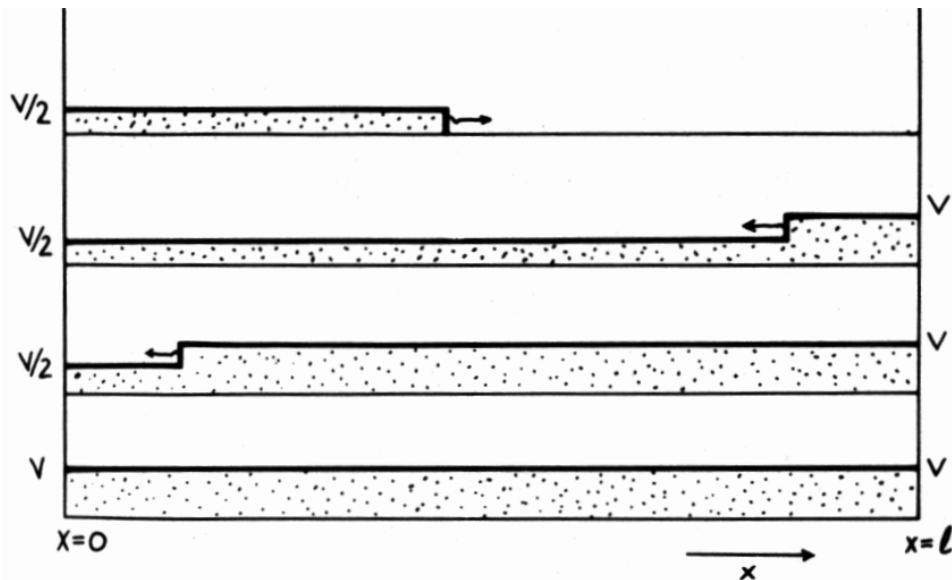
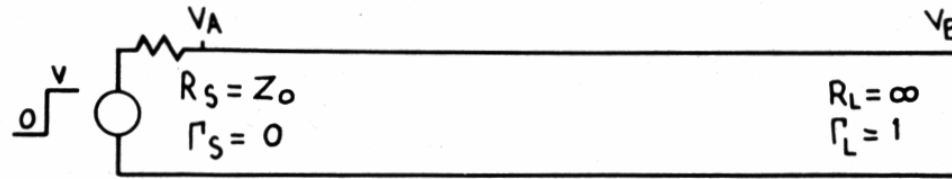
Line Termination (None)



Line Termination (End)

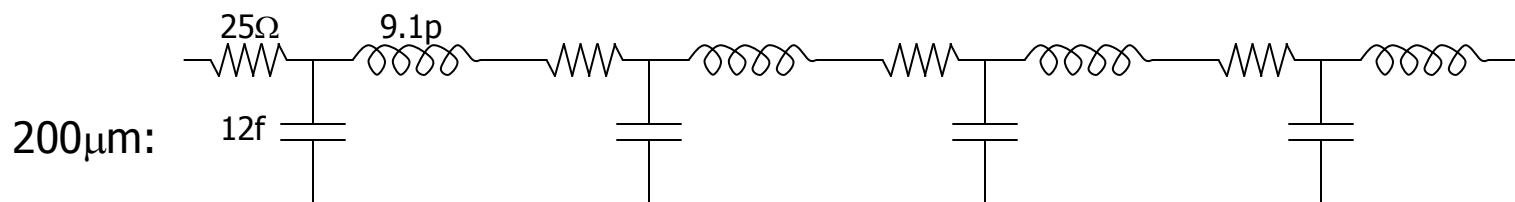


Line Termination: (Source)



Piece-Wise Modeling

- Create a circuit model for short section of line
 - Length < rise-time/3 at local propagation velocity
 - E.G. 50 μm for 25pS on chip, 150nm wide, 350nm tall
- Assume sea of dielectric and perfect ground plane (this time)
 - $C = 2.4\text{pF/cm} = 240\text{fF/mm} = 12\text{fF}/50\mu\text{m}$
 - $L = 3.9/c^2C = 1.81\text{nH/cm} = 0.181\text{nH/mm} = 9.1\text{pH}/50\mu\text{m}$
 - $R = \rho L/(W H) =$
 $0.005\text{cm} * 2.67\mu\Omega\text{cm}/(0.000015\text{cm} * 0.000035\text{cm}) = 25\Omega/50\mu\text{m}$





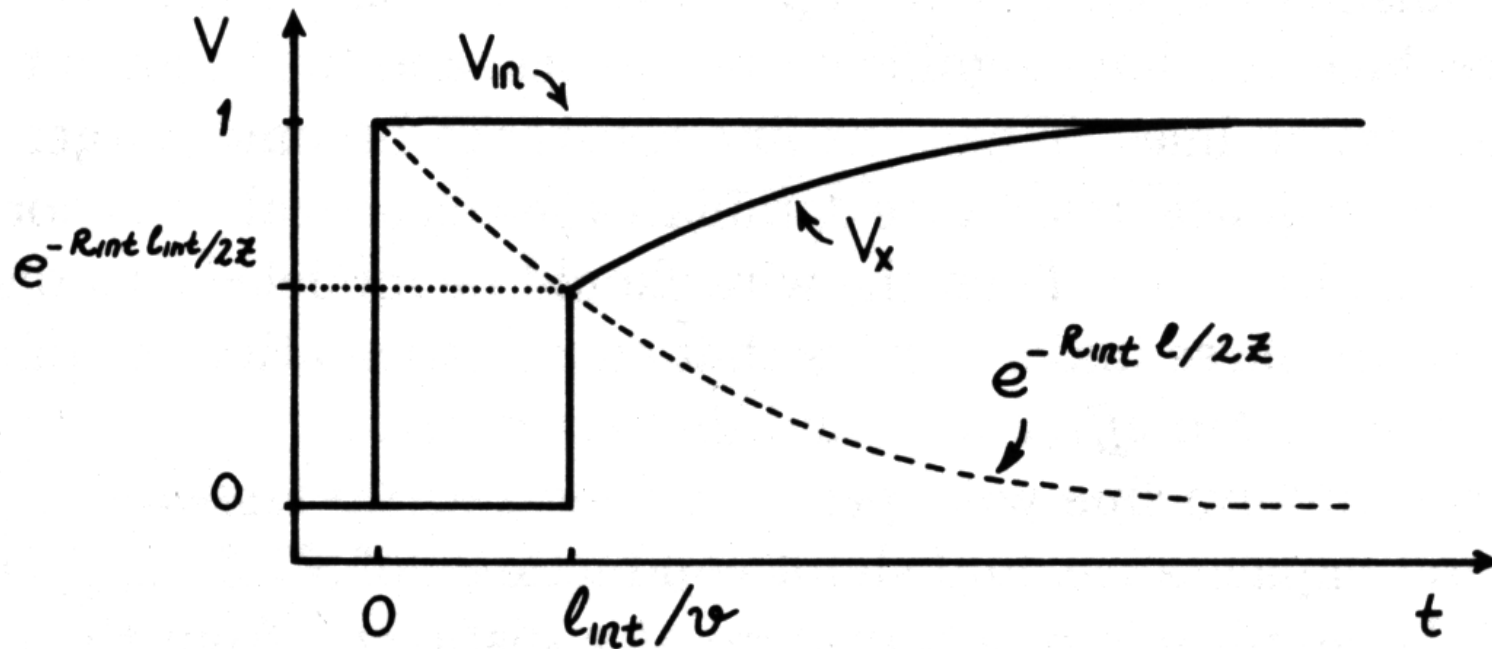
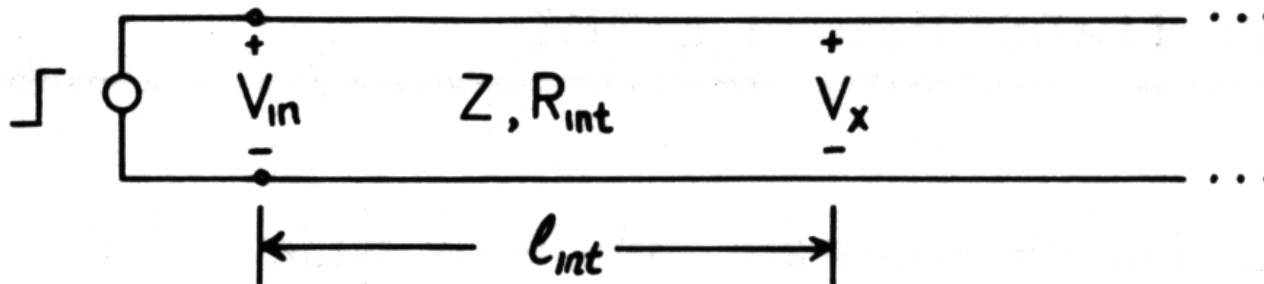
Lossy Transmission

- Attenuation of Signal
 - Resistive Loss, Skin-Effect Loss, Dielectric Loss
- For uniform line with constant R, L, C, G per length:

$$\frac{V(x=l)}{V(x=0)} = e^{-\alpha l}$$

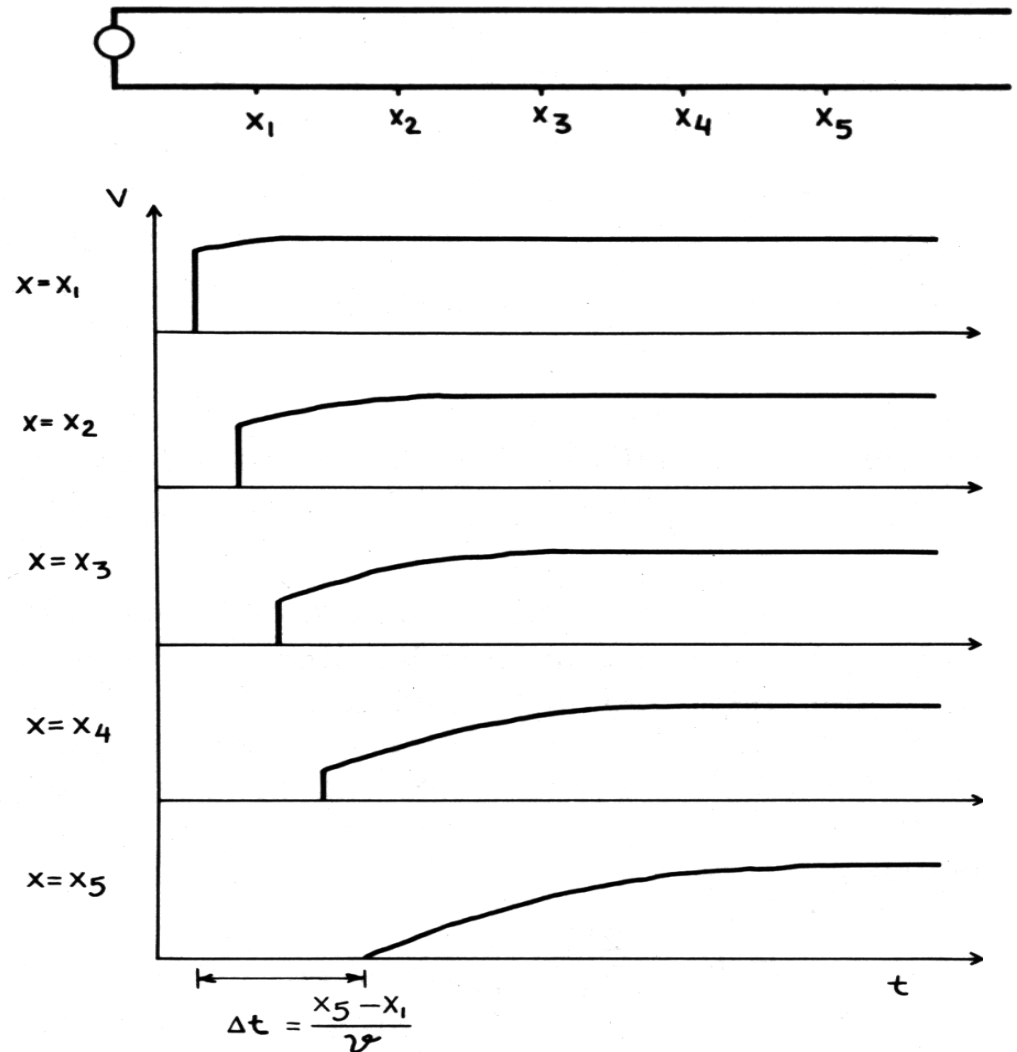
$$\alpha = \alpha_R + \alpha_G = \frac{R}{2} \sqrt{\frac{C}{L}} + \frac{G}{2} \sqrt{\frac{L}{C}} = \frac{R}{2Z_0} + \frac{GZ_0}{2}$$

Conductor Loss (Resistance)



Conductor Loss (step input)

- Initial step declines exponentially as $R\ell/2Z$
- Closely approximates RC dominated line when $R\ell \gg 2Z$
- Beyond this point, line is diffusive
- For large resistance, we cannot ignore the backward distributed reflection

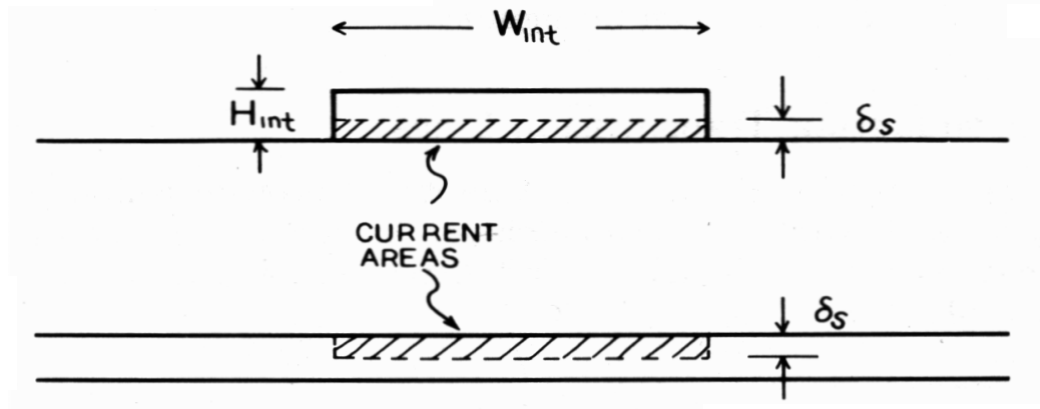




Conductor Loss (Skin Effect)

- An ideal conductor would exclude any electric or magnetic field change – most have finite resistance
- The depth of the field penetration is mediated by the frequency of the wave – at higher frequencies, less of the conductor is available for conducting the current
- For resistivity ρ (Ωcm), frequency f (Hz) the depth is: $\delta = \sqrt{\frac{\rho}{\pi\mu f}}$
- A conductor thickness $t > 2\delta$ will not have significantly lower loss
- For Al at 1GHz skin depth is $2.8\mu\text{m}$

Skin Effect in stripline (circuit board)



- Resistive attenuation: $\alpha = R / 2Z = \frac{\rho}{2WHZ}$
- At high frequencies: $\alpha = \frac{2R_{skin}}{2Z} = \frac{\rho}{W\delta Z} = \frac{\sqrt{\pi\mu f\rho}}{WZ}$



Dielectric Loss

- Material Loss tangent: $\tan \delta_D = \frac{G}{\omega C} = \frac{\sigma_D}{\omega \epsilon_r}$

- Attenuation:
$$\begin{aligned}\alpha_D &= \frac{GZ}{2} \\ &= \pi f C \tan \delta_D \sqrt{L/C} \\ &= \pi f \tan \delta_D \sqrt{LC} \\ &= \pi / c \sqrt{\epsilon_r} \tan \delta_D\end{aligned}$$