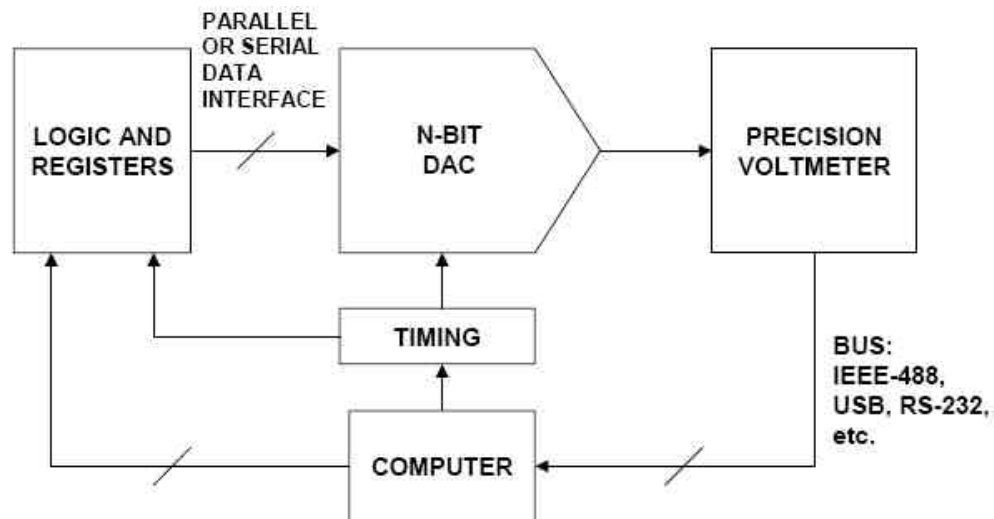
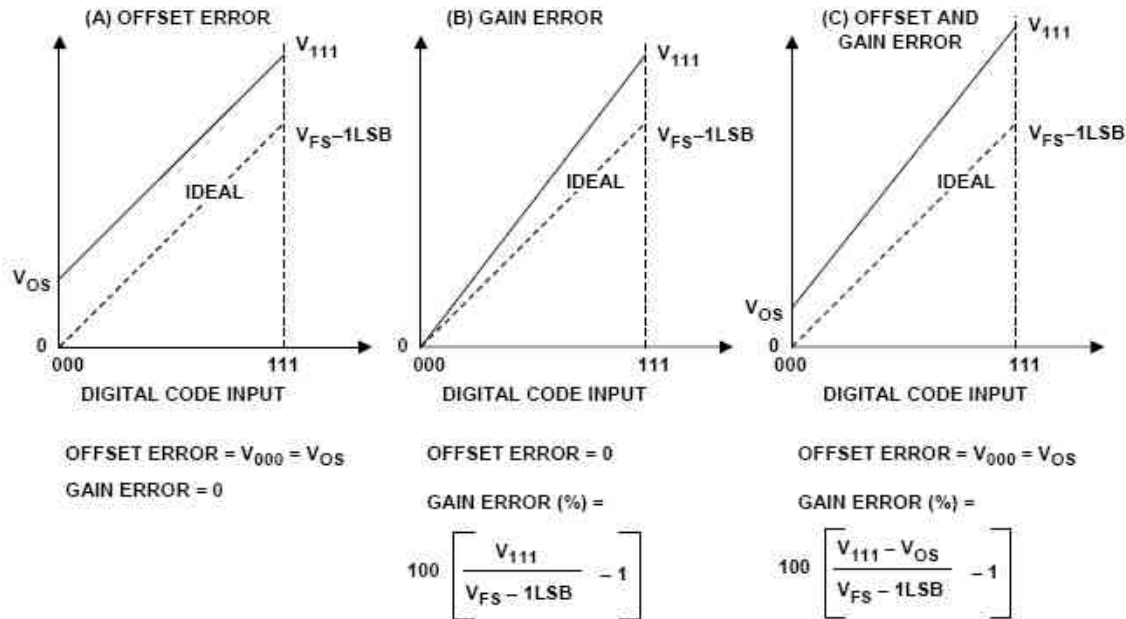


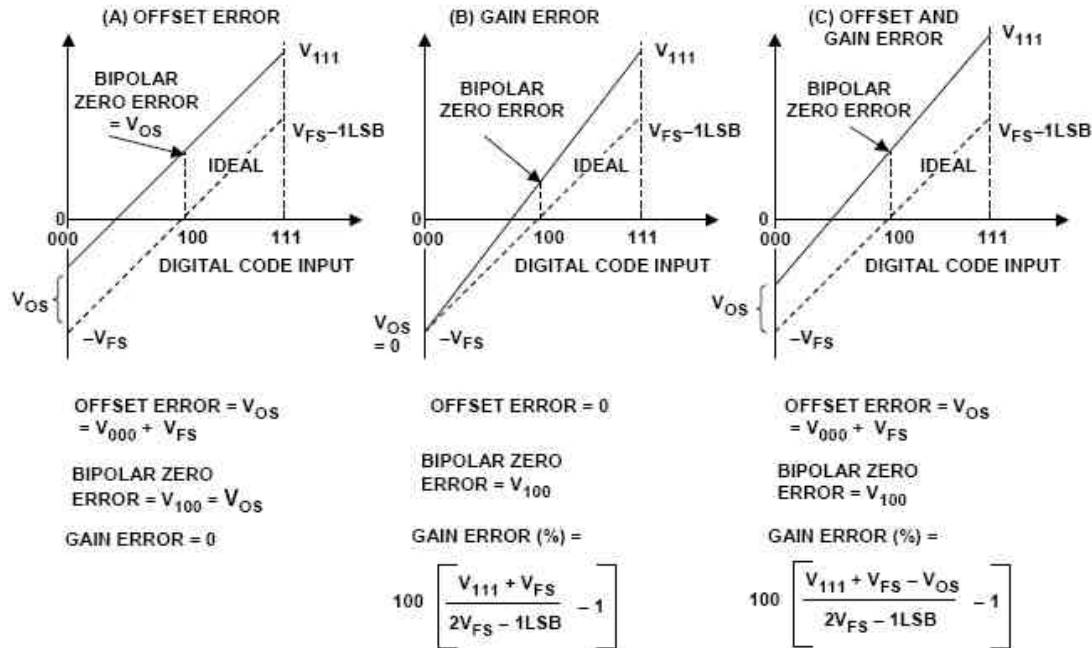
**Notes**

**Figure 5.1:** Basic Test Setup for Measuring DAC Static Transfer Characteristics

**Notes**

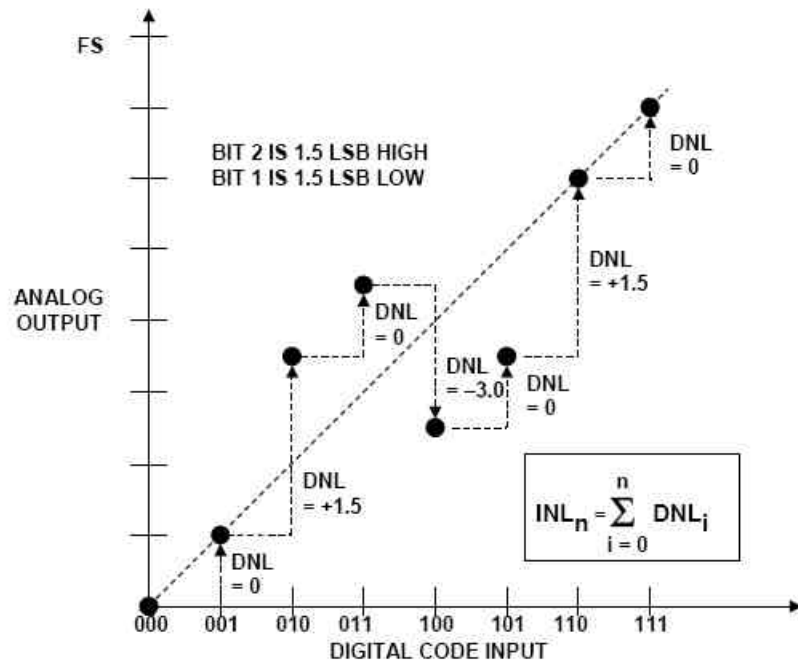
**Figure 5.2: Measuring Offset and Gain Error in a Unipolar DAC**

**Notes**

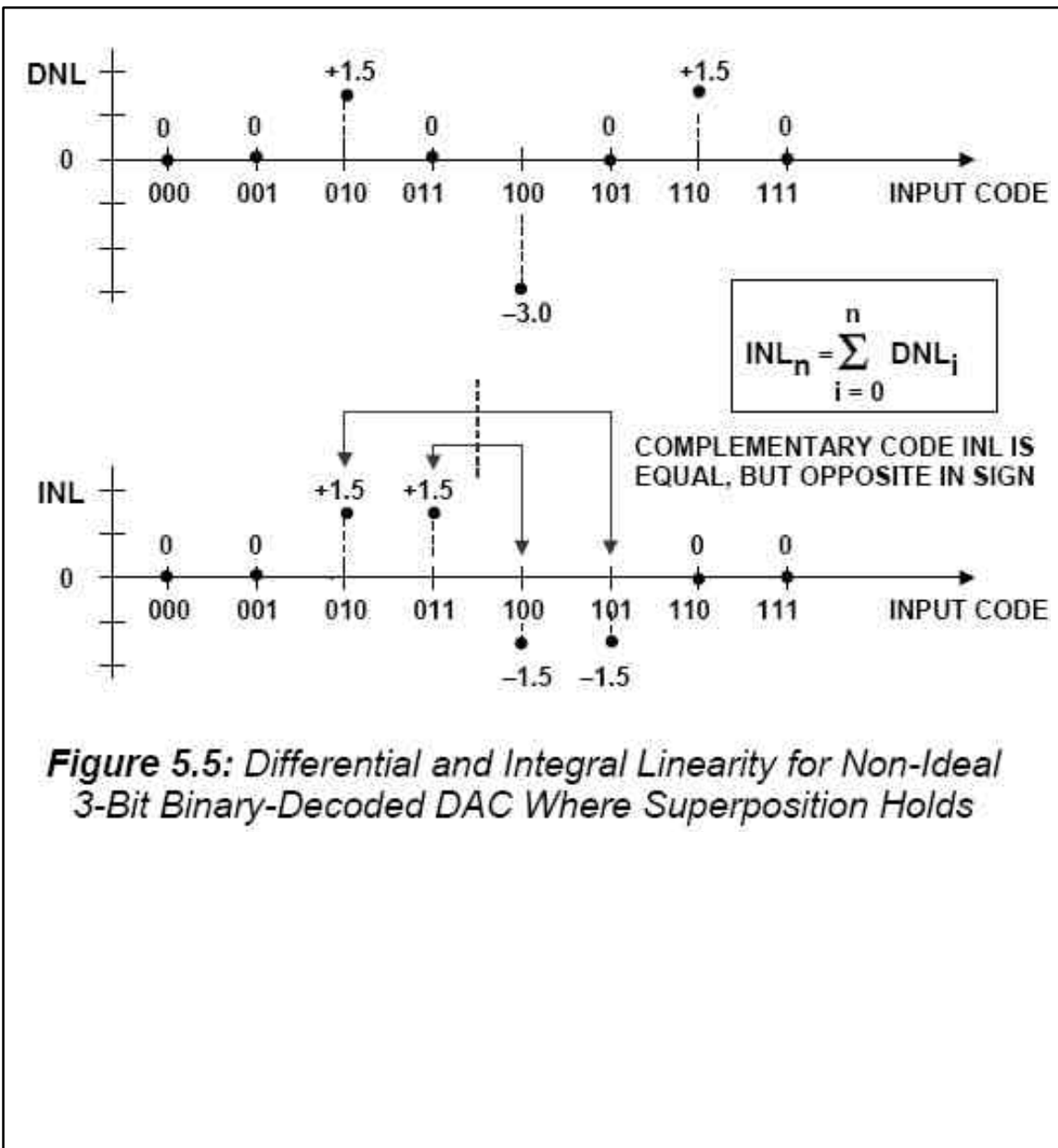


**Figure 5.3: Measuring Offset, Bipolar Zero, and Gain Error in a Bipolar DAC**

**Notes**

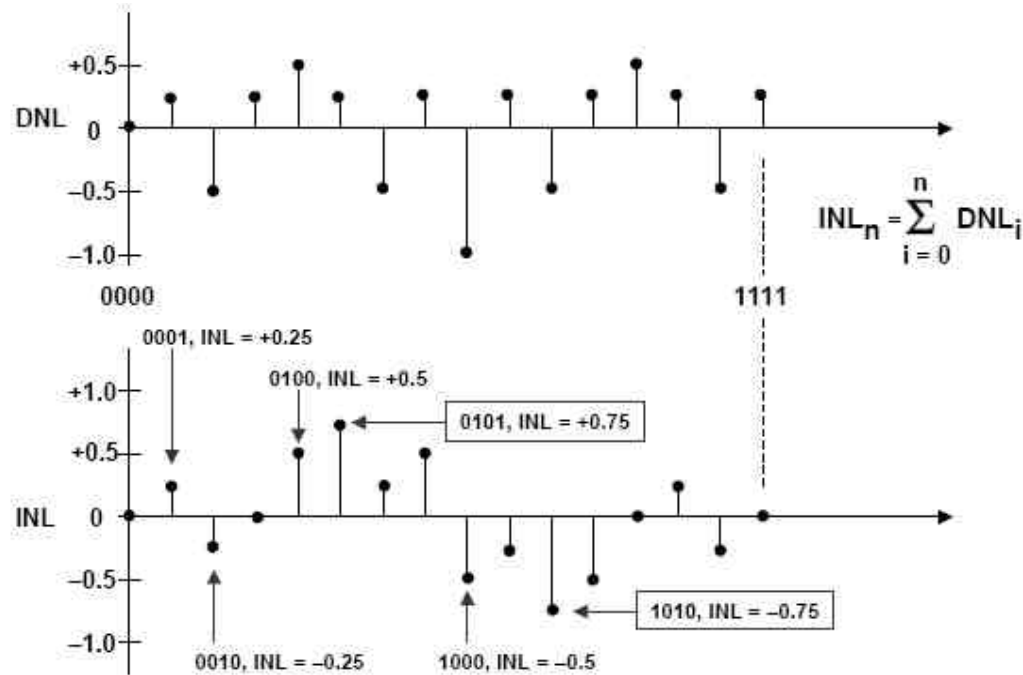


**Figure 5.4:** Non-Ideal 3-Bit DAC Transfer Function Where Superposition Holds

**Notes**

**Figure 5.5: Differential and Integral Linearity for Non-Ideal 3-Bit Binary-Decoded DAC Where Superposition Holds**

**Notes**



**Figure 5.6: DNL and INL for 4-Bit DAC Where Superposition Holds**

**Notes**

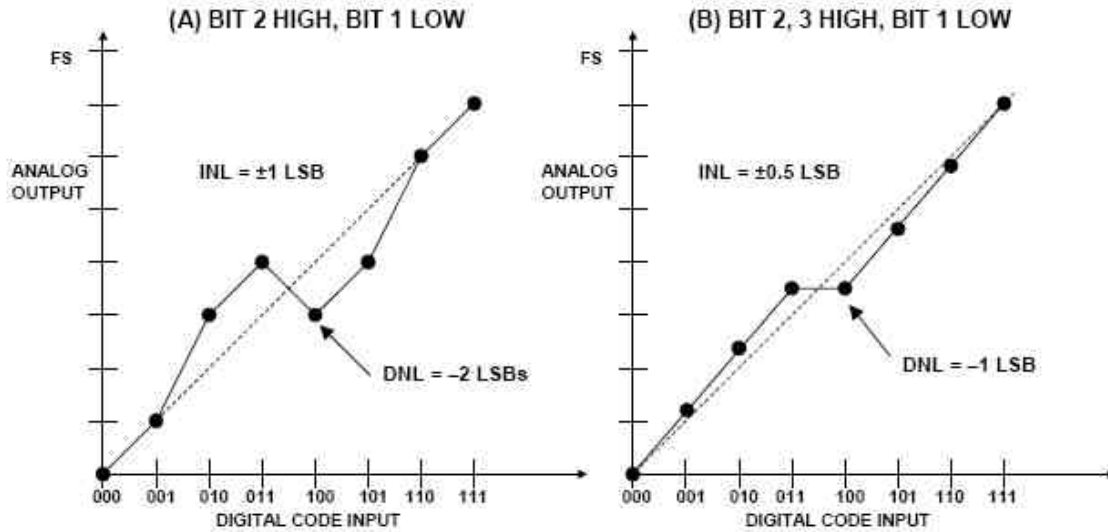
$$\text{CHECK BIT SUM: } V_{1111} = V_{0000} + V_{0001} + V_{0010} + V_{0100} + V_{1000}$$

$$1 \text{ LSB} = \frac{V_{1111} - V_{0000}}{15}$$

|               |                     |  |  |
|---------------|---------------------|--|--|
|               | 1111 = $V_{1111}$   |  |  |
| BIT<br>ERRORS | →                   | 1000 = $V_{1000}$                              | } DNL4 = $V_{1000} - V_{0111} - 1 \text{ LSB}$ |
|               |                     | 0111 = $V_{0111}$                              |  |
|               | →                   | 0100 = $V_{0100}$                              | } DNL3 = $V_{0100} - V_{0011} - 1 \text{ LSB}$ |
|               |                     | 0011 = $V_{0011}$                              |  |
| →             | 0010 = $V_{0010}$   | } DNL2 = $V_{0010} - V_{0001} - 1 \text{ LSB}$ |  |
|               | 0001 = $V_{0001}$   |  |  |
|               | 0000 = $V_{0000}$   | } DNL1 = $V_{0001} - V_{0000} - 1 \text{ LSB}$ |  |
|               | $V_{OS} = V_{0000}$ |  |  |

**Figure 5.7: Major-Carry Bit Tests for 4-Bit Binary-Decoded DAC Where Superposition Holds**

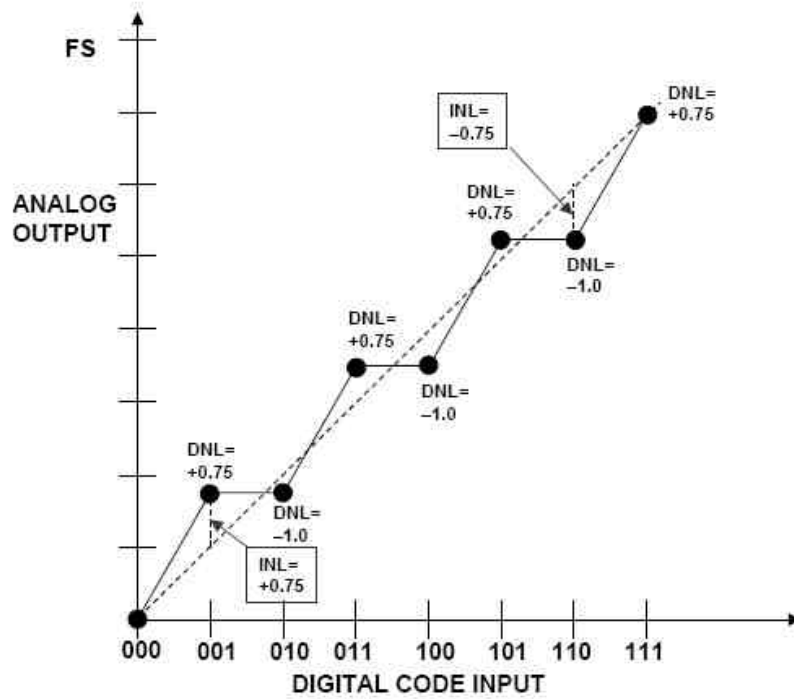
**Notes**



**Figure 5.8: Linearity Errors in Binary-Decoded 3-Bit DACs Where Superposition Holds**

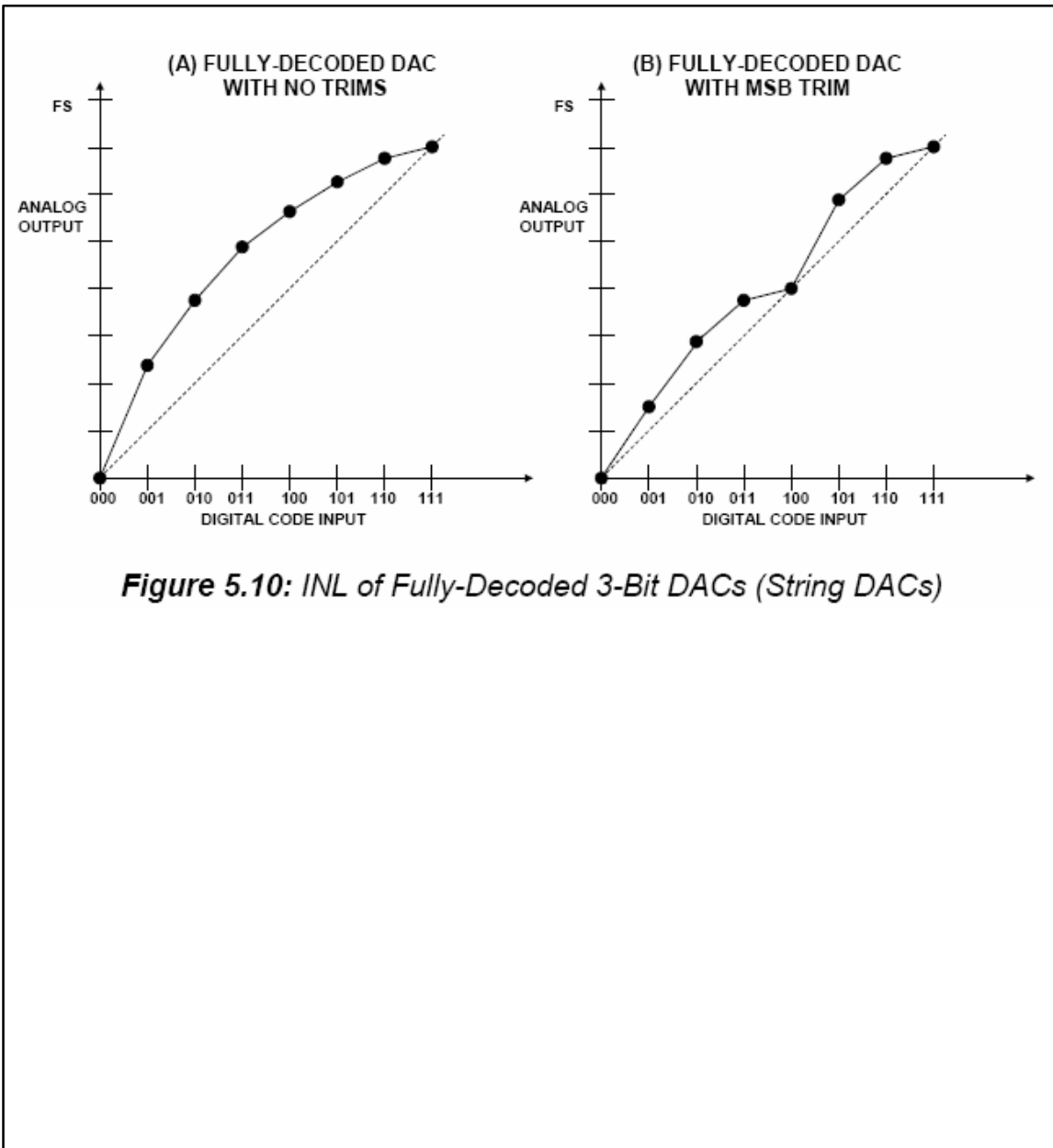


**Notes**

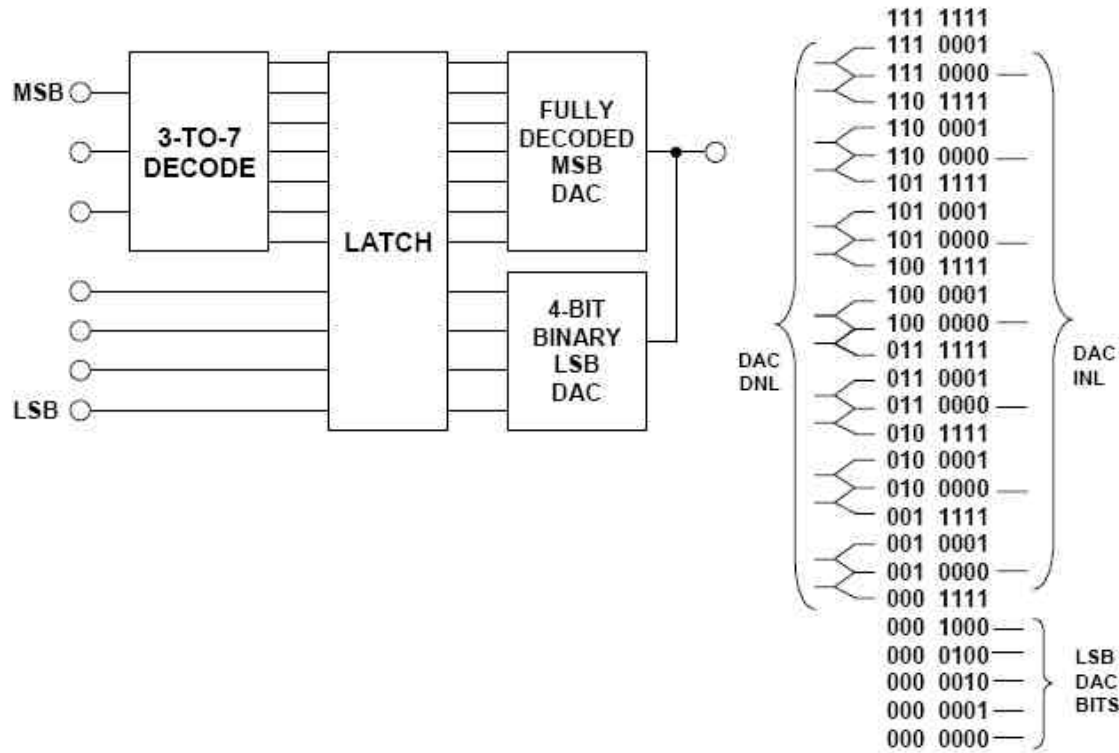


**Figure 5.9: DNL Specification of  $\pm 1$  LSB Does Not Guarantee INL  $< \pm 0.5$  LSB**

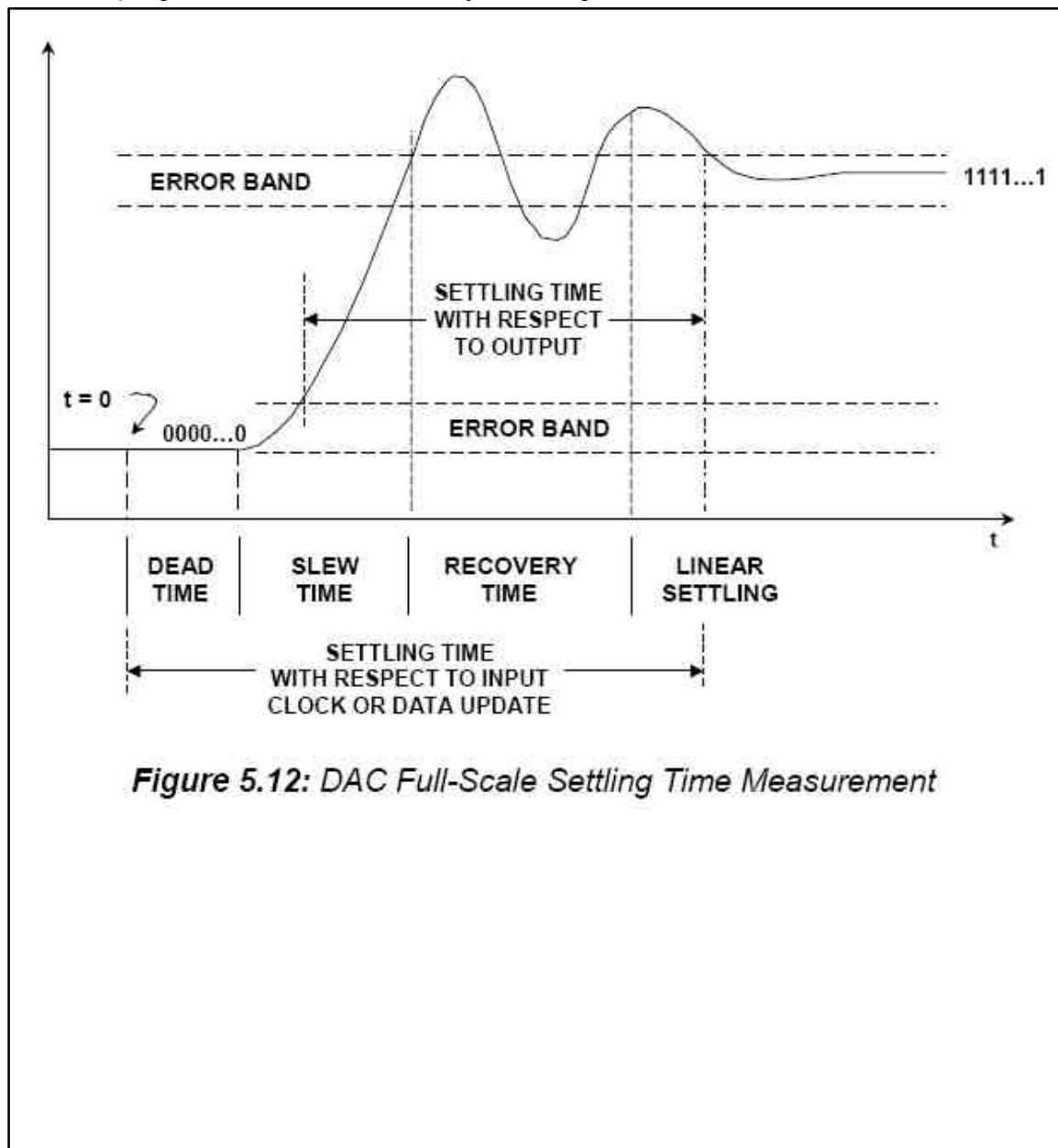
**Notes**



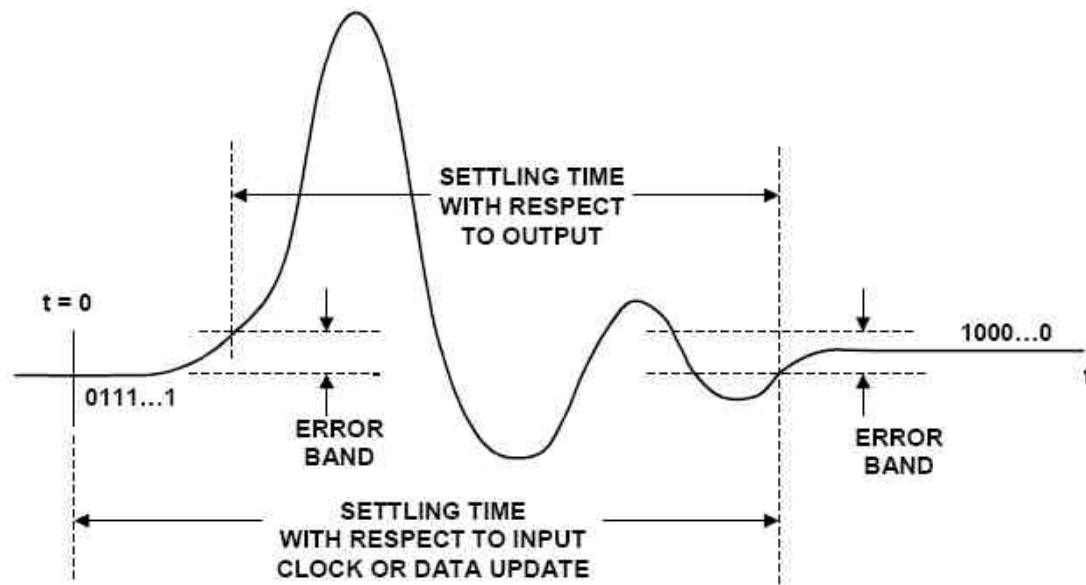
**Notes**



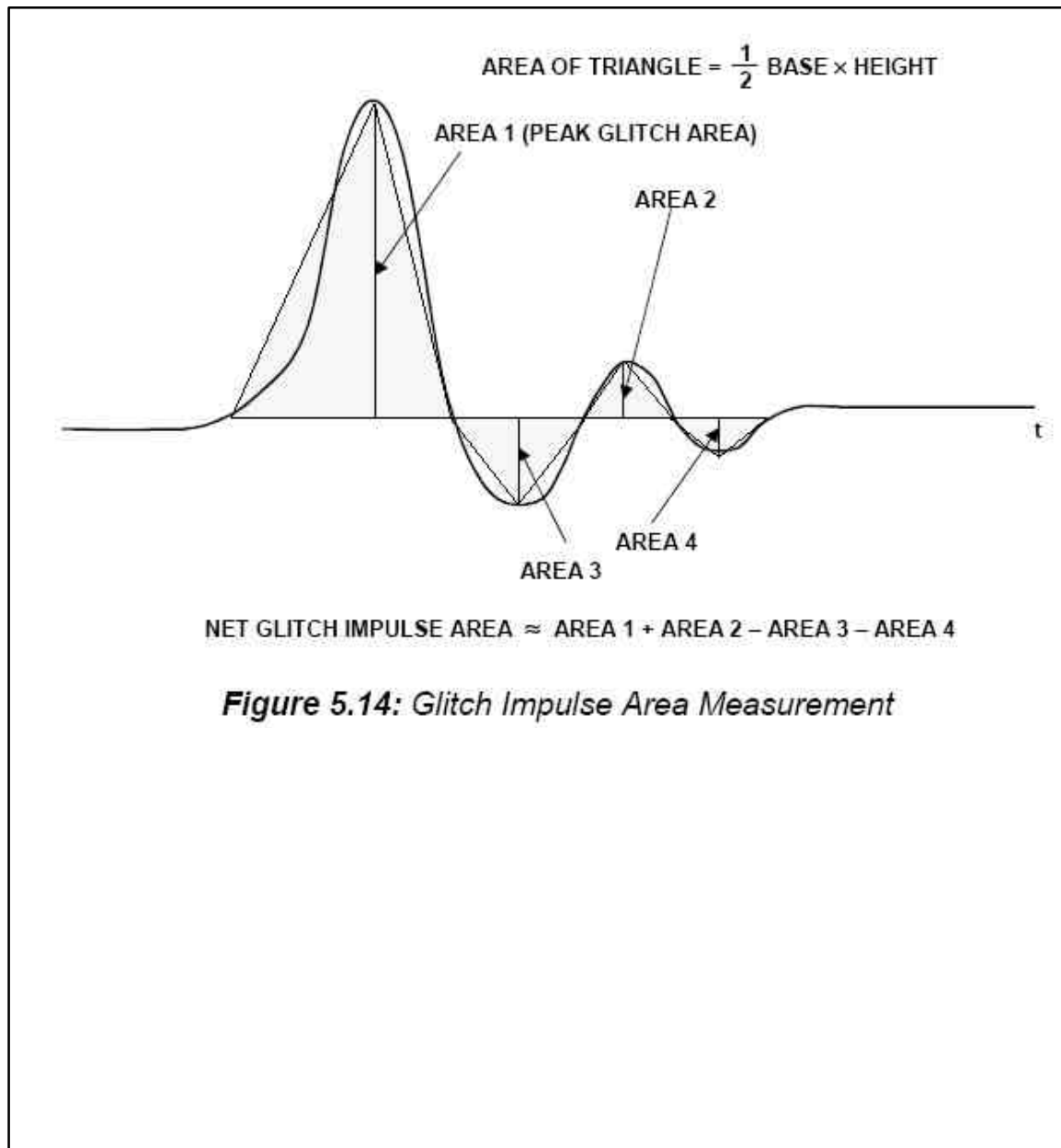
**Figure 5.11: 3-Bit x 4-Bit Segmented 7-Bit DAC Test Codes**

**Notes**

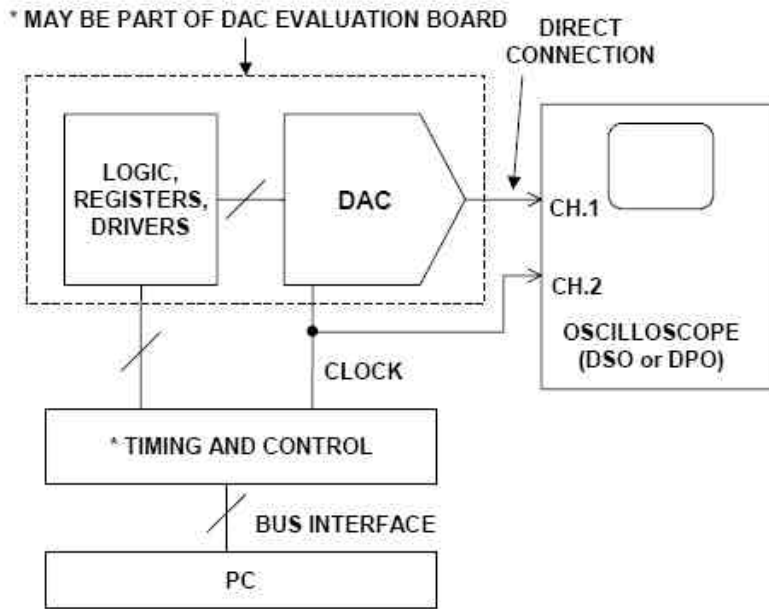
**Figure 5.12: DAC Full-Scale Settling Time Measurement**

**Notes**

**Figure 5.13: DAC Mid-Scale Settling Time Measurement**

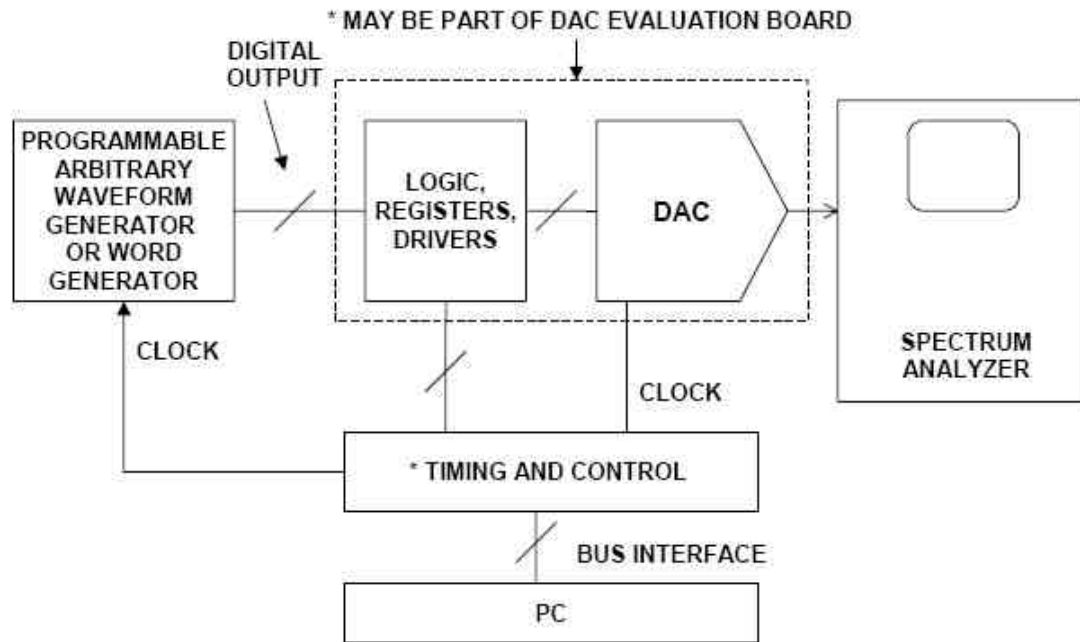
**Notes**

**Notes**



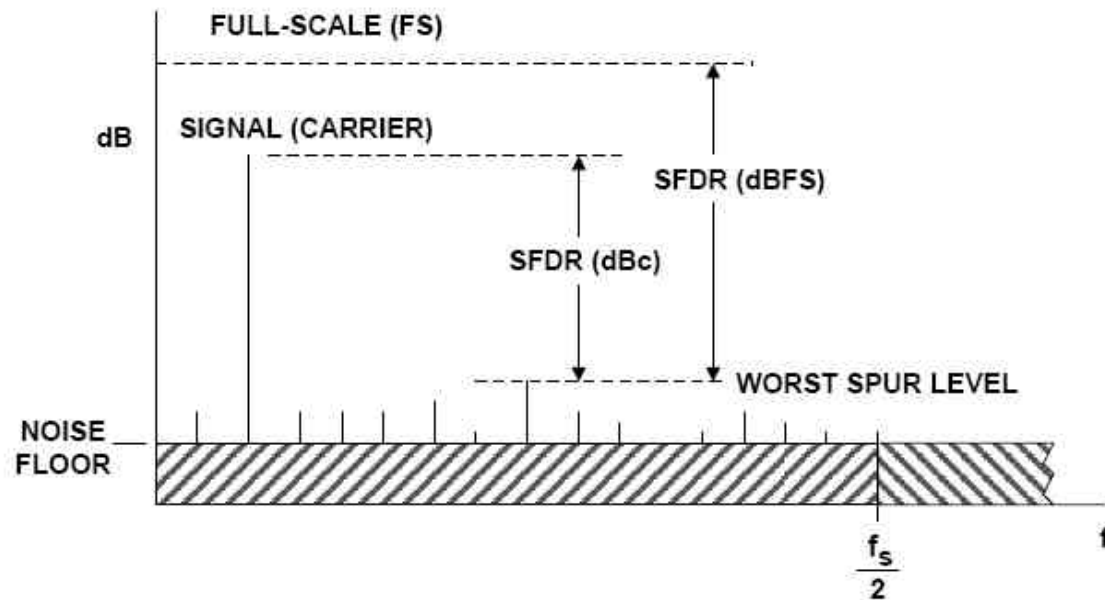
**Figure 5.15: Test Setup for Measuring Settling Time and Glitch Impulse Area**

**Notes**



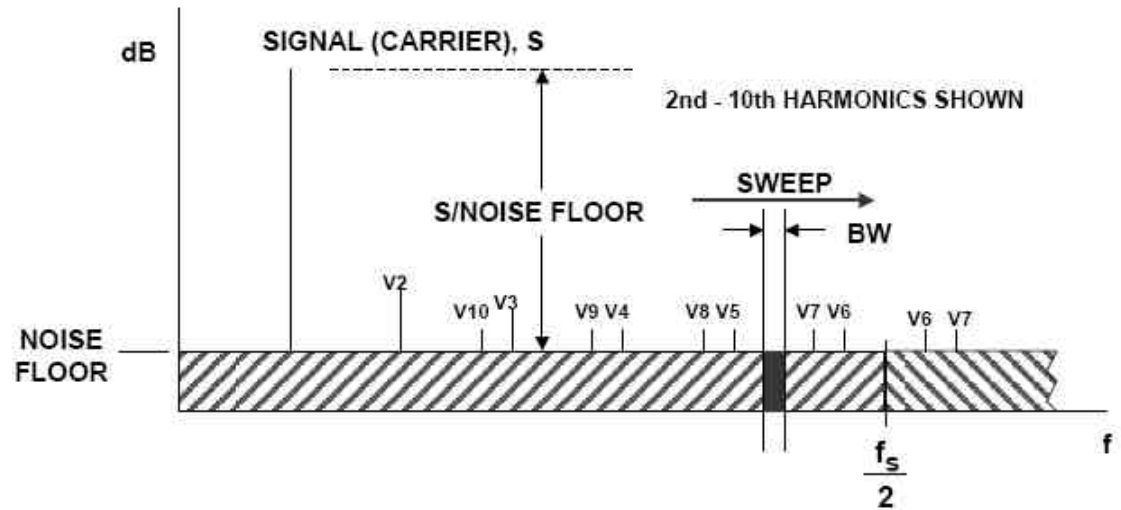
**Figure 5.16: Test Setup for Measuring DAC Distortion and Noise**



**Notes**

**Figure 5.17: Measuring DAC Spurious Free Dynamic Range (SFDR)**

**Notes**



◆ BW = ANALYZER RESOLUTION BANDWIDTH

◆  $SNR = S/NOISE FLOOR - 10 \log_{10} \left[ \frac{f_s/2}{BW} \right]$

**Figure 5.18:** Measuring DAC Distortion and SNR with an Analog Spectrum Analyzer

**Notes**

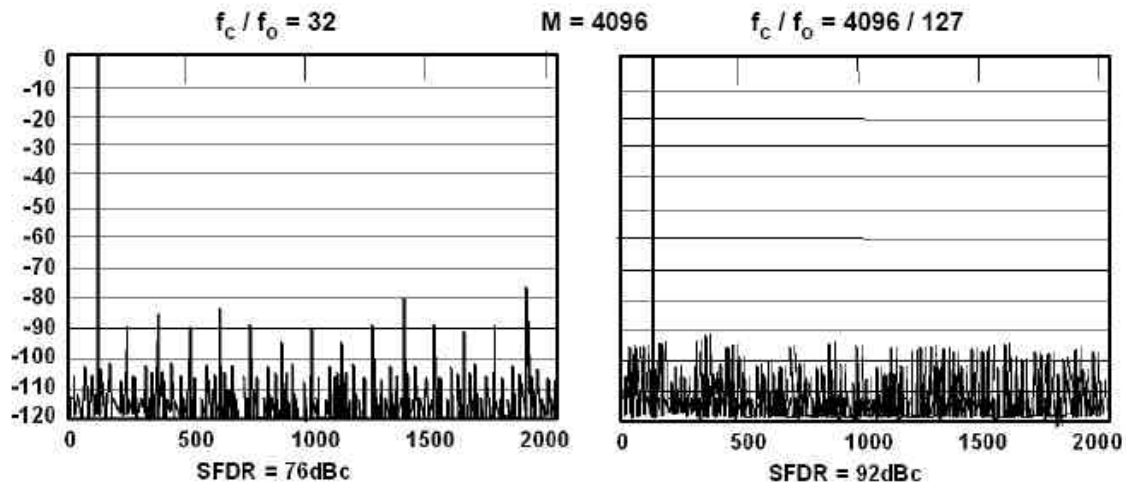
$$\blacklozenge \text{ SNR} = \text{S/NOISE FLOOR} - 10 \log_{10} \left[ \frac{f_s/2}{\text{BW}} \right]$$

$$\blacklozenge \text{ THD} = 20 \log_{10} \sqrt{\left[ 10^{-V2/20} \right]^2 + \left[ 10^{-V3/20} \right]^2 + \dots + \left[ 10^{-V6/20} \right]^2}$$

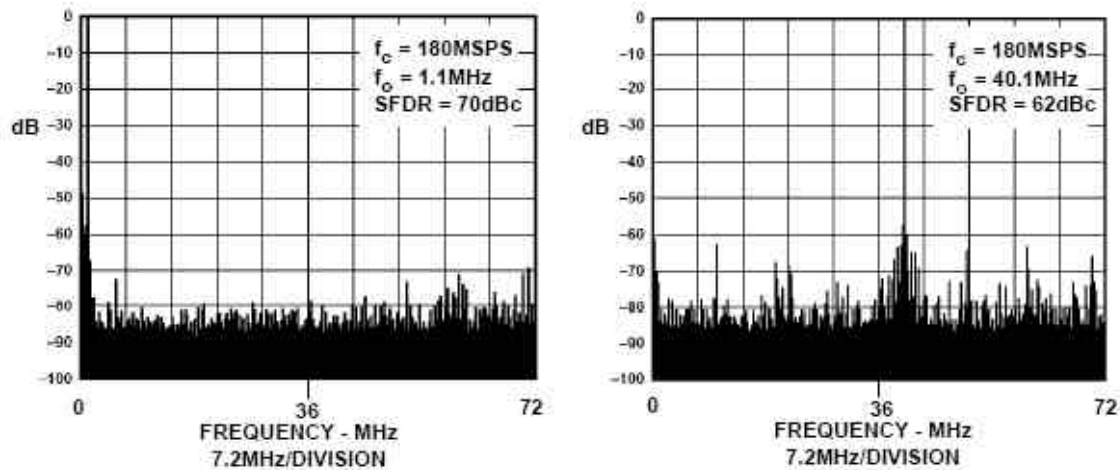
$$\blacklozenge \text{ SINAD} = 20 \log_{10} \sqrt{\left[ 10^{-\text{SNR}/20} \right]^2 + \left[ 10^{-\text{THD}/20} \right]^2}$$

NOTE: NOISE FLOOR, SNR, THD, SINAD, V2, V3, ... , V6 in units of dBc

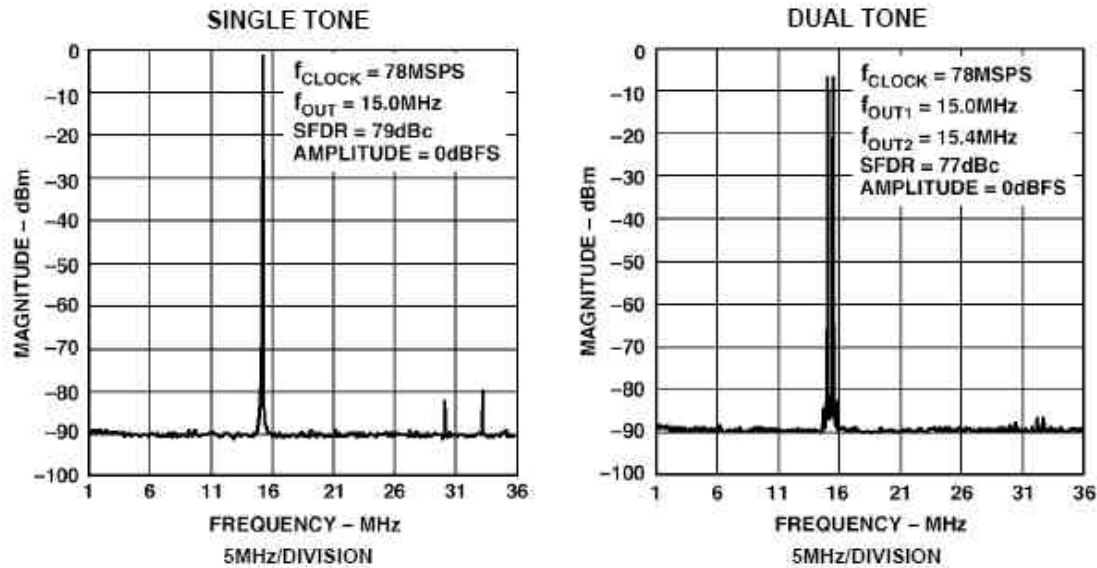
**Figure 5.19:** Calculating  $S/(N+D)$  (SINAD) from SNR and THD

**Notes**

**Figure 5.20:** Effect of Ratio of Sampling Clock  $f_c$  to Output Frequency  $f_o$  on SFDR for Ideal 12-bit DAC

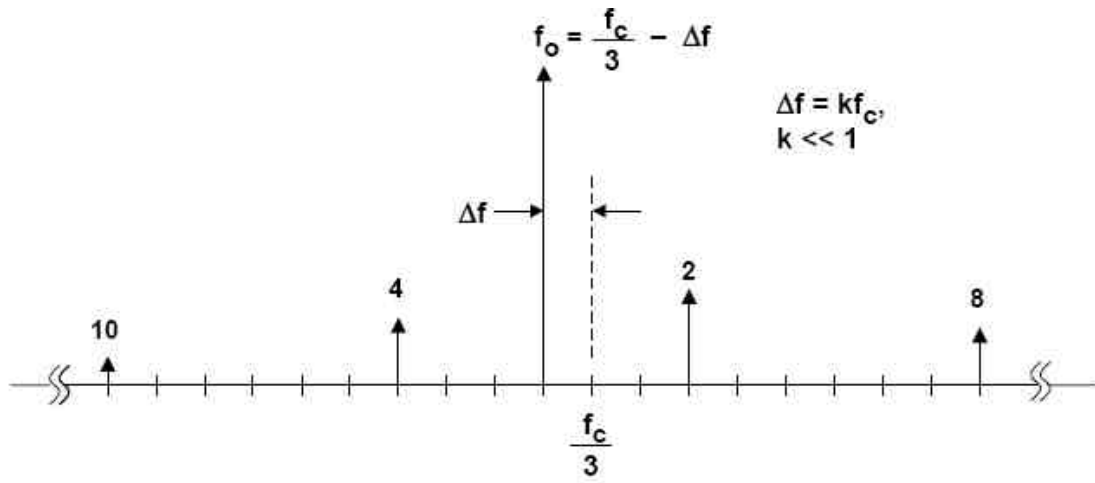
**Notes**

*Figure 5.21: AD9851 10-Bit, 180-MSPS DDS Spectral Output*

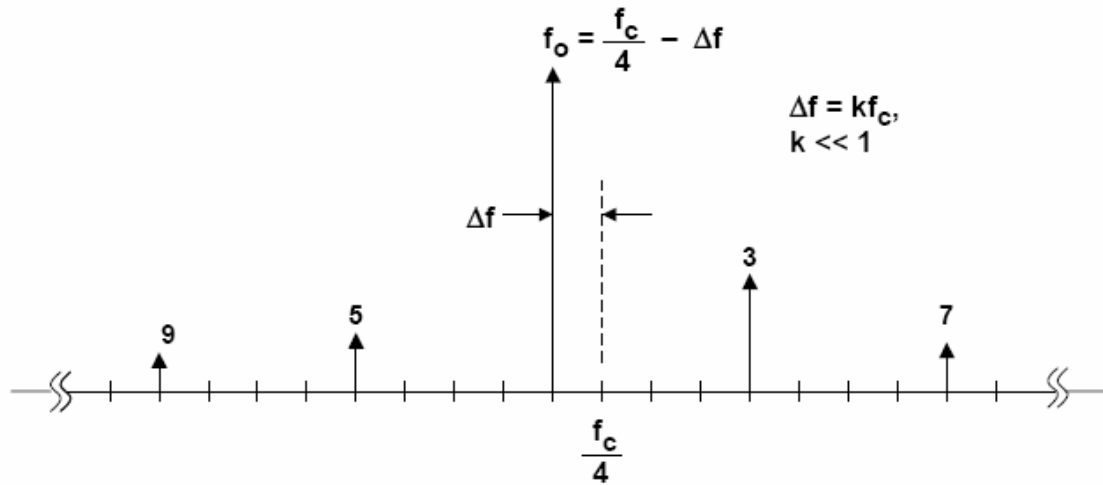
**Notes**

**Figure 5.22: AD9744, 14-Bit, 165-MSPS TxDAC<sup>®</sup> Spectral Output**

**Notes**

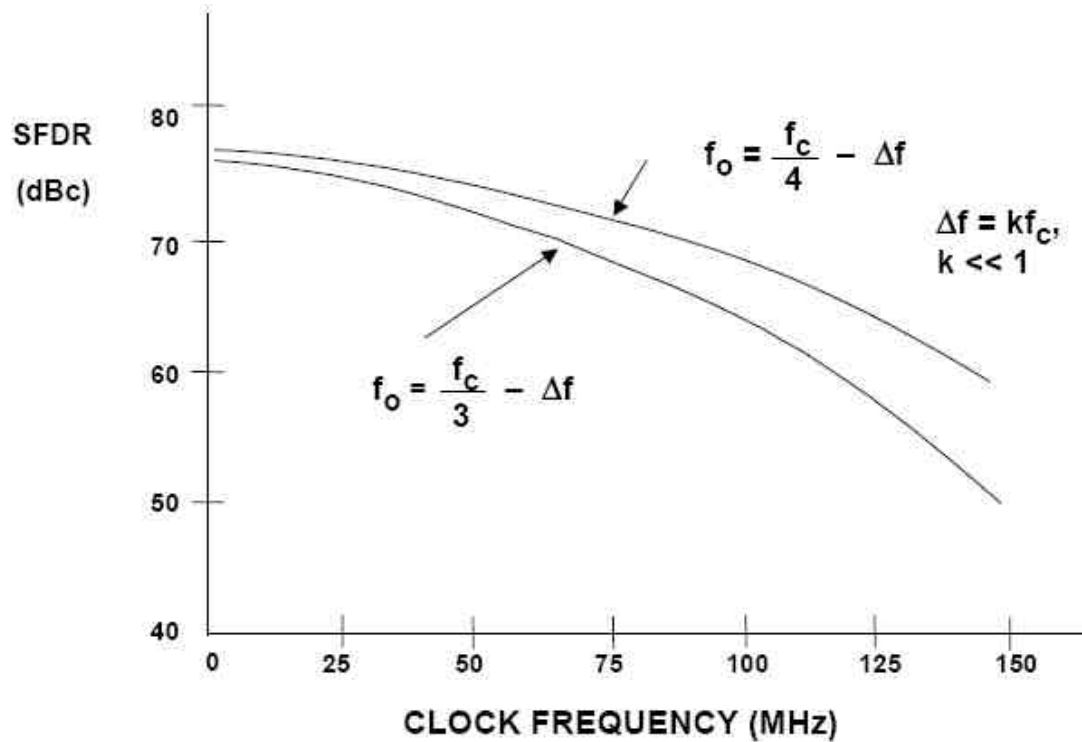


**Figure 5.23:** Location of Even Harmonics for  $f_o = f_c/3 - \Delta f$

**Notes**

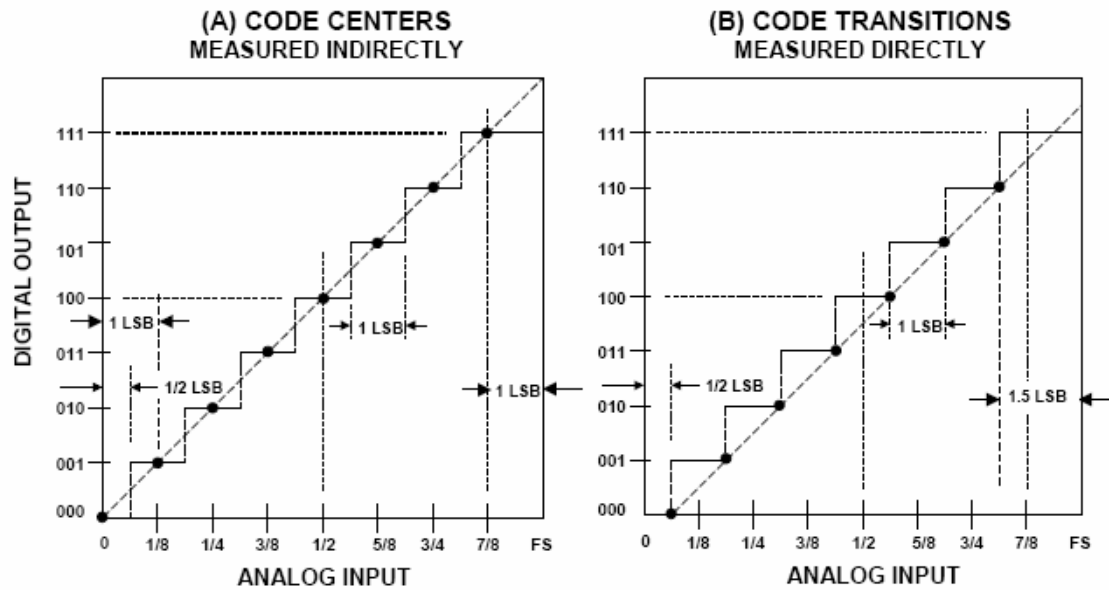
**Figure 5.24:** Location of Odd Harmonics for  $f_o = f_c/4 - \Delta f$



**Notes**

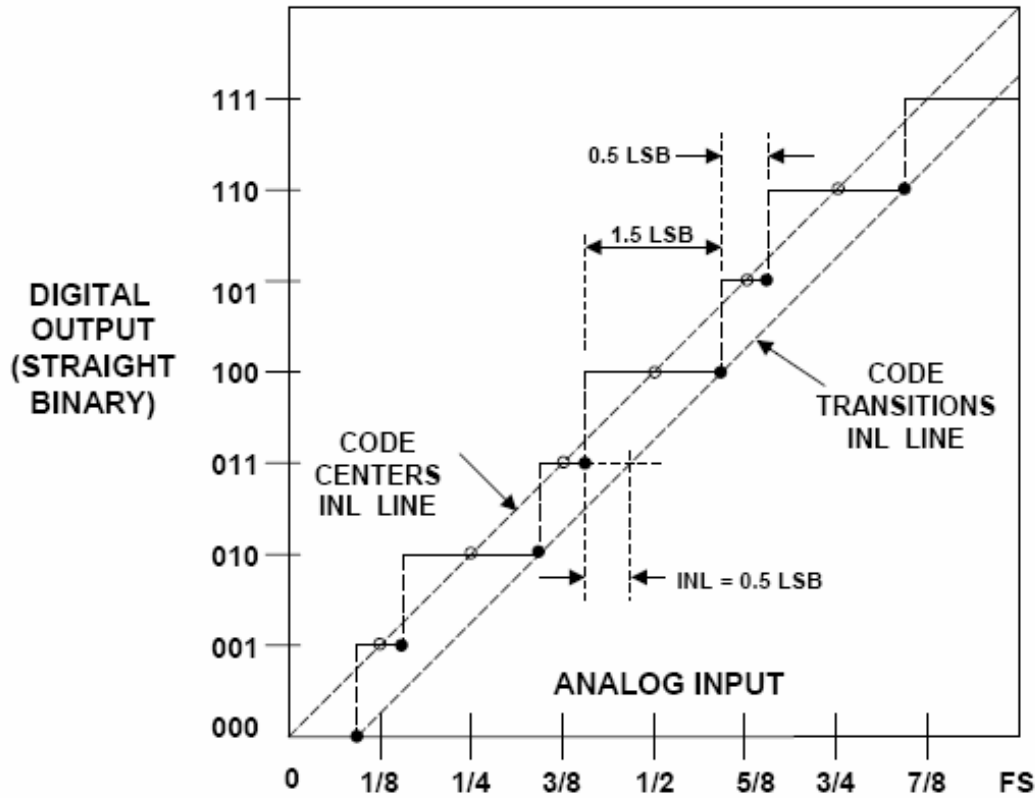
**Figure 5.25:** Worst Harmonic vs. Clock Frequency for  $f_o = f_c/3 - \Delta f$  and  $f_o = f_c/4 - \Delta f$

**Notes**



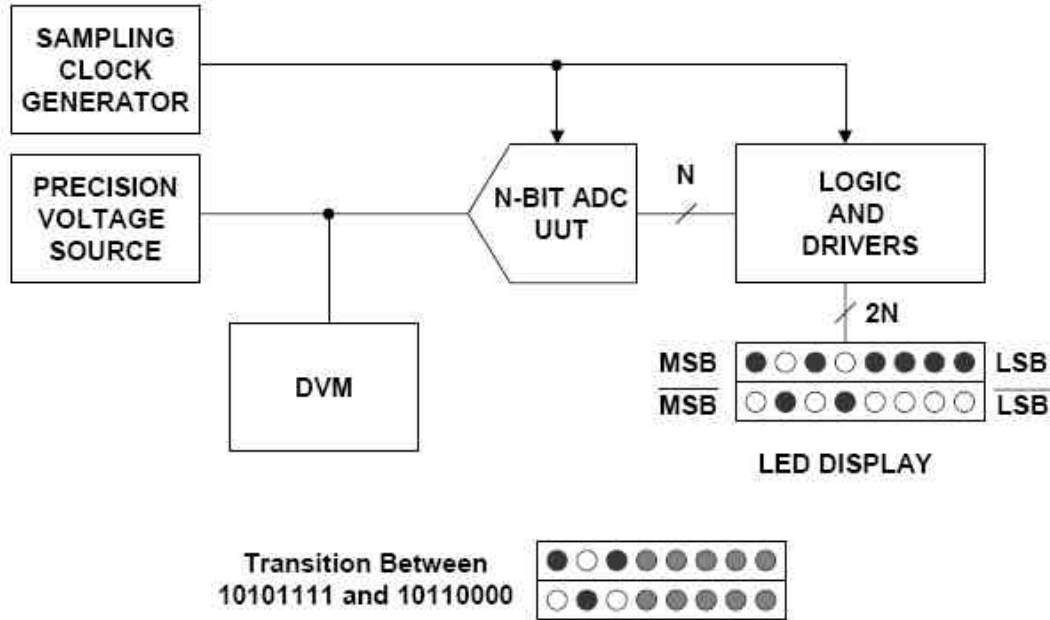
**Figure 5.26: Measuring ADC Code Transitions to Determine Code Centers**

**Notes**



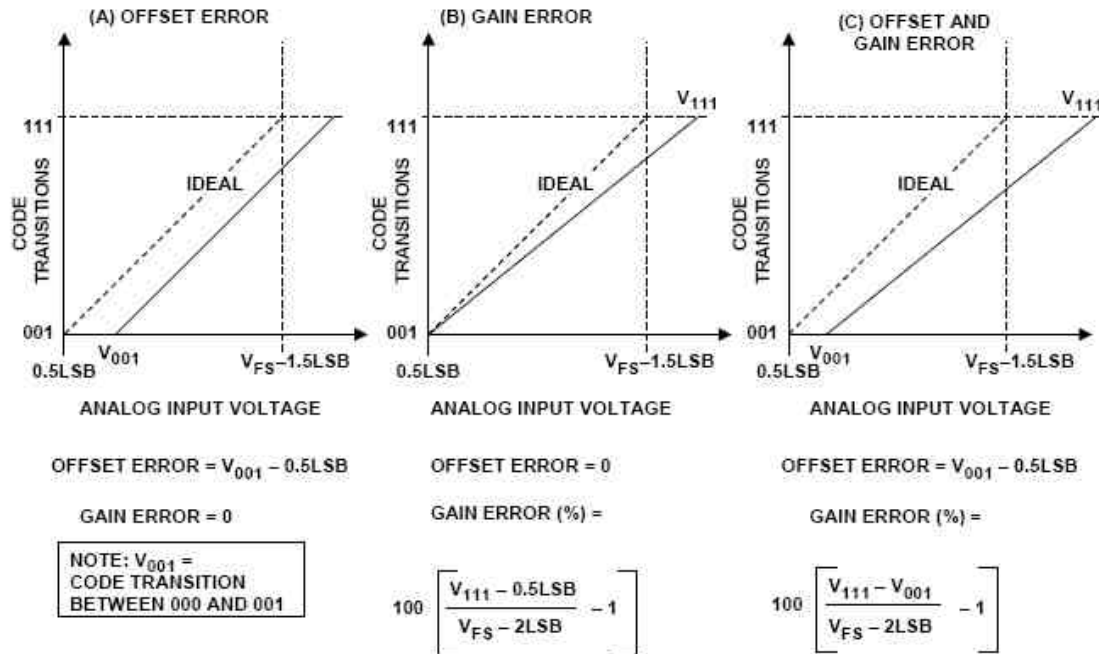
**Figure 5.27: Code Transitions Preferable to Code Centers for Measuring ADC DNL and INL**

**Notes**



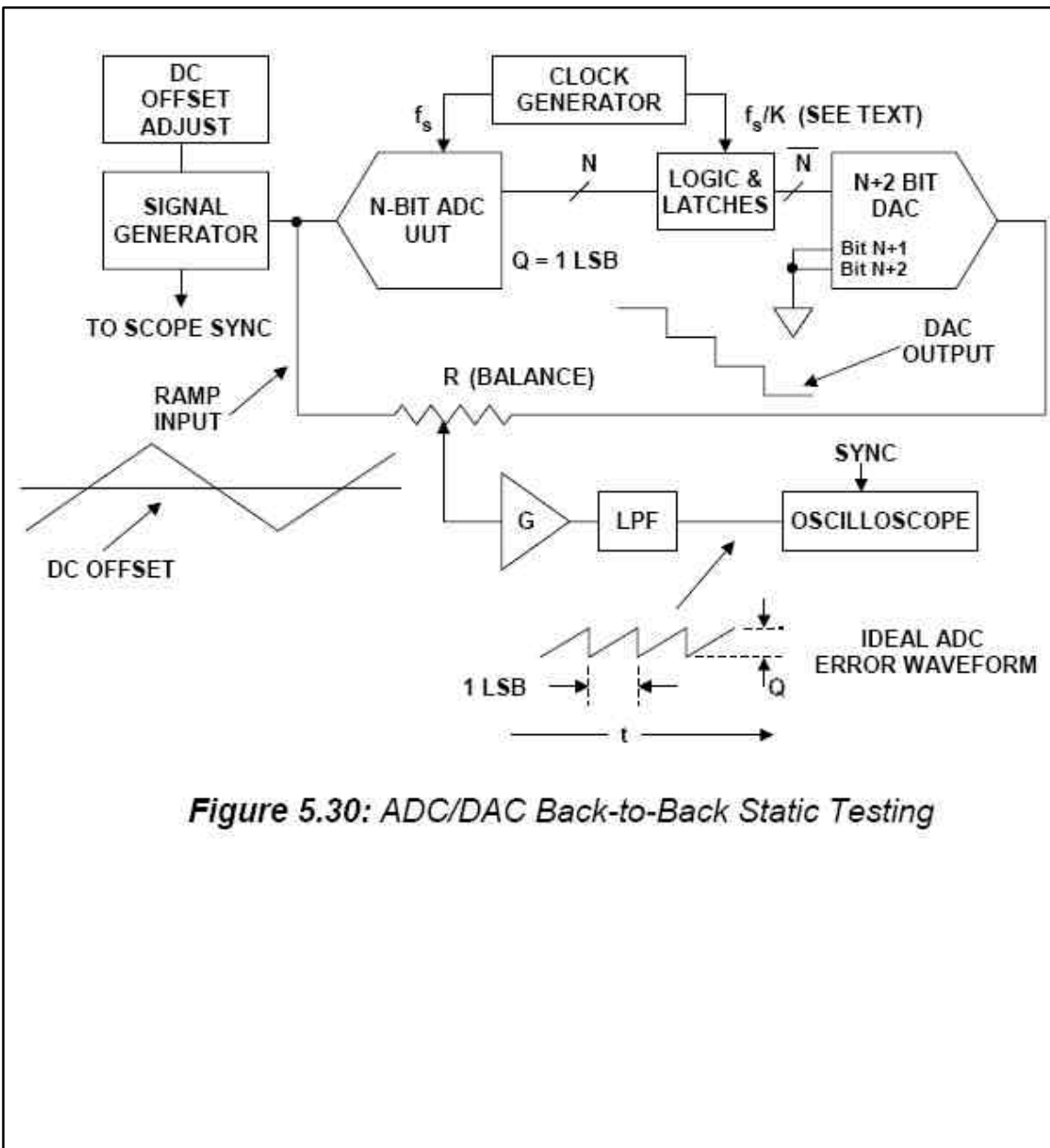
*Figure 5.28: Simple Test Setup for Measuring ADC Code Transitions*

**Notes**



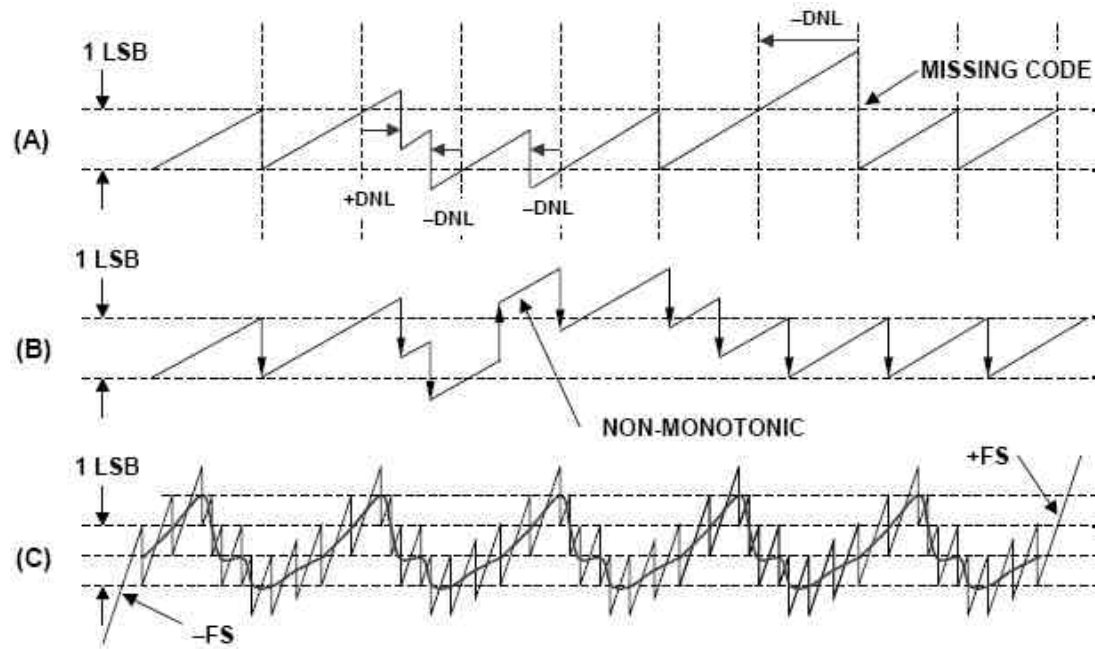
**Figure 5.29: Measuring ADC Offset and Gain Error**

**Notes**

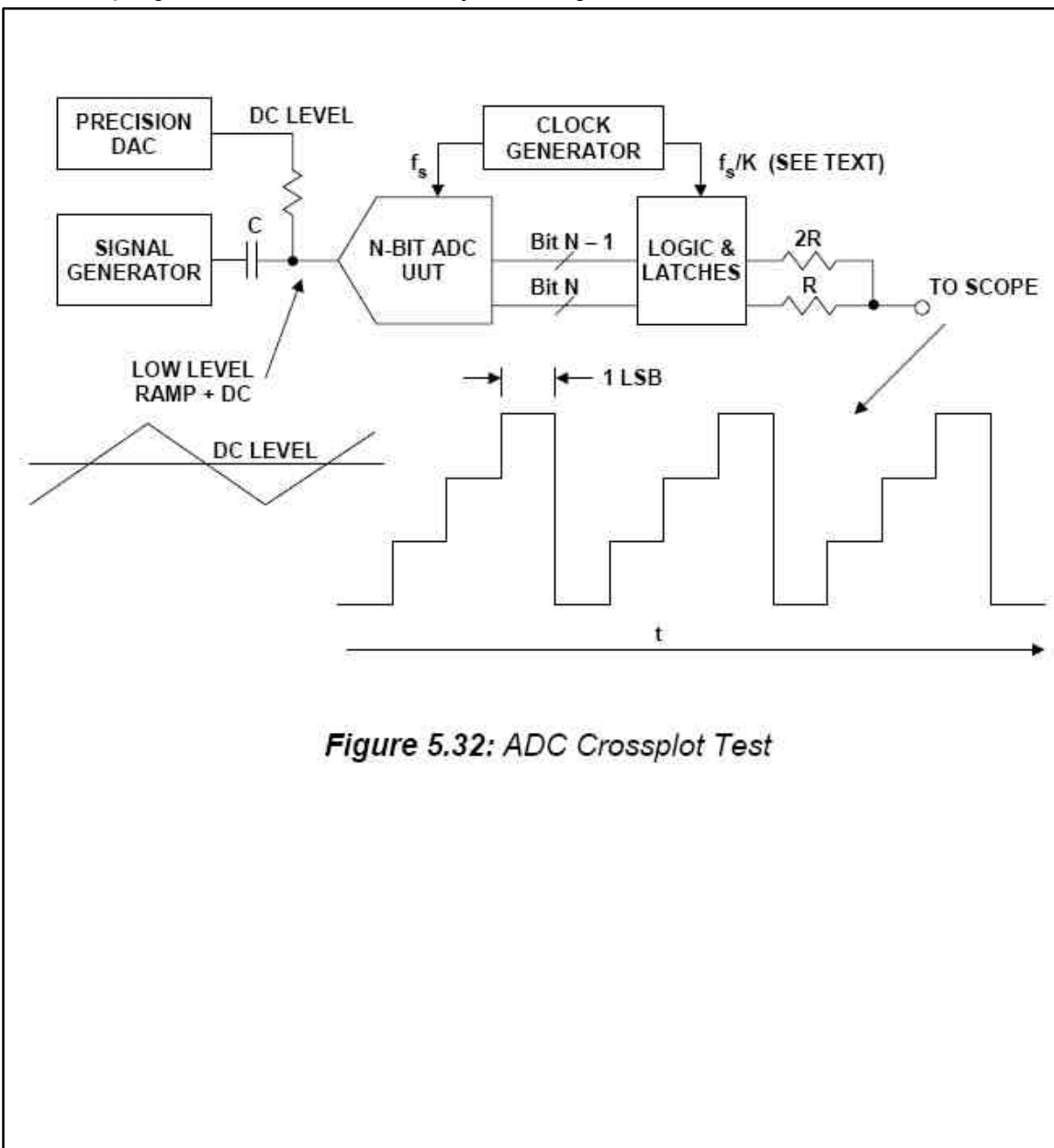


**Figure 5.30: ADC/DAC Back-to-Back Static Testing**

**Notes**

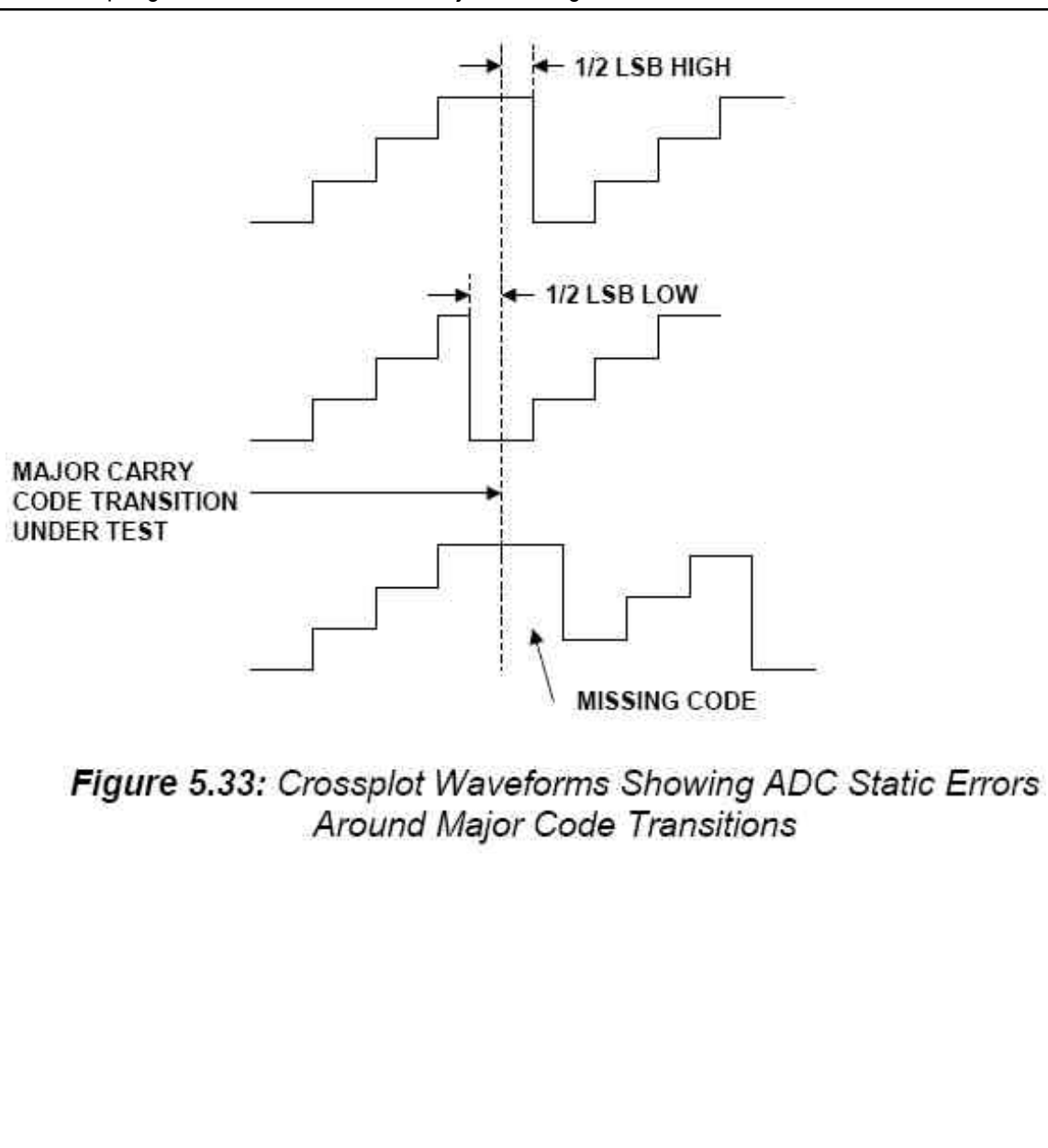


**Figure 5.31: ADC Error Waveforms Using "Back-to-Back" Test Setup**

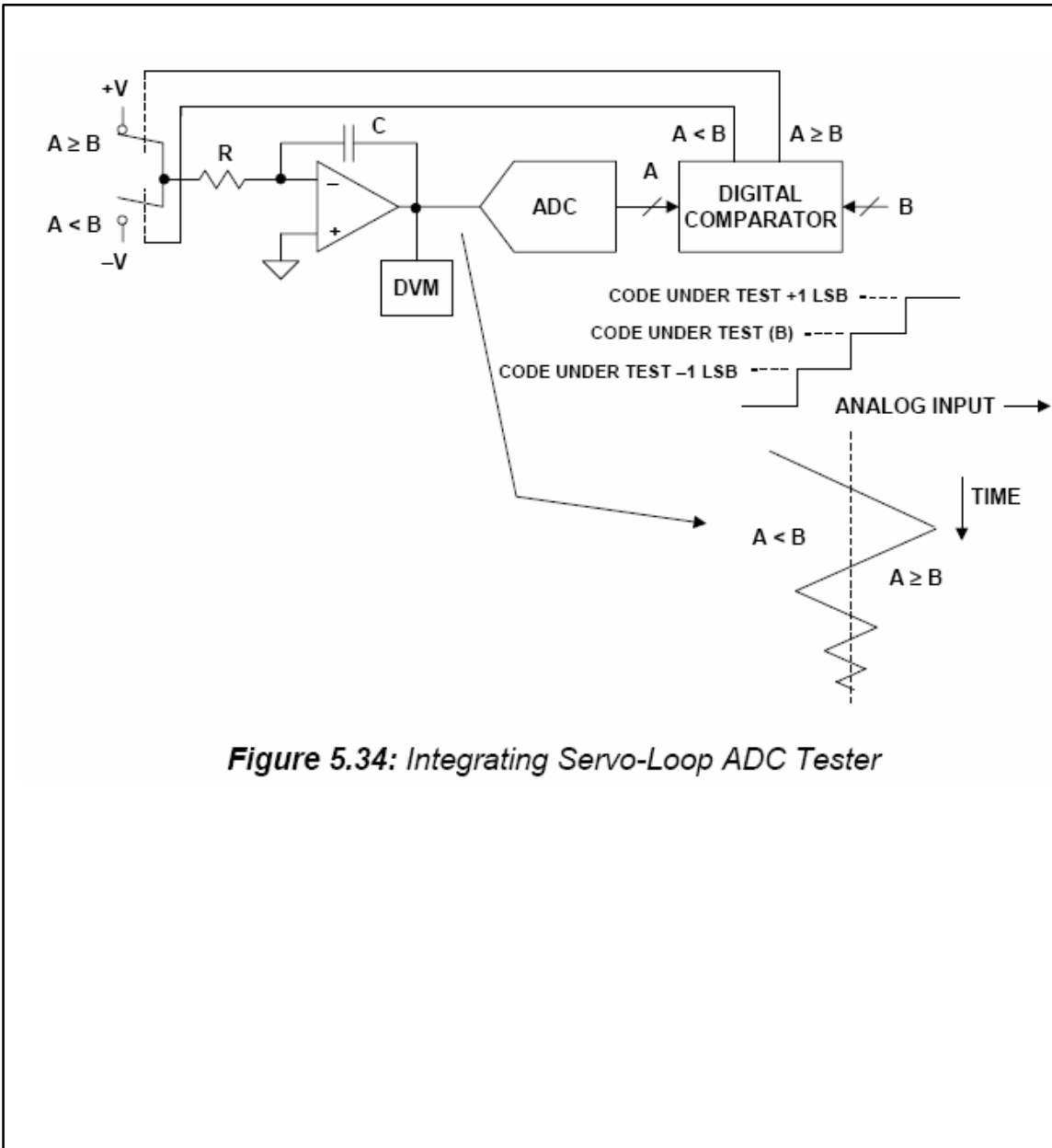
**Notes**

**Figure 5.32: ADC Crossplot Test**



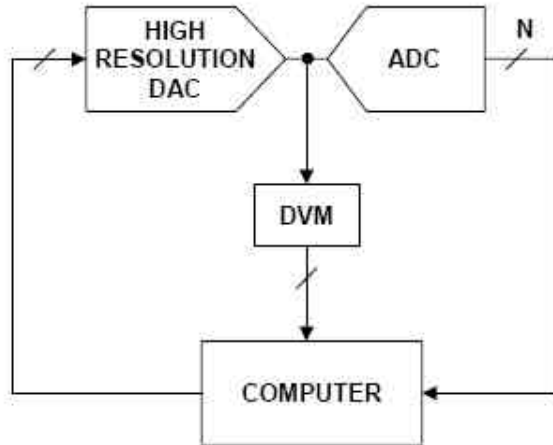
**Notes**

**Notes**



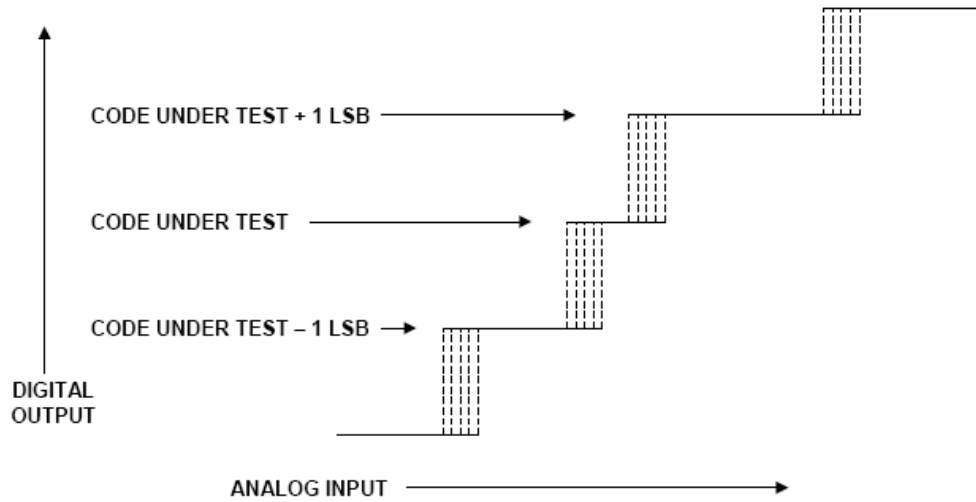
**Figure 5.34: Integrating Servo-Loop ADC Tester**

**Notes**

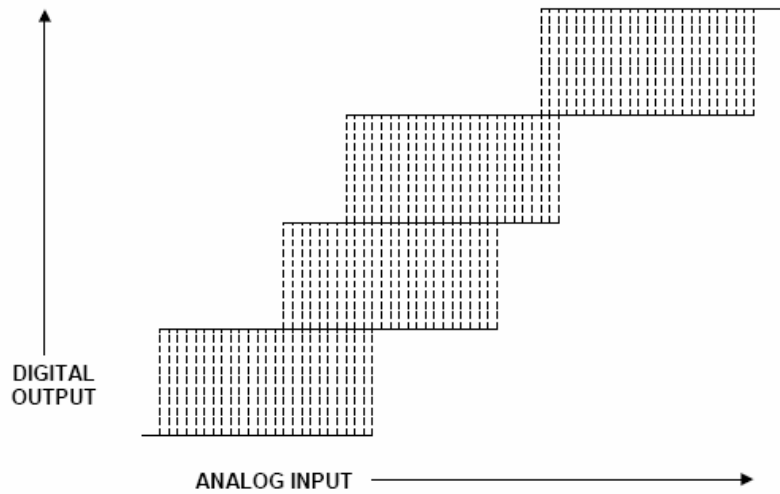


*Figure 5.35: Generalized Computer Controlled Servo-Loop ADC Tester*

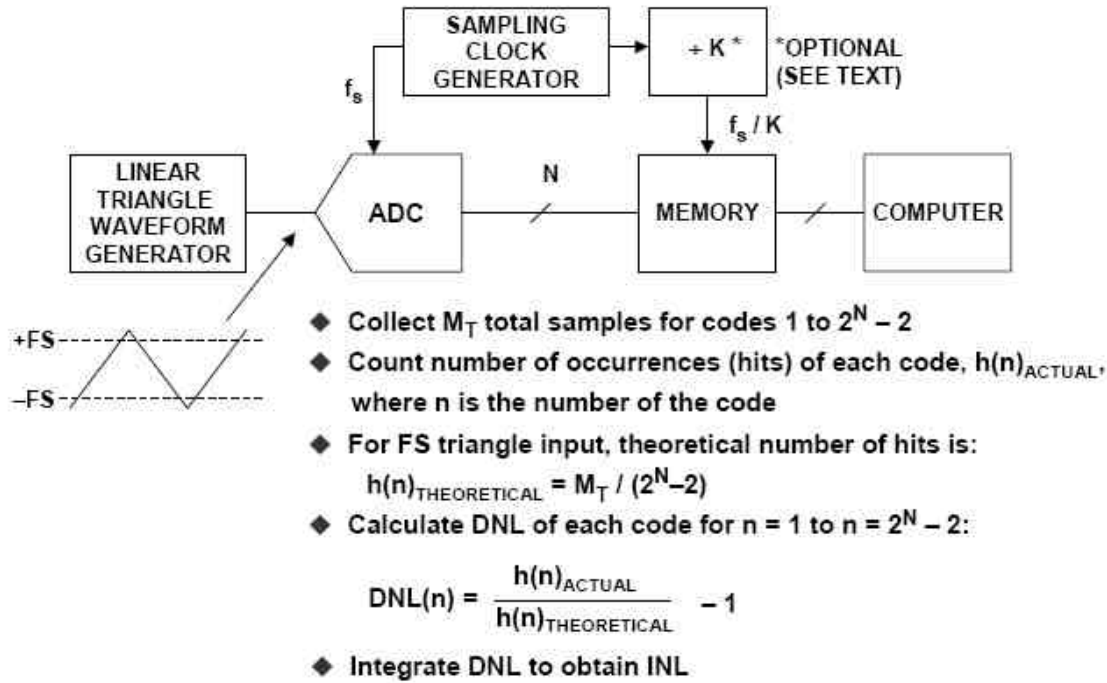
**Notes**

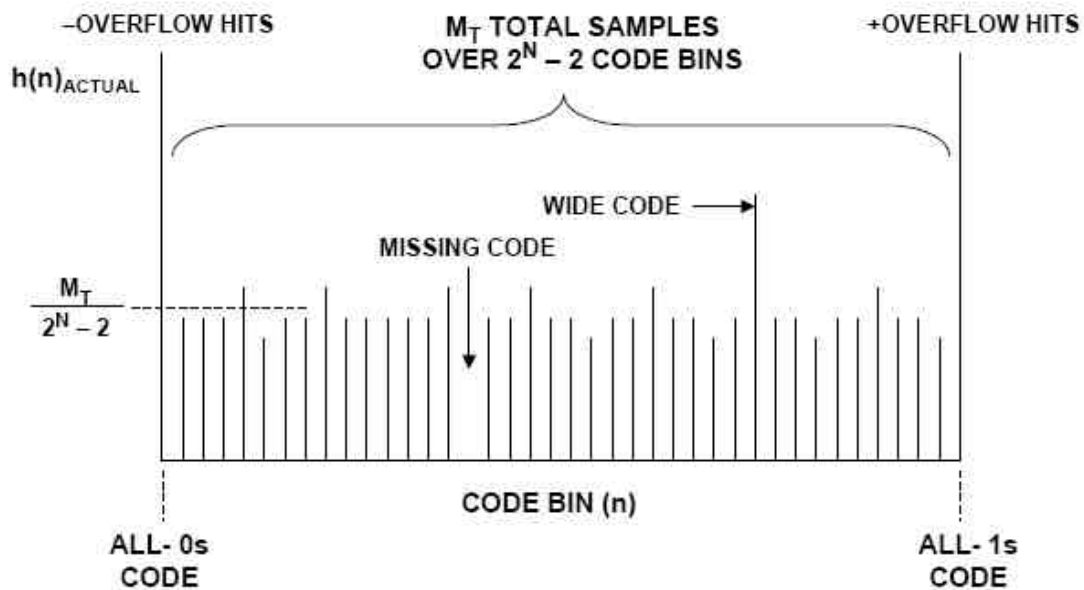


**Figure 5.36:** ADC Transfer Function With Relatively Low Input-Referred Noise

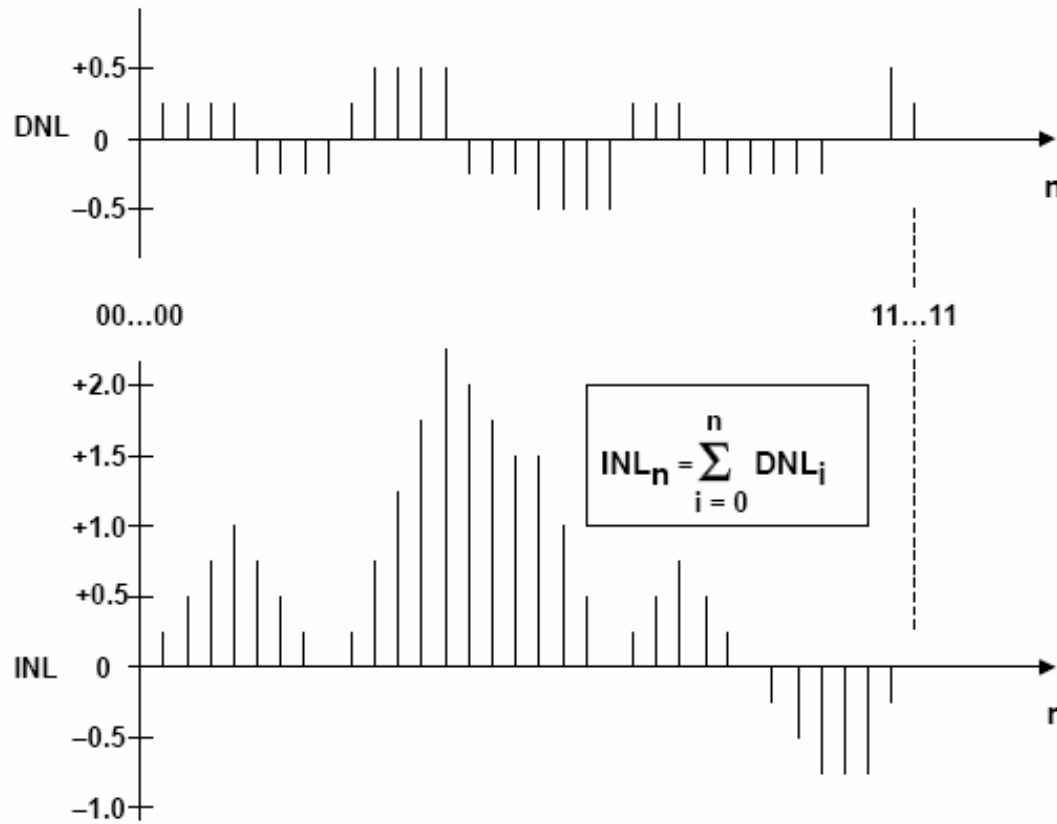


**Figure 5.37:** ADC Transfer Function With Relatively High Input-Referred Noise

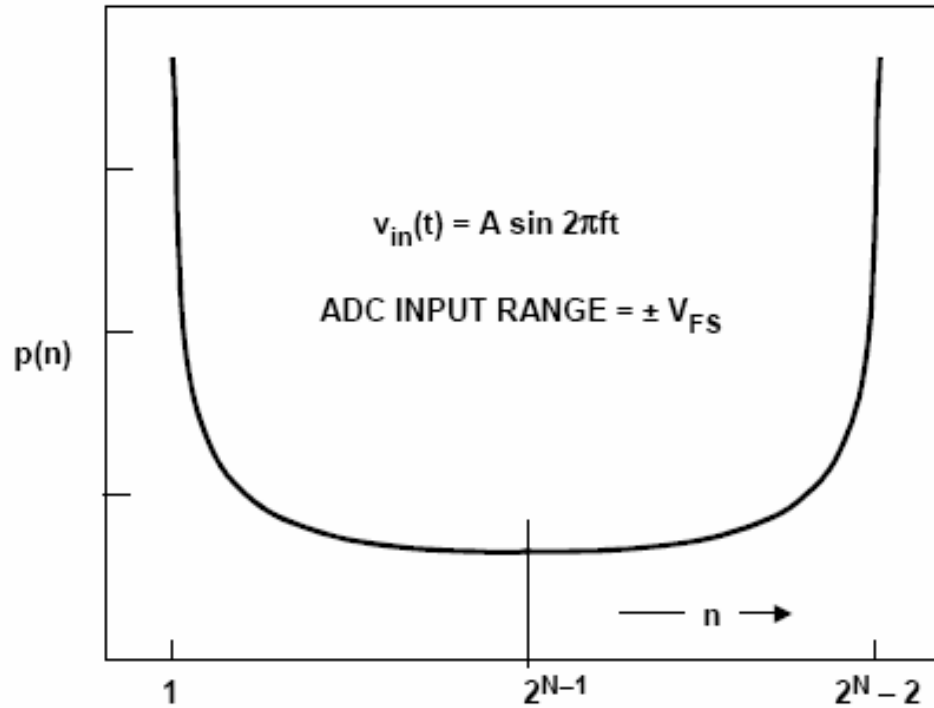
**Notes***Figure 5.38: Histogram (Code Density) Test Setup*

**Notes**

**Figure 5.39: Histogram for Linear Ramp Test**

**Notes**

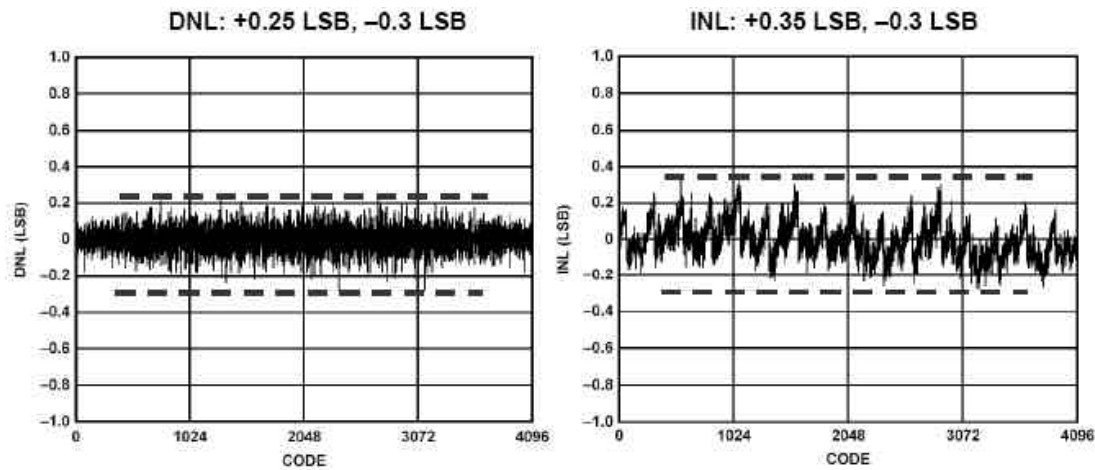
**Figure 5.40: Integration of DNL Data Yields INL**

**Notes**

$$p(n) = \frac{1}{\pi} \left[ \sin^{-1} \left[ \frac{V_{FS} (n - 2^{N-1})}{A \cdot 2^N} \right] - \sin^{-1} \left[ \frac{V_{FS} (n - 1 - 2^{N-1})}{A \cdot 2^N} \right] \right]$$

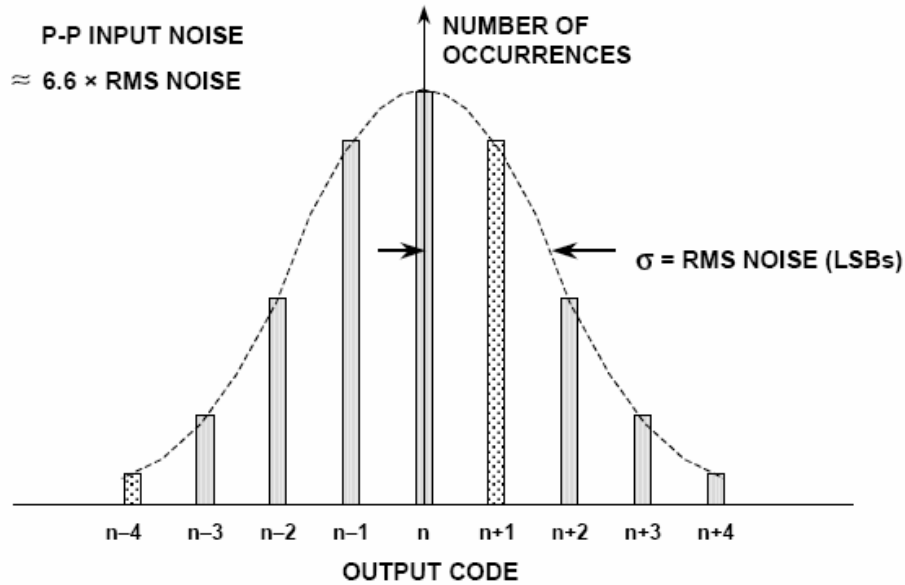
**Figure 5.41: Sinewave Probability Density Function**



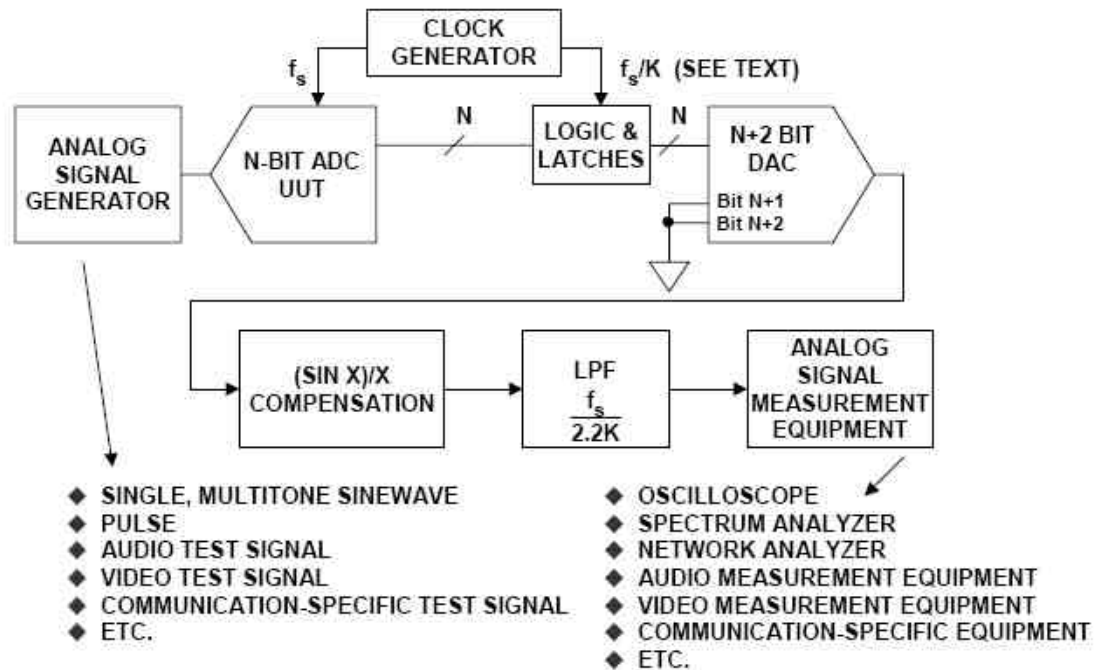
**Notes**

*Figure 5.42: Typical Static DNL and INL Histogram Plots for AD9236 12-Bit, 80-MSPS ADC*

**Notes**

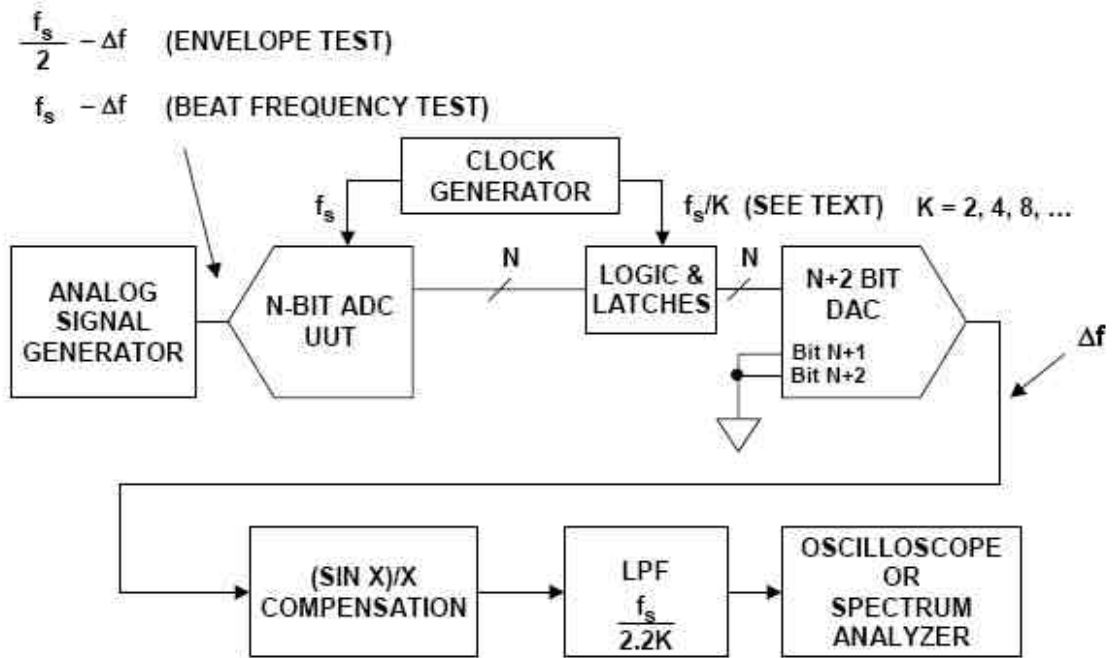


**Figure 5.43:** Measuring Input-Referred Noise Using "Grounded Input" Histogram

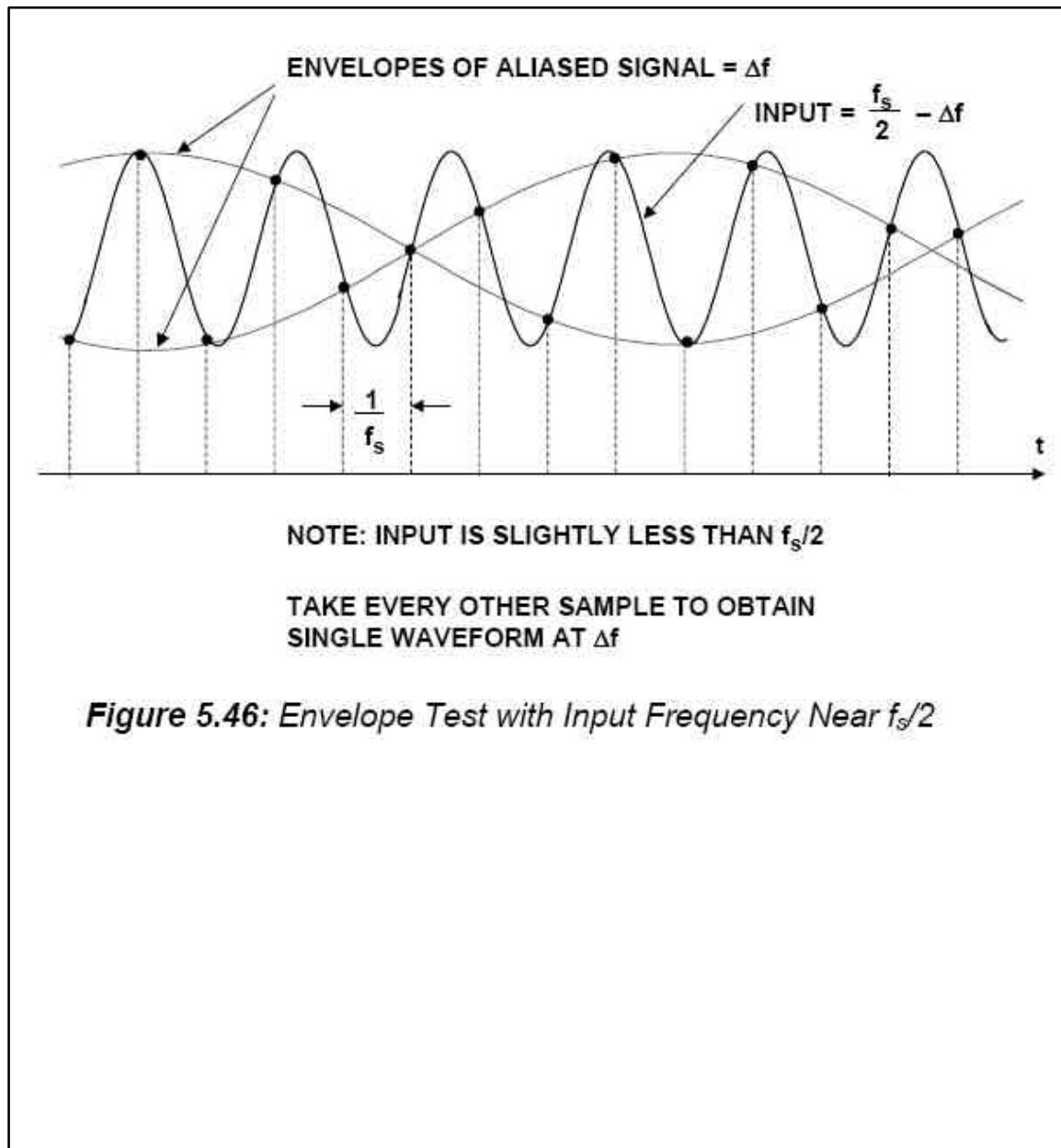
**Notes**

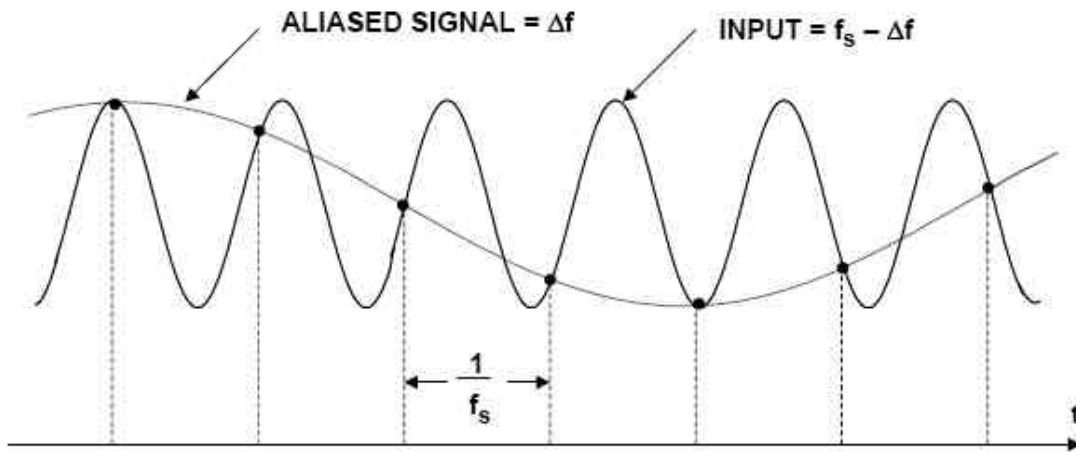
**Figure 5.44: "Back-to-Back" Setup for ADC Dynamic Testing**

**Notes**



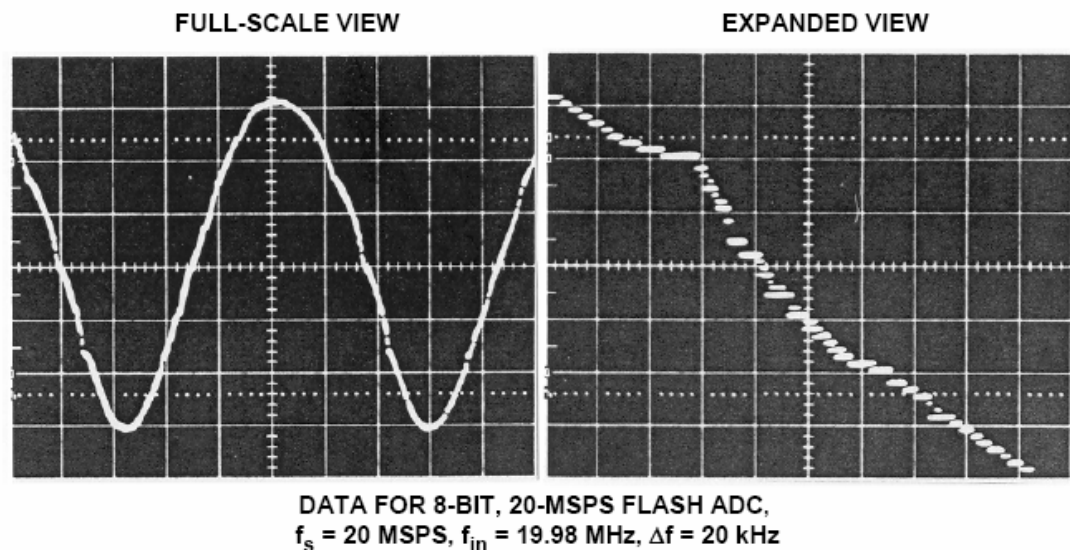
**Figure 5.45: Envelope and Beat Frequency Test Setup**

**Notes**

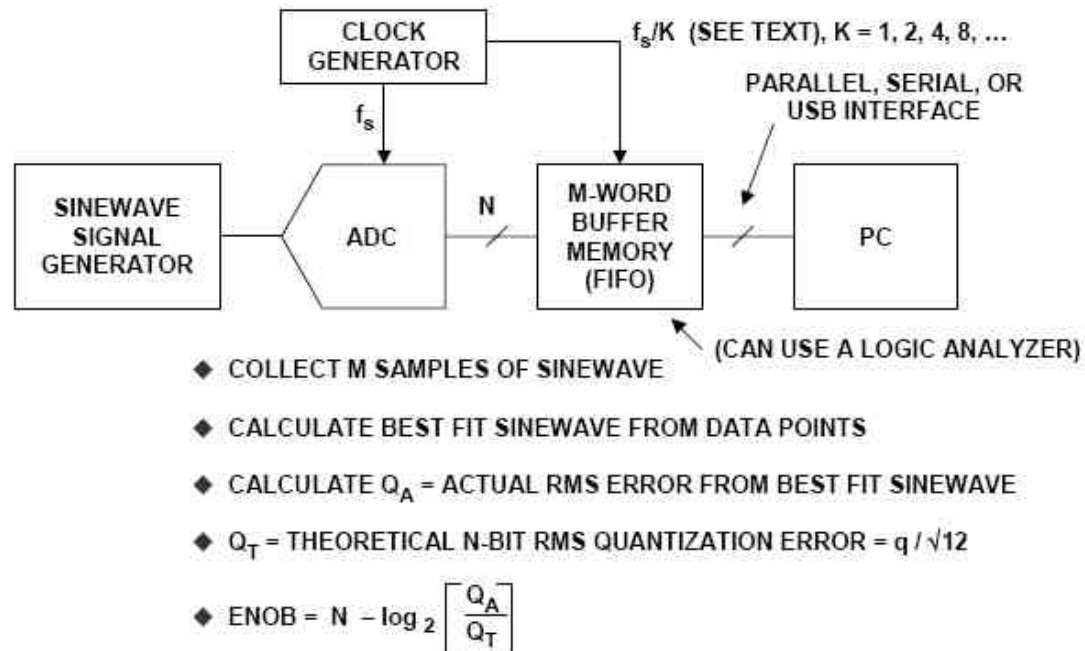
**Notes**

NOTE: INPUT IS SLIGHTLY LESS THAN  $f_s$

**Figure 5.47: Beat Frequency Test with Input Frequency Near  $f_s$**

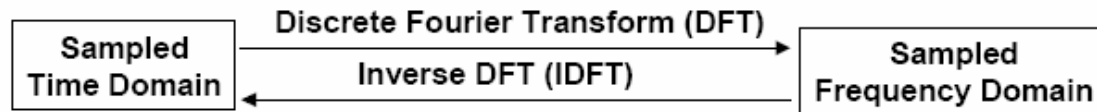
**Notes**

*Figure 5.48: Beat Frequency and Envelope Tests Show ADC AC Nonlinearities*

**Notes**

**Figure 5.49: Sinewave Curve Fit Test Setup for Measuring ADC ENOB**



**Notes**

## ◆ Digital Spectral Analysis

- Spectrum Analyzers
- Speech Processing
- Imaging
- Pattern Recognition
- ADC Testing

## ◆ Filter Design

- Calculating Impulse Response from Frequency Response
- Calculating Frequency Response from Impulse Response

## ◆ The Fast Fourier Transform (FFT) is Simply an Algorithm for Efficiently Calculating the DFT

*Figure 5.50: Applications of the Discrete Fourier Transform (DFT)*

**Notes**

◆ **FOURIER TRANSFORM:**

Signal is Continuous and Aperiodic



◆ **FOURIER SERIES:**

Signal is Continuous and Periodic



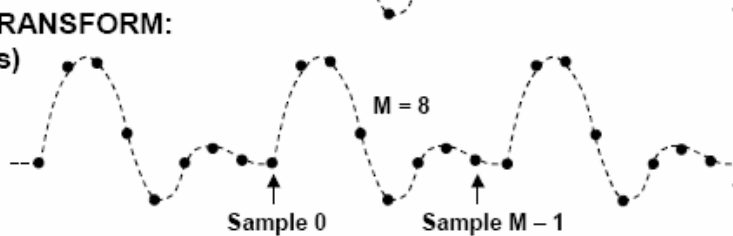
◆ **DISCRETE TIME FOURIER SERIES:**

Signal is Sampled and Aperiodic



◆ **DISCRETE FOURIER TRANSFORM:**

(Discrete Fourier Series)  
Signal is Sampled and Periodic



*Figure 5.51: Fourier Transform Family*

**Notes**

- ◆ A Periodic Signal Can be Decomposed into the Sum of Properly Chosen Cosine and Sine Waves (Jean Baptiste Joseph Fourier, 1807)
- ◆ The DFT Operates on a Finite Number (M) of Digitized Time Samples,  $x(n)$ . When These Samples are Repeated and Placed “End-to-End”, they Appear Periodic to the Transform.
- ◆ The Complex DFT Output Spectrum  $X(k)$  is the Result of Correlating the Input Samples with sine and cosine Basis Functions:

$$X(k) = \frac{1}{M} \sum_{n=0}^{M-1} x(n) e^{-j2\pi nk/M} = \frac{1}{M} \sum_{n=0}^{M-1} x(n) \left[ \cos \frac{2\pi nk}{M} - j \sin \frac{2\pi nk}{M} \right]$$
$$0 \leq k \leq M-1$$

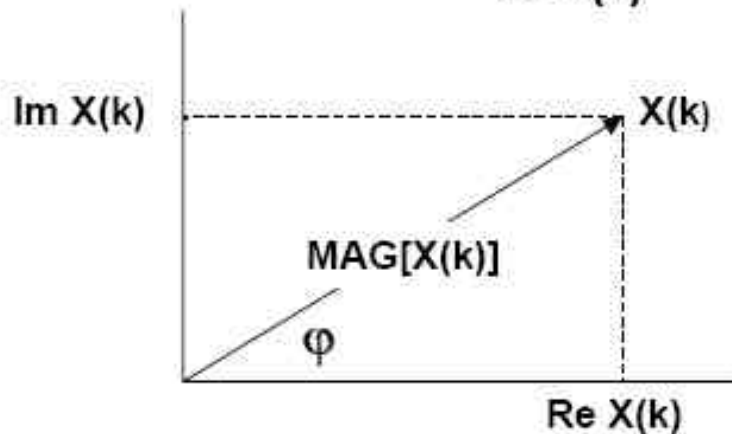
*Figure 5.52: The Discrete Fourier Transform (DFT)*

**Notes**

$$\blacklozenge \quad X(k) = \text{Re}X(k) + j \text{Im}X(k)$$

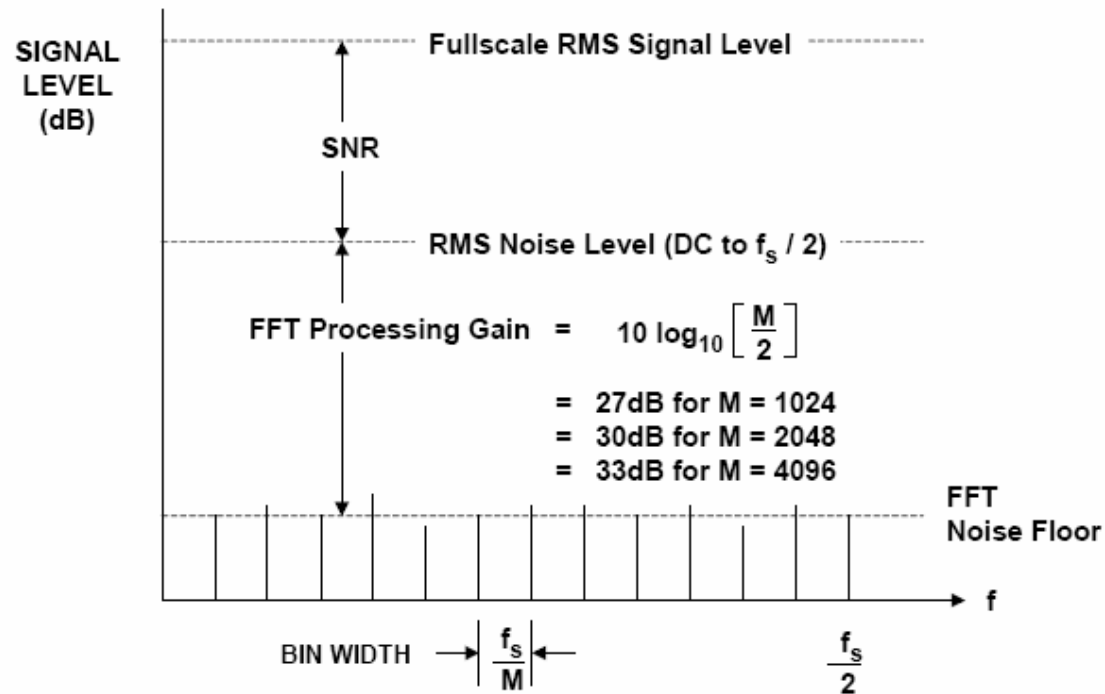
$$\blacklozenge \quad \text{MAG}[X(k)] = \sqrt{\text{Re}X(k)^2 + \text{Im}X(k)^2}$$

$$\blacklozenge \quad \varphi [X(k)] = \tan^{-1} \frac{\text{Im}X(k)}{\text{Re}X(k)}$$



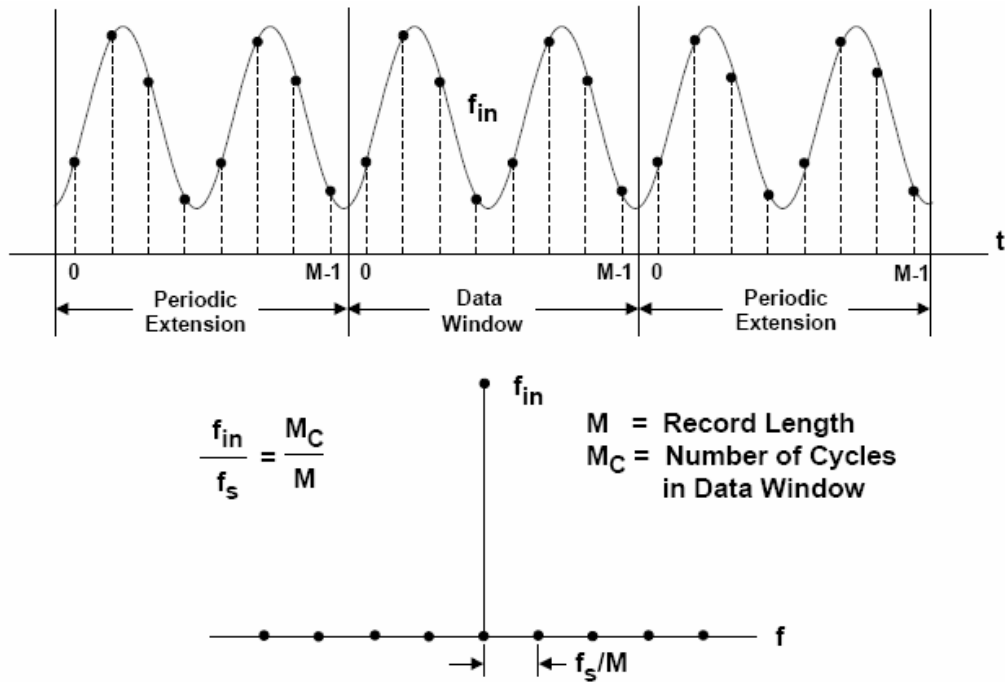
**Figure 5.53: Converting Real and Imaginary DFT Outputs into Magnitude and Phase**

**Notes**



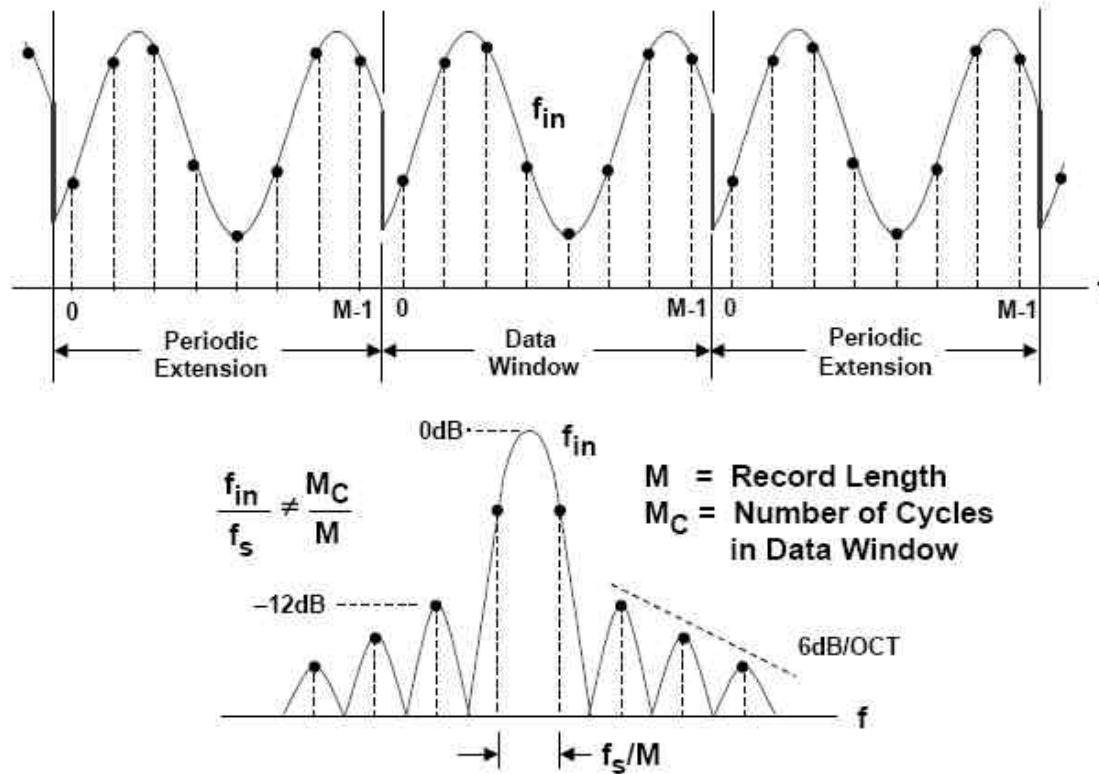
**Figure 5.54: FFT Output Shows Effects of Processing Gain**

**Notes**

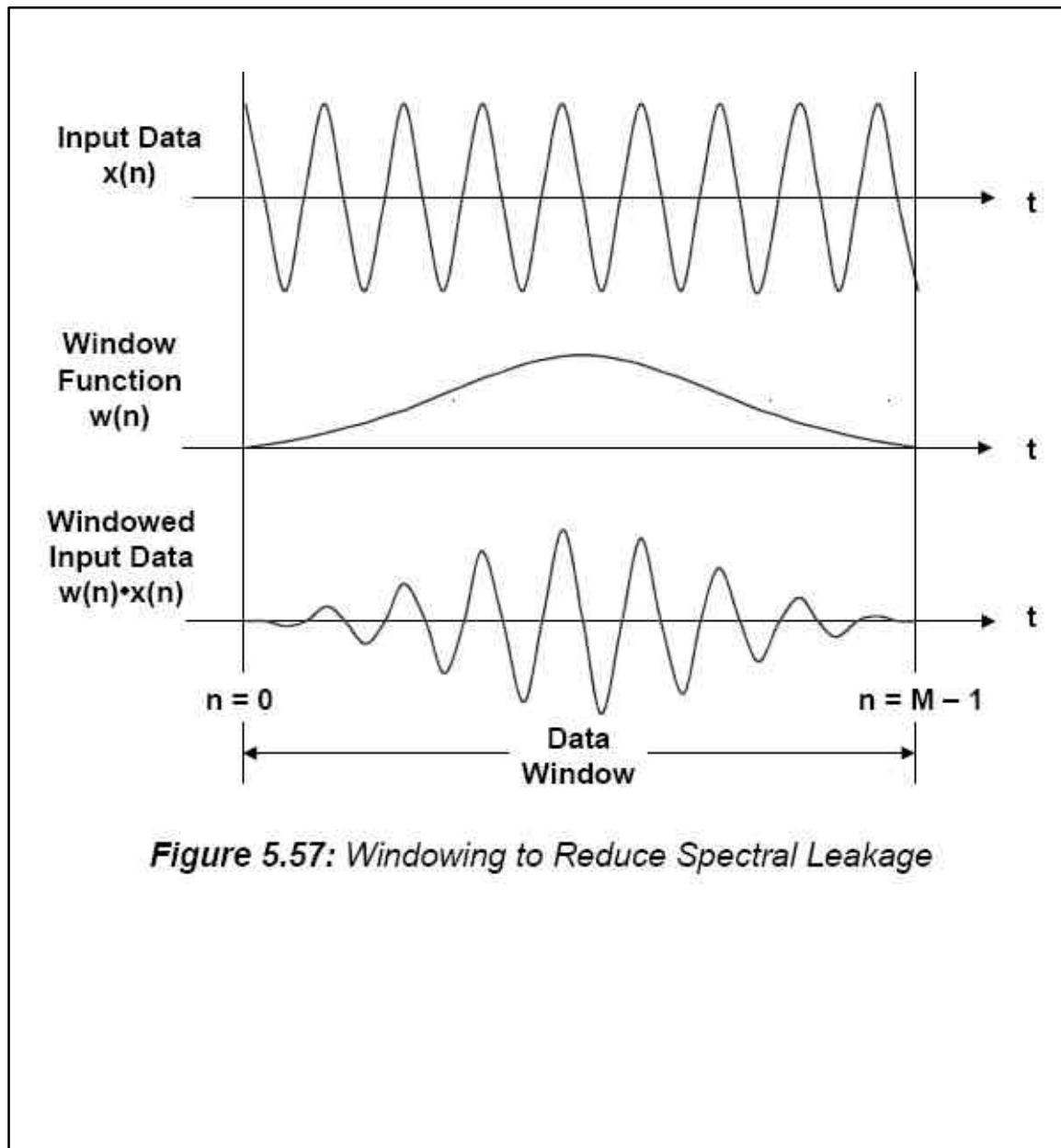


**Figure 5.55: FFT of Sinewave Having Integral Number of Cycles in Data Window**

**Notes**



**Figure 5.56: FFT of Sinewave Having Non-Integral Number of Cycles in Data Window**

**Notes**



**Notes**

◆ **Hamming:**  $w(n) = 0.54 - 0.46 \cos \left[ \frac{2\pi n}{M} \right]$

◆ **Blackman:**  $w(n) = 0.42 - 0.5 \cos \left[ \frac{2\pi n}{M} \right] + 0.08 \cos \left[ \frac{4\pi n}{M} \right]$

◆ **Hanning:**  $w(n) = 0.5 - 0.5 \cos \left[ \frac{2\pi n}{M} \right]$

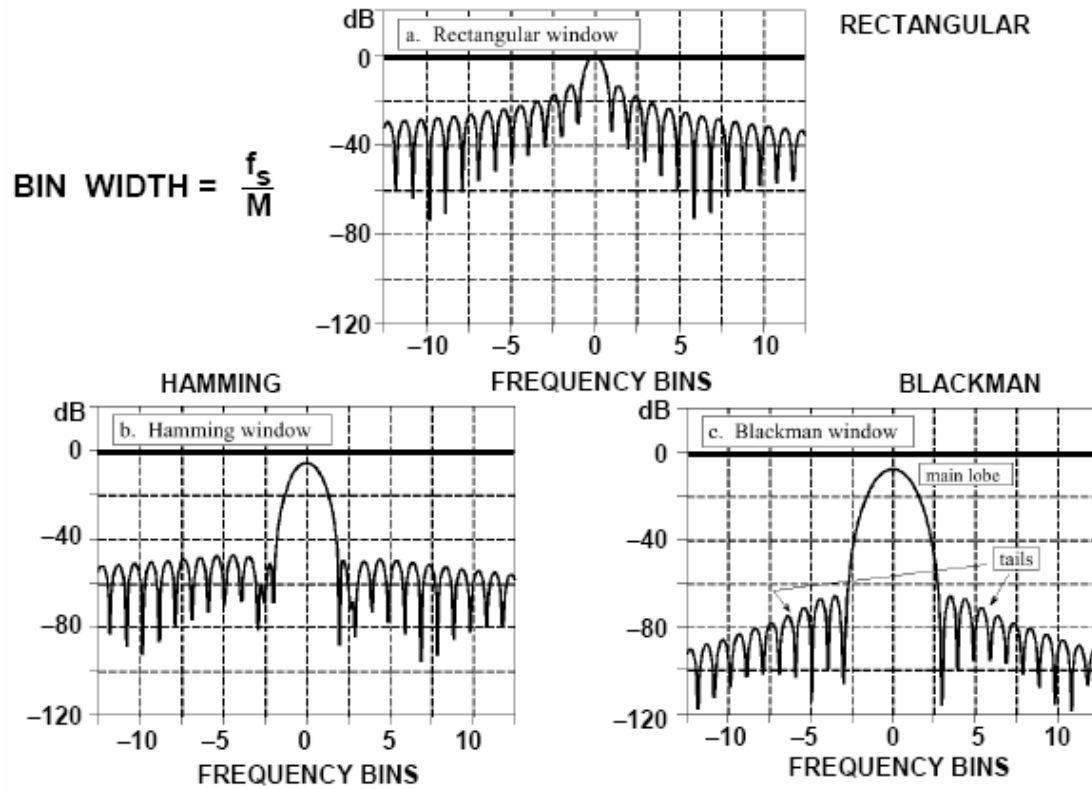
◆ **Minimum 4-Term Blackman Harris**

$$w(n) = 0.35875 - 0.48829 \cos \left[ \frac{2\pi n}{M} \right] + 0.14128 \cos \left[ \frac{4\pi n}{M} \right] - 0.01168 \cos \left[ \frac{6\pi n}{M} \right]$$

$0 \leq n \leq M - 1$

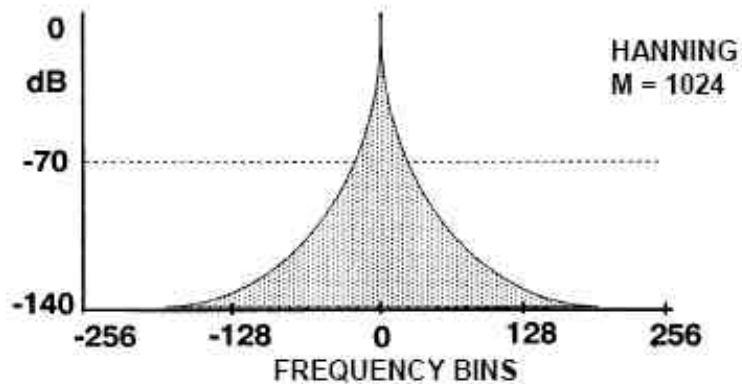
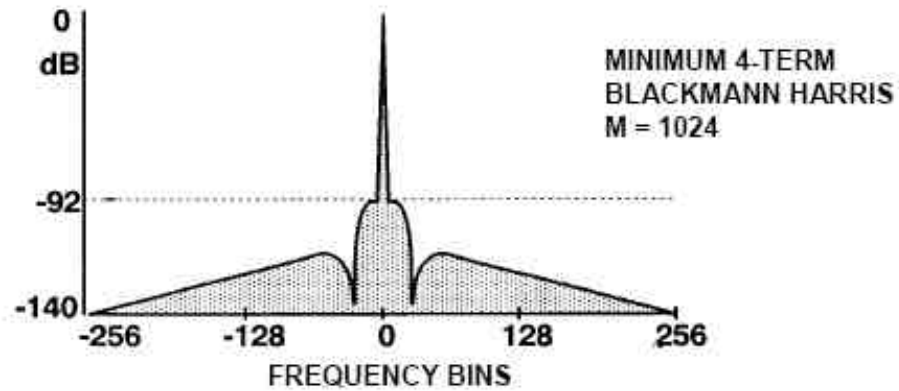
*Figure 5.58: Some Window Functions*

**Notes**



**Figure 5.59: Frequency Response of Rectangular, Hamming, and Blackman Windows for  $M = 256$**

**Notes**

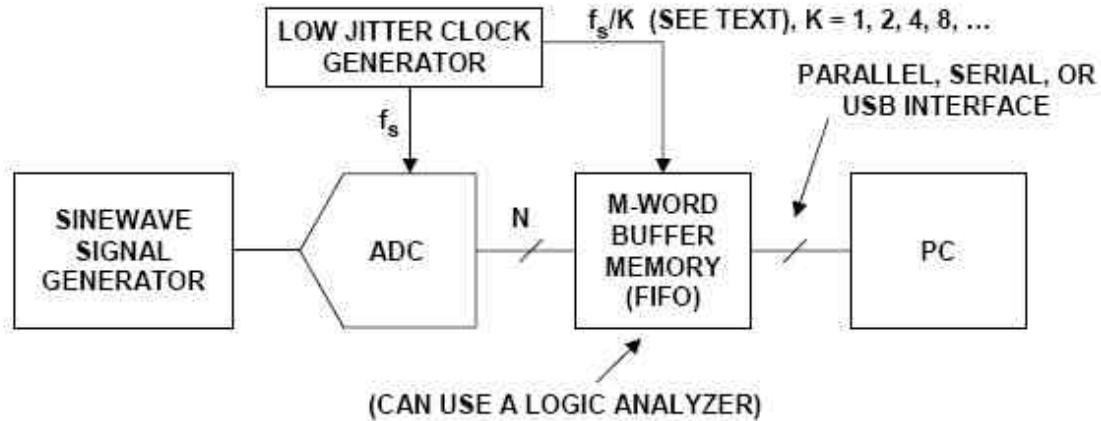


*Figure 5.60: Comparison of Two Popular Window Functions Used in ADC Testing*

**Notes**

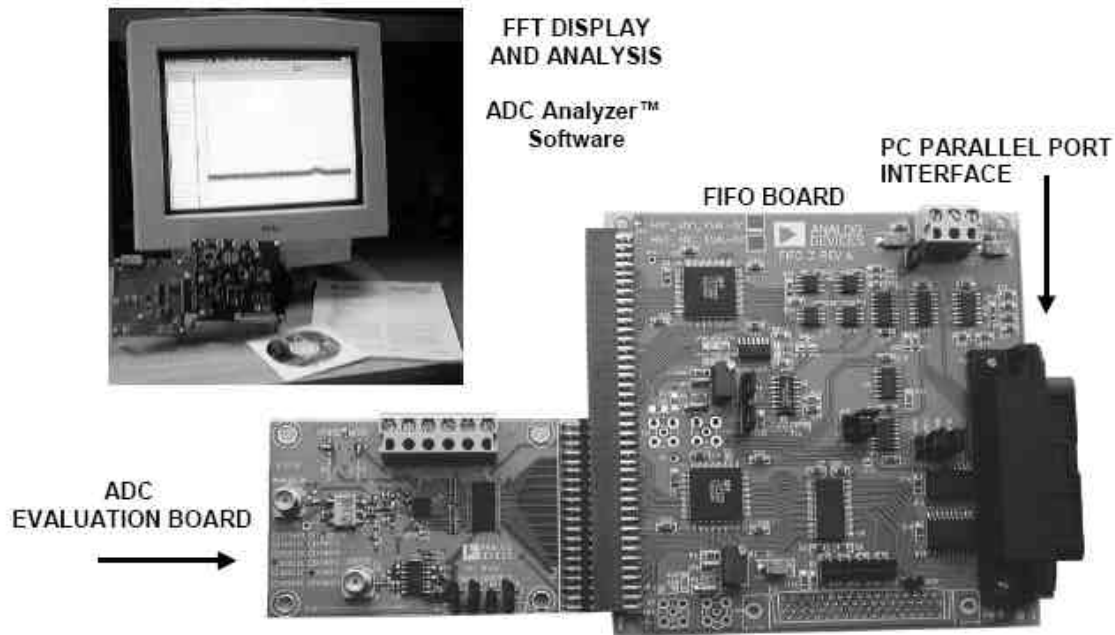
| WINDOW FUNCTION                | 3dB BW (Bins) | 6dB BW (Bins) | HIGHEST SIDELOBE (dB) | SIDELOBE ROLLOFF (dB/Octave) |
|--------------------------------|---------------|---------------|-----------------------|------------------------------|
| Rectangle                      | 0.89          | 1.21          | -12                   | 6                            |
| Hamming                        | 1.3           | 1.81          | -43                   | 6                            |
| Blackman                       | 1.68          | 2.35          | -58                   | 18                           |
| Hanning                        | 1.44          | 2.00          | -32                   | 18                           |
| Minimum 4-Term Blackman-Harris | 1.90          | 2.72          | -92                   | 6                            |

*Figure 5.61: Popular Windows and Figures of Merit*

**Notes**

*Figure 5.62: FFT Test Setup*

**Notes**



*Figure 5.63: Analog Devices' High Speed ADC FIFO Evaluation Kit*