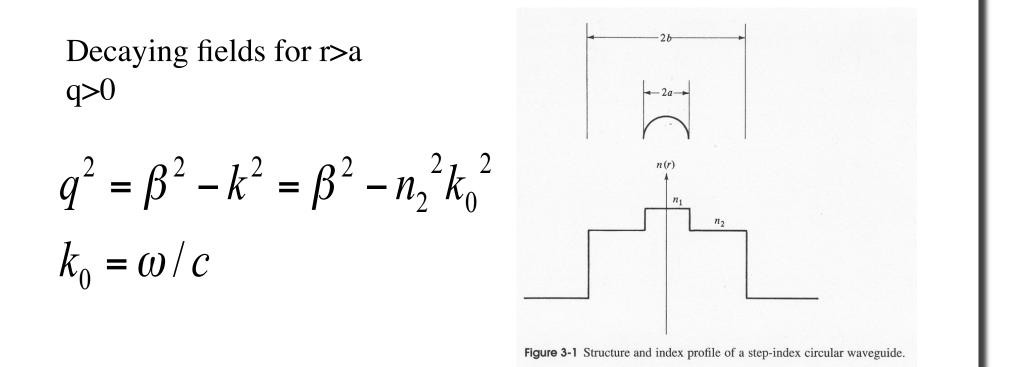
Lecture 5 - Propagation in Optical Fibers and Dispersion

Reading and Homework

- ⇒ Read Chapters 1 and 2 of Agrawal
- \Rightarrow HW #2 due Thursday Oct. 18
- ⇒ Reminder HW #1 due Thursday Oct. 11

Boundary Conditions



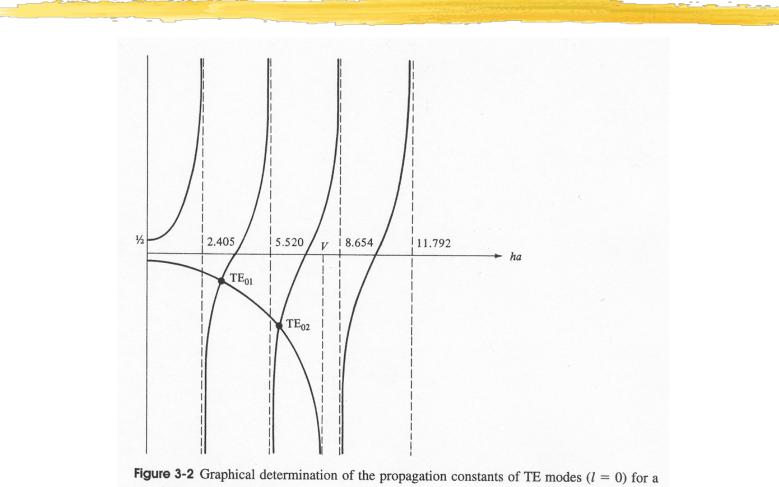
For fields in the core r<a, we need finite fields (which eliminates Y and K which go to infinity as r approaches 0.

Boundary Conditions

- ⇒ In order for the mode to be supported, it must be a standing wave pattern along r inside the core and a decaying exponential along r inside the cladding, with the boundary conditions supported at the step interface.
- $\Rightarrow \beta$ is therefore bounded by

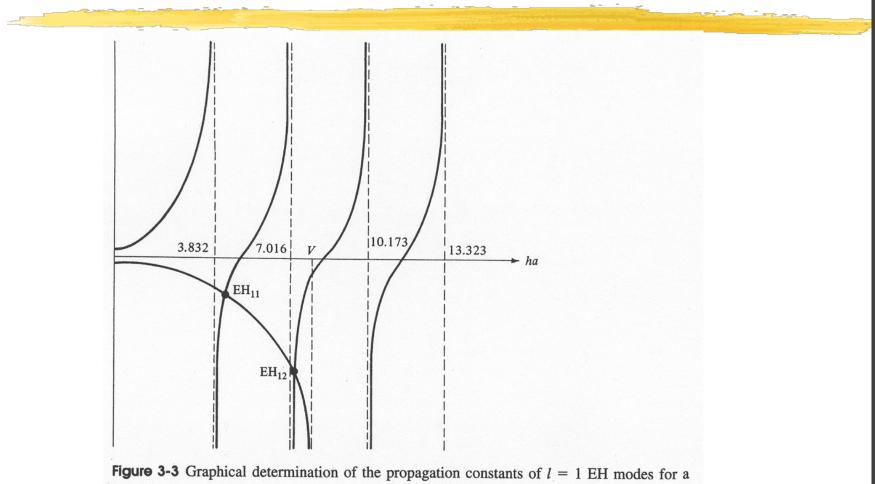
 $n_1 k_0 \le \beta \le n_2 k_0$

TE 1=0 Modes



step-index waveguide.

l=1 (not TE or TM, but EH)



step-index fiber.

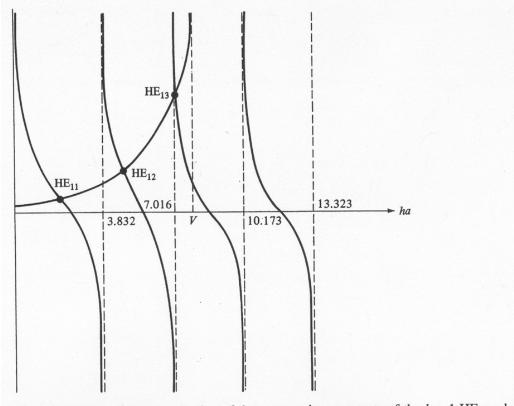


Figure 3-4 Graphical determination of the propagation constants of the l = 1 HE modes for a step-index dielectric waveguide.



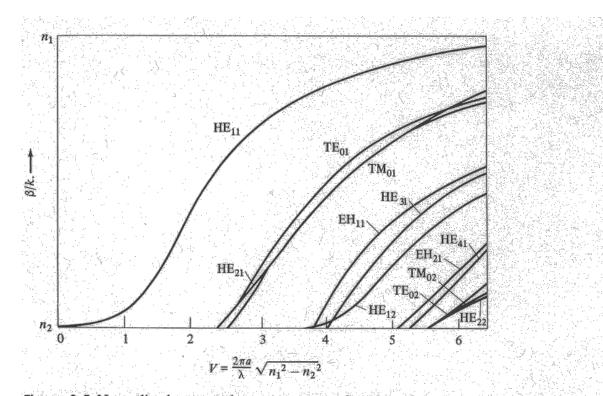
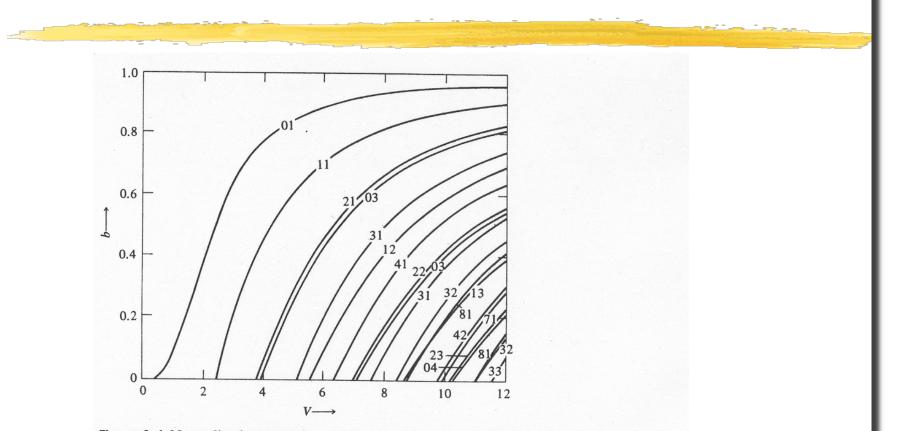
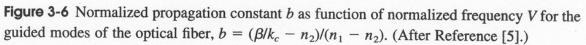


Figure 3-5 Normalized propagation constant as a function of V parameter for a few of the lowest-order modes of a step-index waveguide [4].

For n1-n2<<n1, LP approximation is valid.

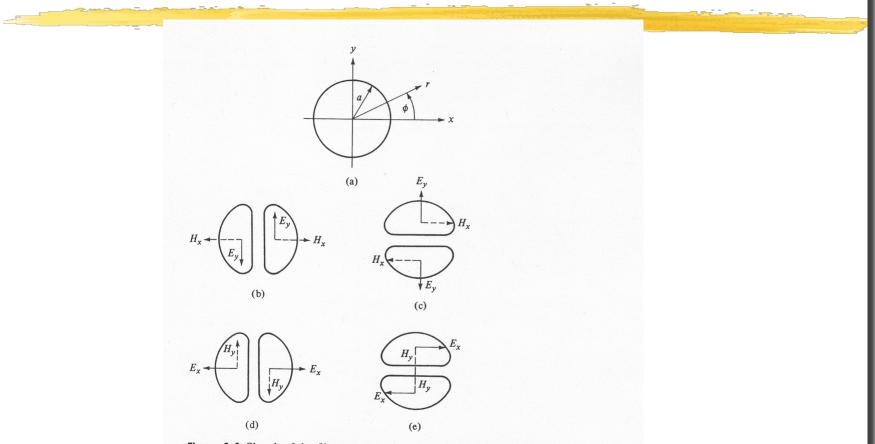




Single mode cut off: V=2.405

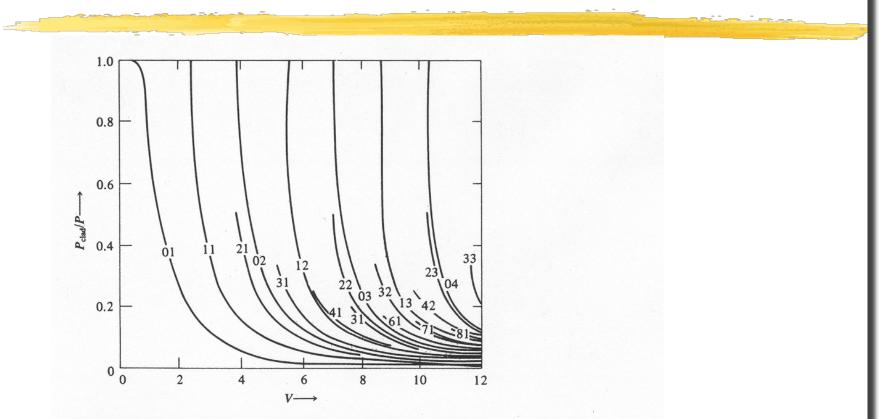
ECE 228A Fall 2008 Daniel J. Blumenthal

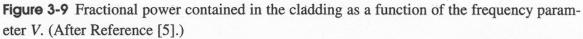
Degenerate Modes LP₁₁





Modes as a function of V parameter



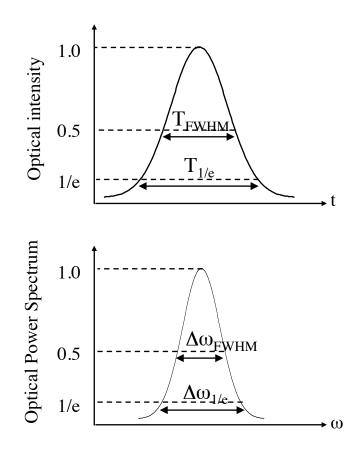


At cutoff, all the power is in the cladding.

Dispersion in Single Mode Fibers

- Modal dispersion in multimode fibers is not present in single mode fiber (SMF)
- ⇒ However, other types of dispersion are present in SMF
 - ⇒ Material dispersion
 - ⇒ Waveguide dispersion
 - ⇒ Polarization mode dispersion
- ⇒ The first two effects fall under the term "Chromatic Dispersion"
- \Rightarrow The third effect is known as PMD
- ⇒ Dispersion can set the ultimate bit-rate limit in single mode fiber when loss and fiber nonlinearities are not dominant

Gaussian Pulses



➡ Define rms pulsewidth and bandwidth values:

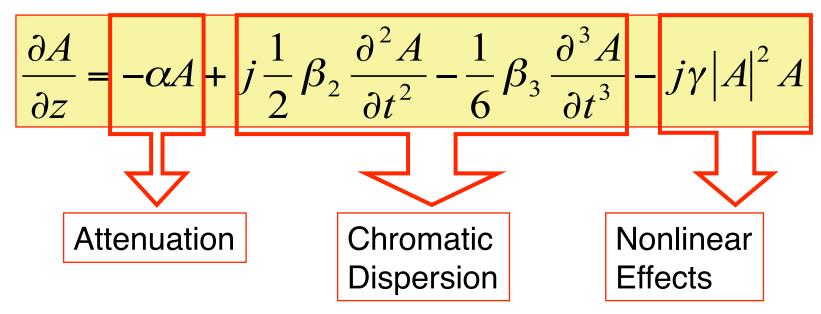
- $rightarrow \sigma_0 = T_{1/e} / \sqrt{2}$ (rms pulse width)
- $\Rightarrow \sigma_{\omega} = \Delta \omega_{1/e} / \sqrt{2}$ (rms spectral width)
- Define linear chirp factor
 C

Define relation between pulse width and bandwidth

$$\Delta \omega_{1/e} = (1 + C^2)^{1/2}/T_0$$

Non-Linear Schrodinger Equation

- Both linear (dispersive) and nonlinear effects must be taken into account for pulse propagation in the fiber
- ⇒ The propagation of a signal in a single mode fiber is set (to a very high level of accuracy) by the following equation, called the nonlinear Schrodinger equation:



- \Rightarrow A(z,t) is the complex-envelope of the optical field
- \Rightarrow The resulting optical power is $P(z,t) = |A(z,t)|^2$