



Lecture 1: Overview of Optical Communications Links and Intro to Photodetection



Overview of Optical Communications Links

Fiber-Optic Network Applications

⇒ Main application: digital transmission

⇒ Voice, telephone

⇒ Data

⇒ IP Networks

⇒ ATM, Gigabit Ethernet, FDDI, etc.

⇒ Distributed Computing and Databases

⇒ Video, Multimedia



Note:

Traffic generated by data-centric application (mainly IP) is rapidly surpassing the voice-centric traffic

⇒ Microwave Photonics

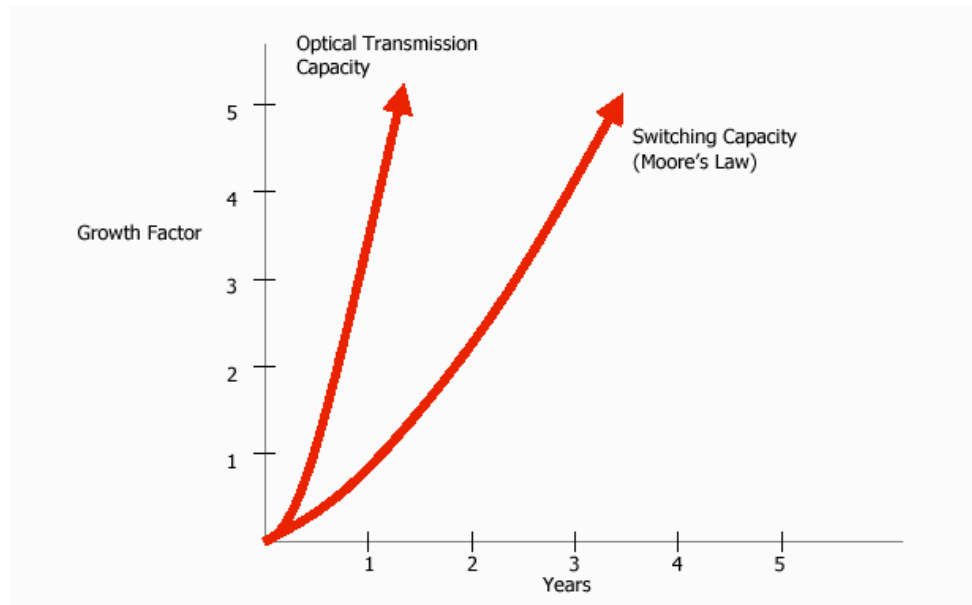
⇒ Fiber/Wireless

⇒ Hybrid Fiber/Coax

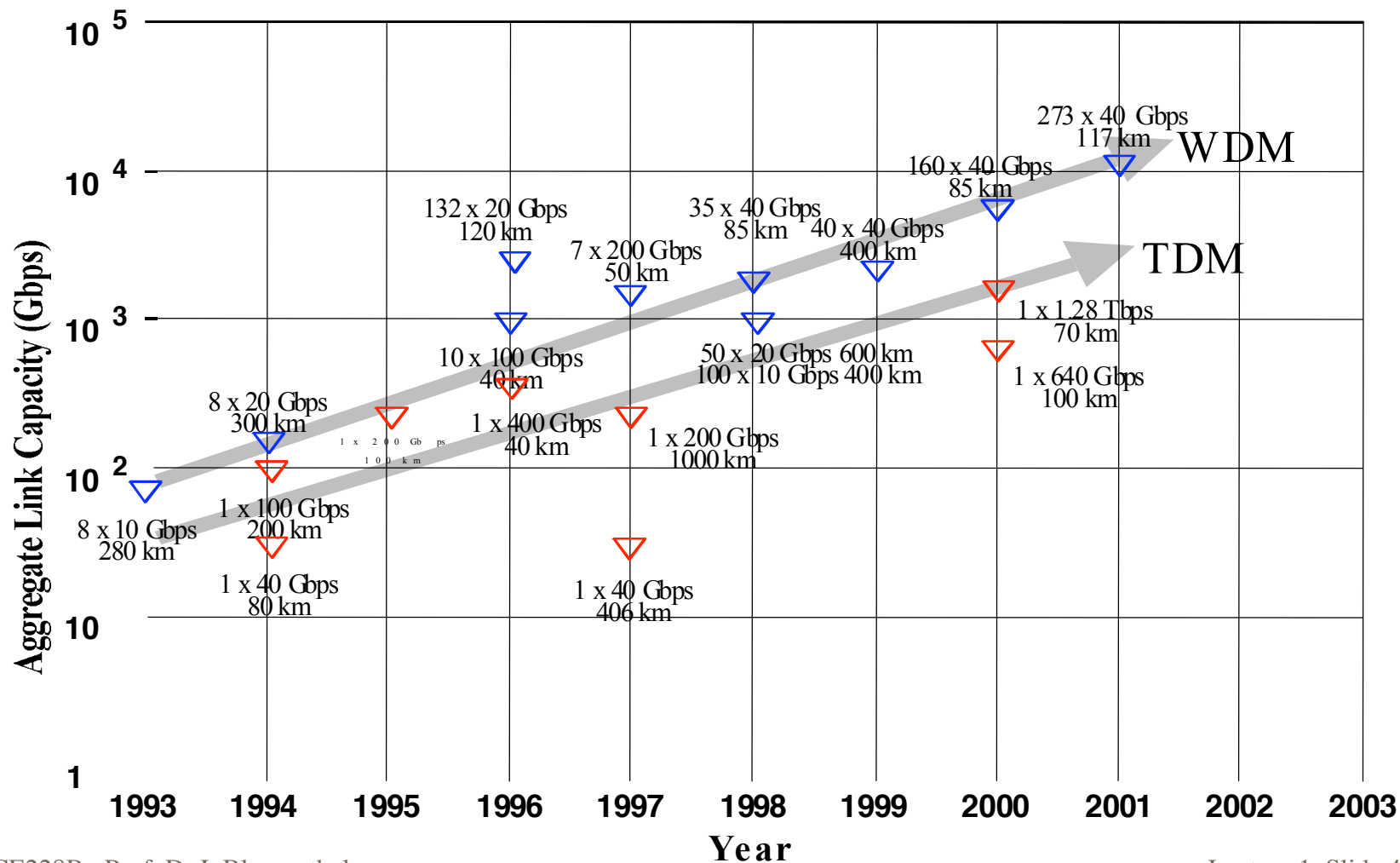
⇒ Other applications

⇒ Fiber/Wireless

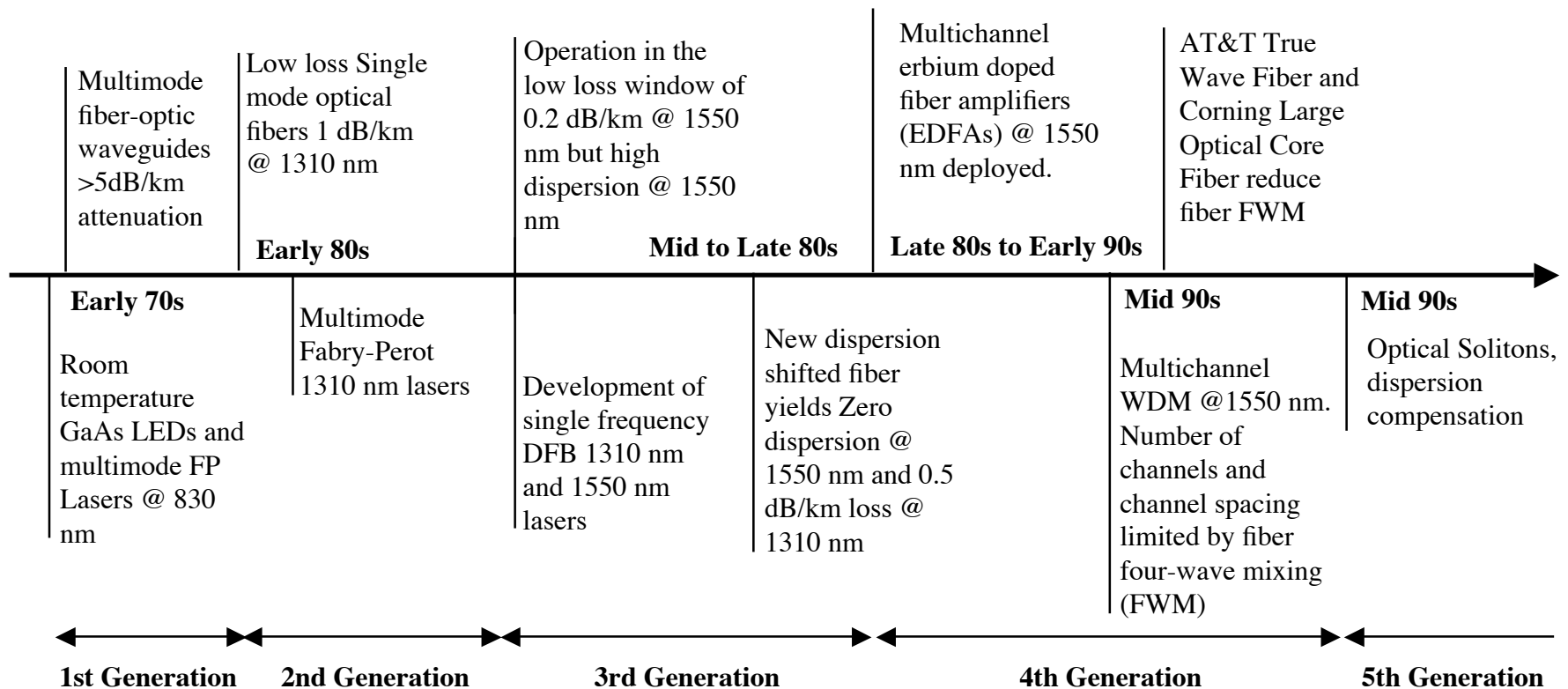
⇒ Hybrid Fiber/Coax



Transmission Bandwidth Evolution

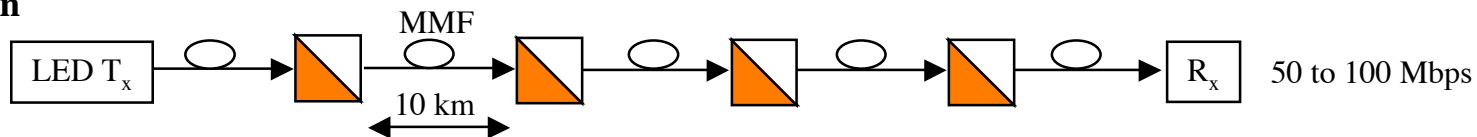


Evolution of Fiber-Optic Point-to-Point Transmission

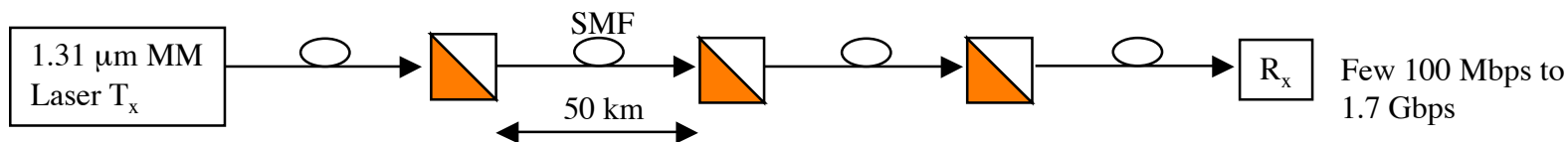


DWDM Link Evolution

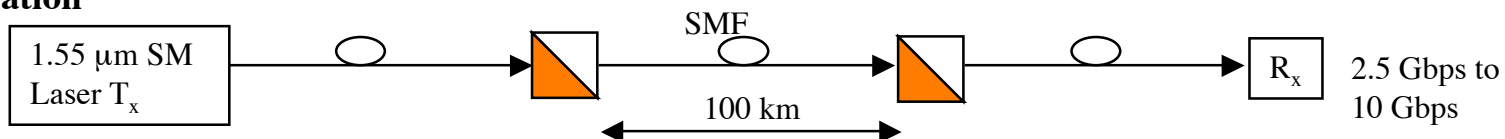
1st Generation



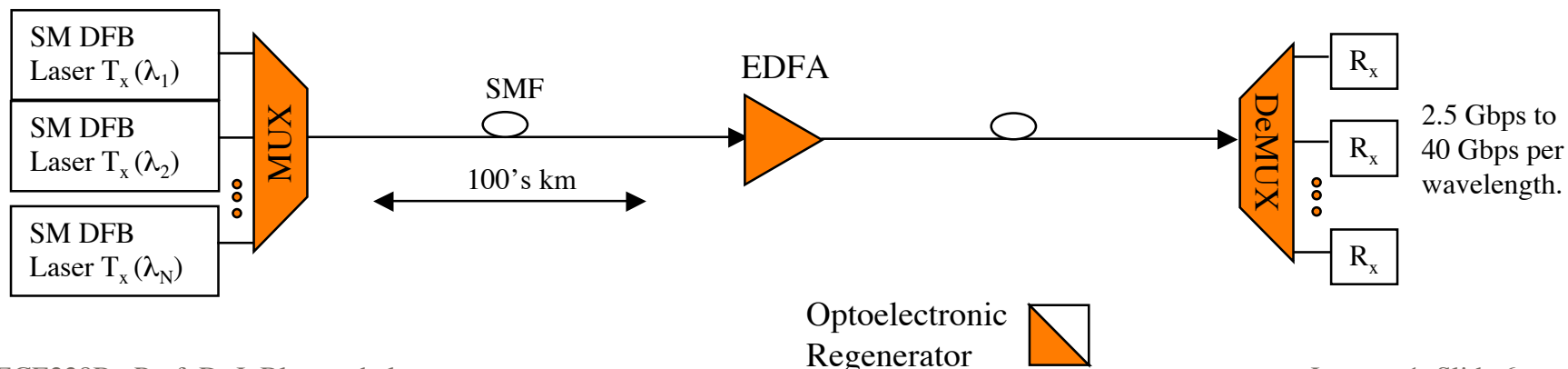
2nd Generation



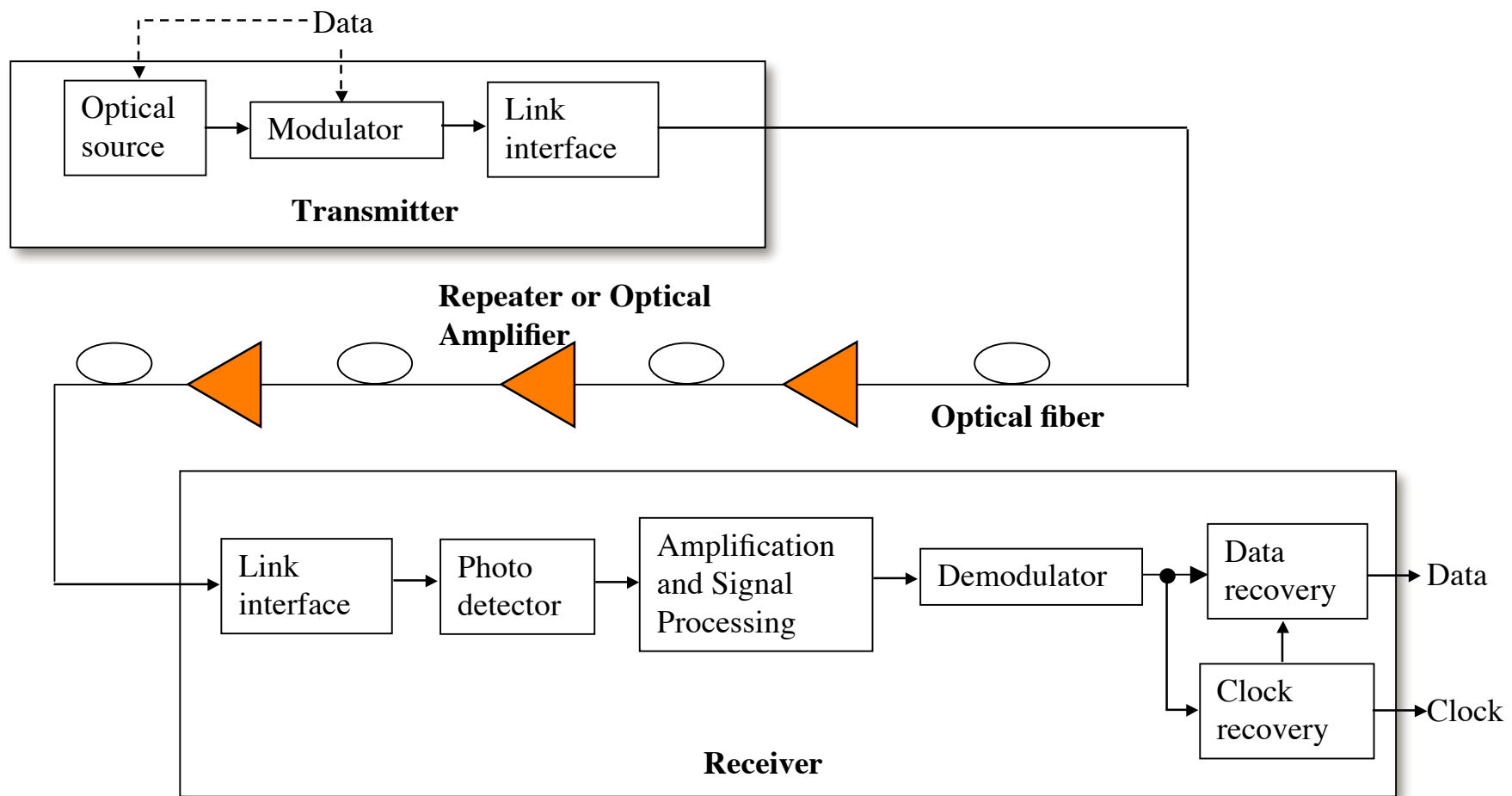
3rd Generation



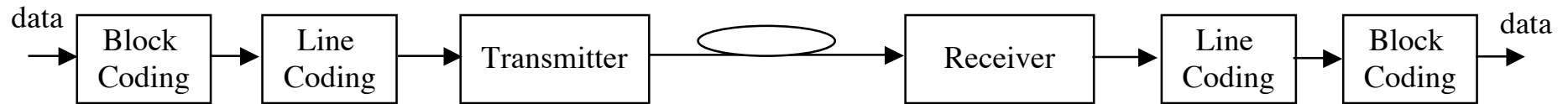
4th Generation



Basic Fiber Optic Point-to-Point Link



Basic Communication System



Block Coding

- Error Correction
- Redundancy
- Overcome noise and transmission impairments
- E.g. FEC, Turbo-Codes

Line Coding

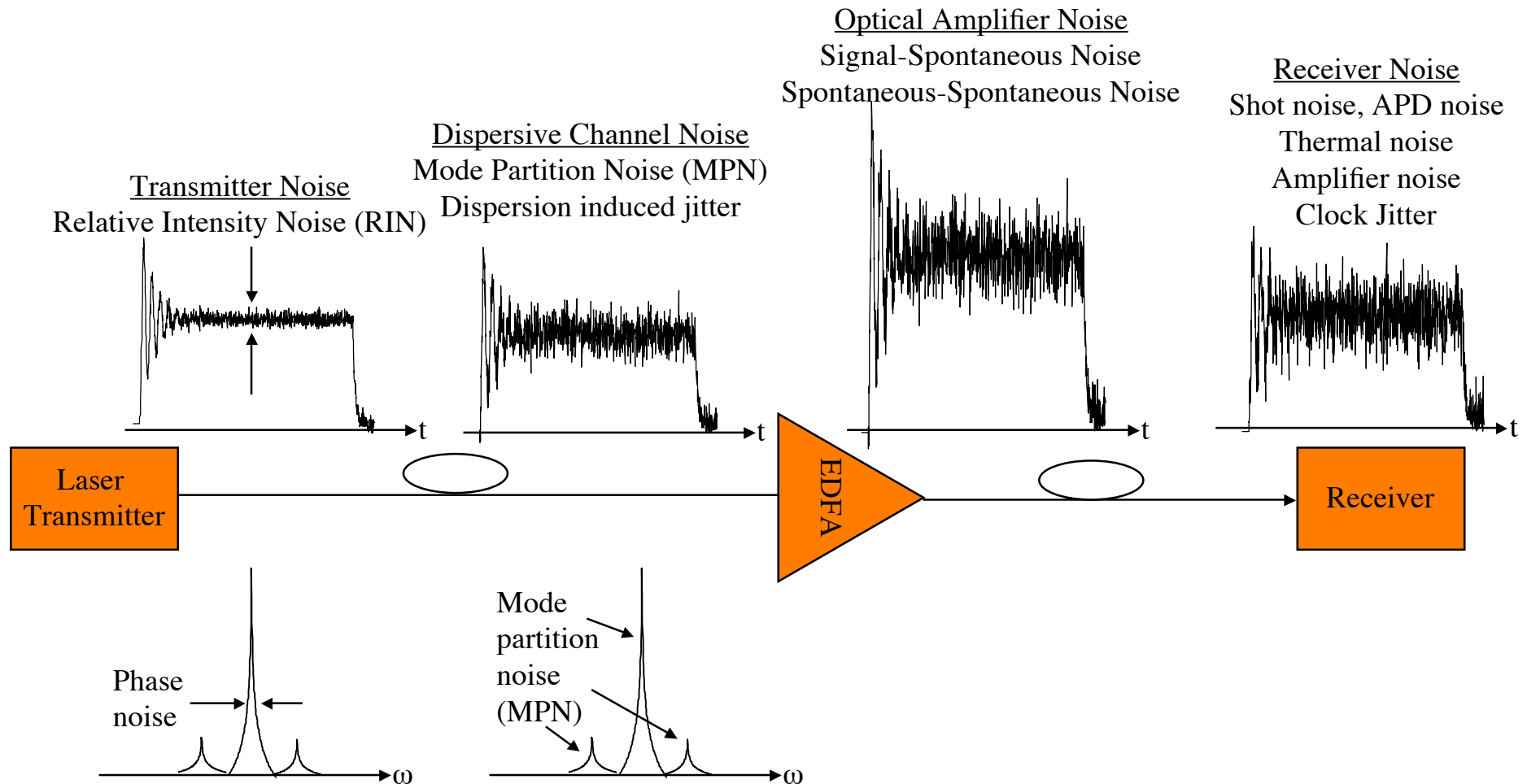
- DC balance
- Redundancy
- E.g Manchester Codes

Link Capacity and Spectral Efficiency

- ⇒ Capacity of an optical communications channel is the maximum bit rate that can be transmitted without error for a given noise, bandwidth and power.
- ⇒ Capacity can be calculated independent of modulation, coding or decoding technique
- ⇒ For a WDM (Wavelength Division Multiplexed) optical communications system

$$S = \text{Spectral Efficiency} = \frac{\text{Capacity per Channel}}{\text{Channel Spacing}} = \frac{C}{\Delta f} = \frac{\text{Bits/Second}}{\text{Hz}}$$

Signal to Noise Ratio (SNR)





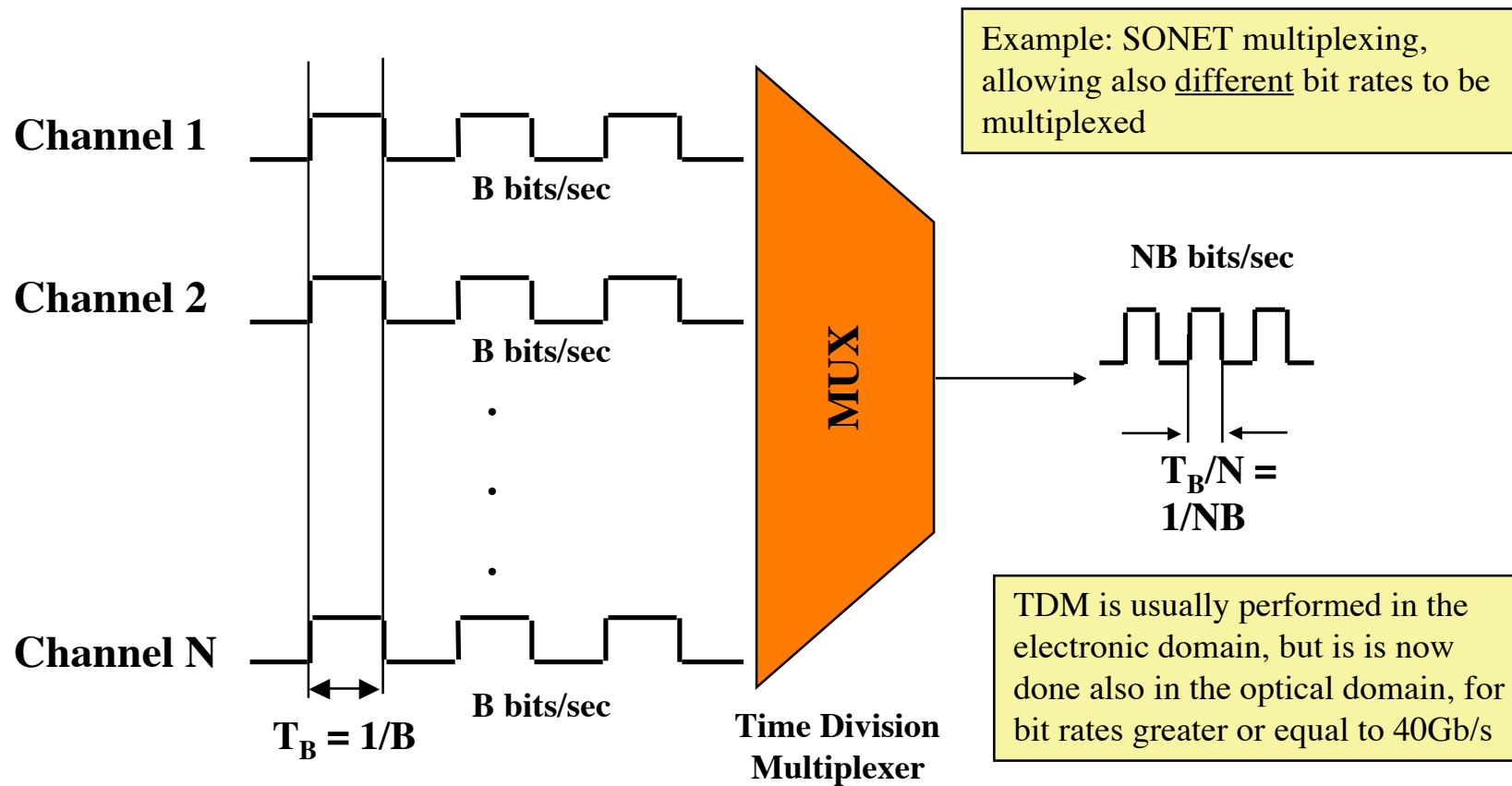
Multiplexing Techniques

Multiplexing Techniques

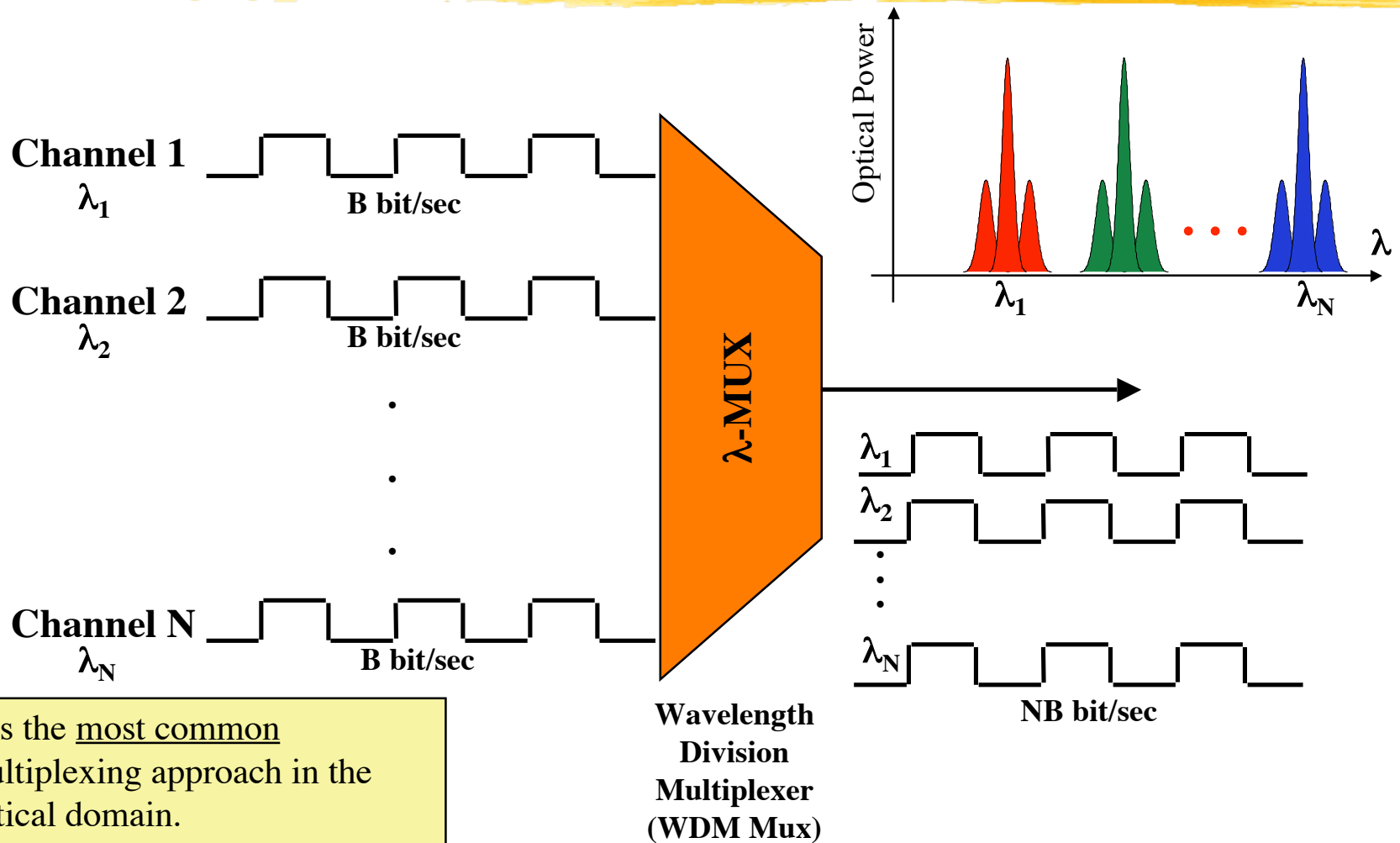


- ⇒ Multiplexing is the technique used to carry several different information channels on a common physical medium. The standard techniques are:
 - ⇒ Time Division Multiplexing (TDM)
 - ⇒ Frequency Division Multiplexing, indicated as “Wavelength Division Multiplexing” (WDM) in optics
 - ⇒ Space Division Multiplexing (SDM)
 - ⇒ Code Division Multiplexing (CDMA)
 - ⇒ Multilevel coding

Time Division Multiplexing (TDM)

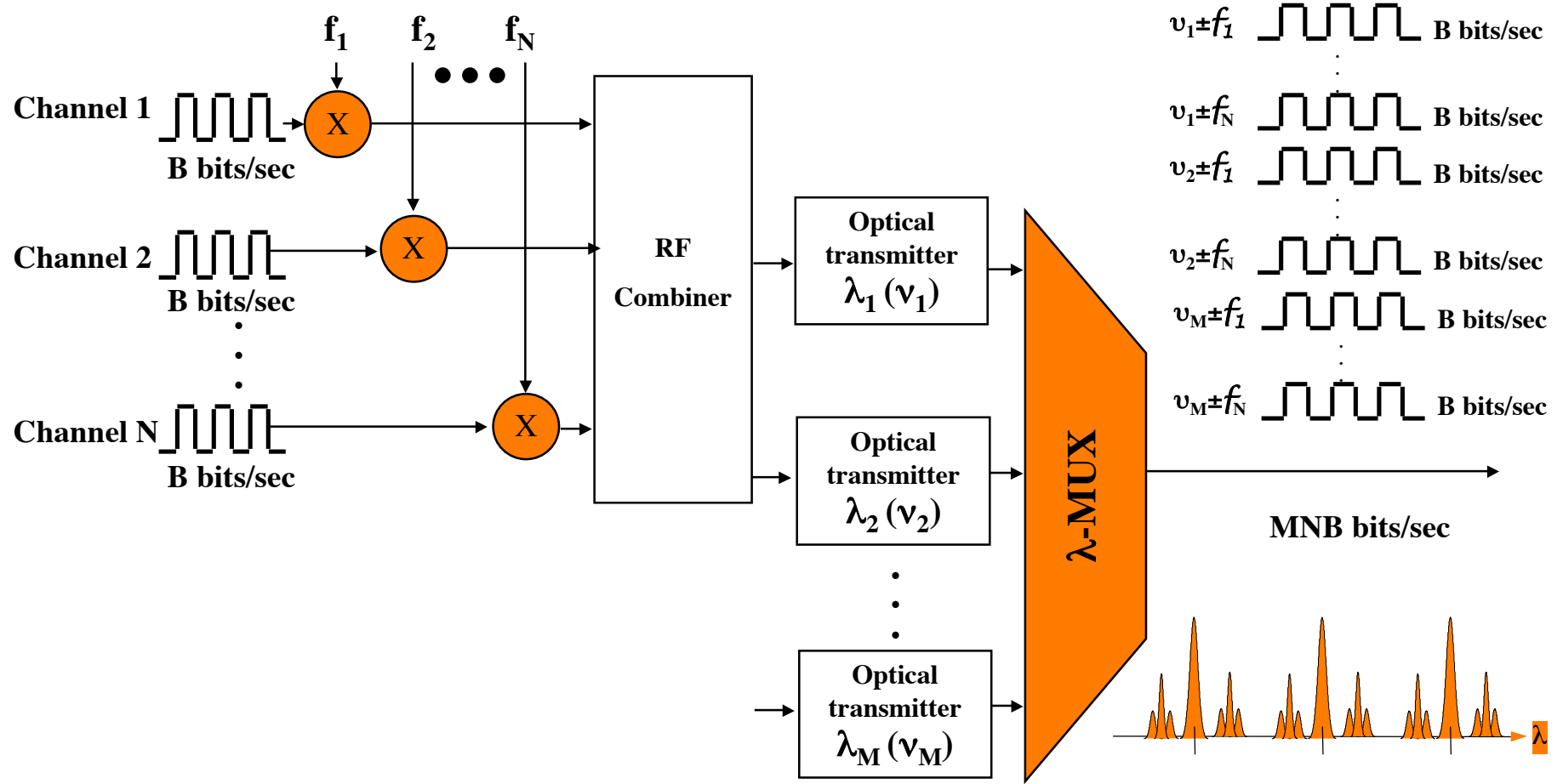


Wavelength Division Multiplexing (WDM)



It is the most common multiplexing approach in the optical domain.

Wavelength/Subcarrier Multiplexing





Optical Modulation

Modulation Basics (I)

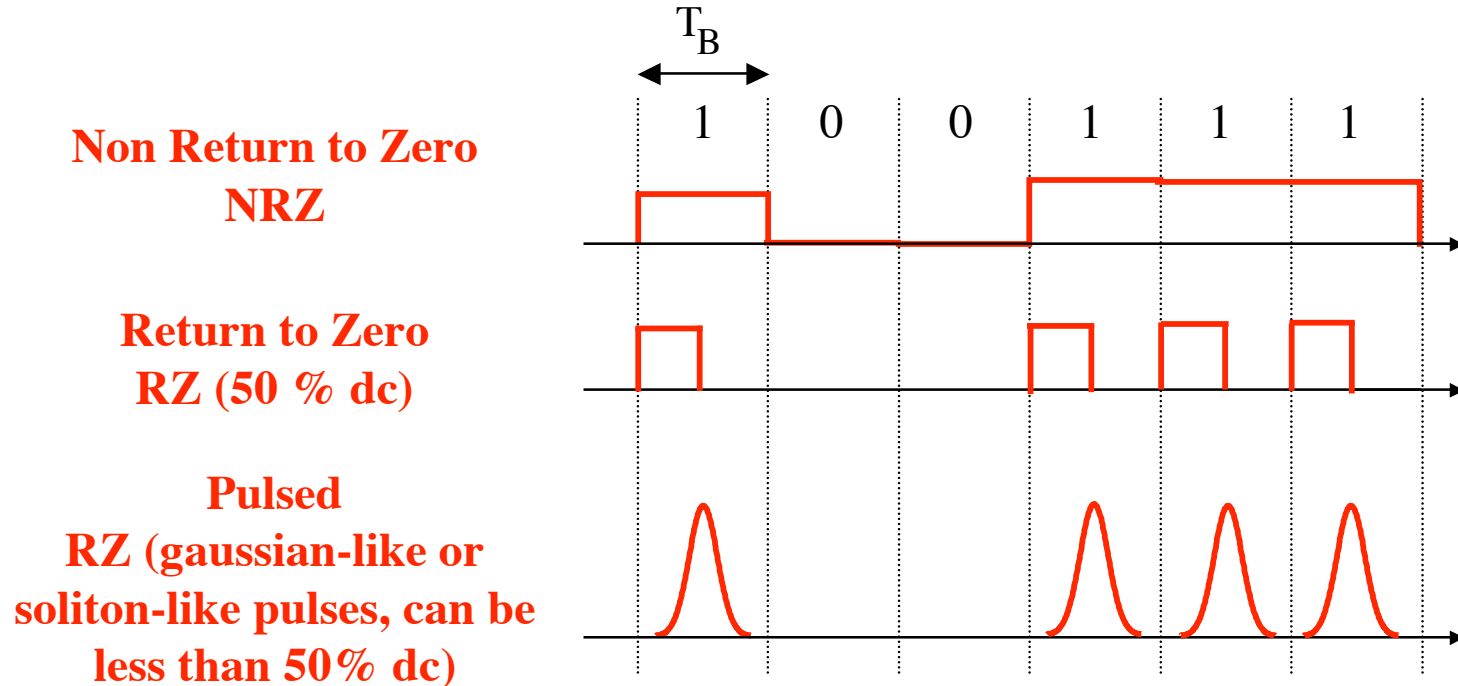
- ⇒ Define
 - ⇒ R_b = bit rate = bits/second
 - ⇒ R_c = added redundancy per bit to improve SNR = baud = symbols/second
 - ⇒ B = occupied bandwidth per channel
 - ⇒ M = number of points in signal constellation
- ⇒ Binary Modulation
 - ⇒ One bit per symbol
- ⇒ Non-Binary Modulation
 - ⇒ More than one bit per symbol
- ⇒ No inter-symbol interference (ISI)
 - ⇒ $R_s \leq B$
- ⇒ Error correction
 - ⇒ $R_c \leq 1$
- ⇒ No error correction
 - ⇒ $R_c = 1$

Information bit rate per channel
in one polarization state

$$R_b = R_s R_c \log_2 M$$

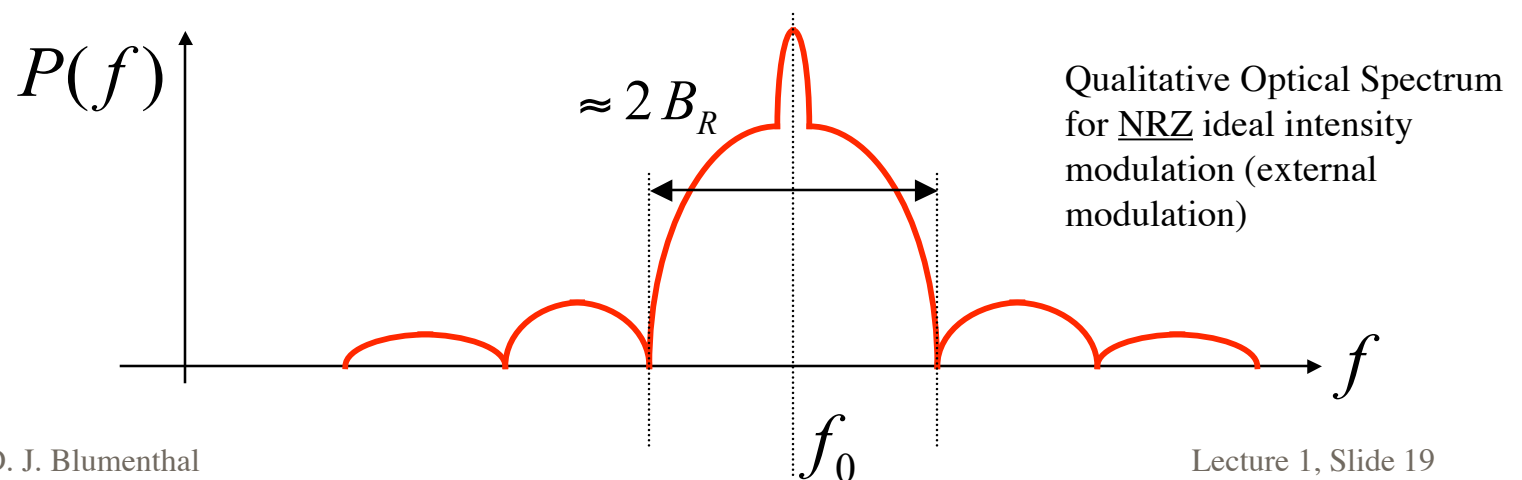
Binary Intensity Modulation

- ⇒ The primary modulation format used for commercially deployed optical systems are intensity modulation (optical power modulation)

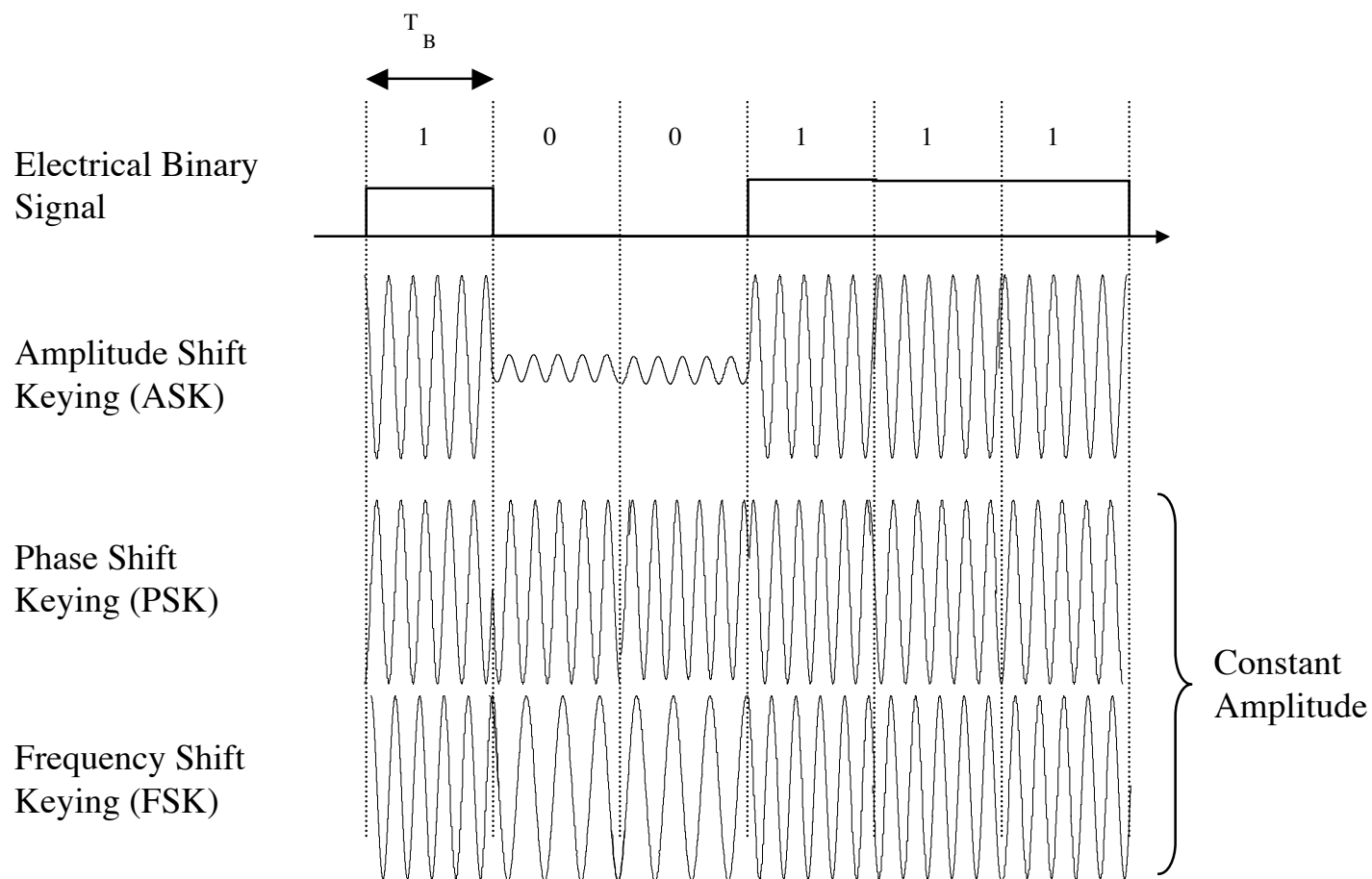


Optical spectrum for intensity modulation

- ⇒ If the intensity modulation is imposed to the optical signal together with unwanted phase or frequency modulation (e.g. chirp under direct laser modulation, excess laser phase noise)
 - ⇒ The resulting optical spectrum is larger than the bit rate
- ⇒ If the modulation is a (nearly) pure intensity modulation, without any accompanying phase/frequency shift (e.g. external modulation)
 - ⇒ The resulting spectrum has a primary lobe that occupies the order of the bit rate

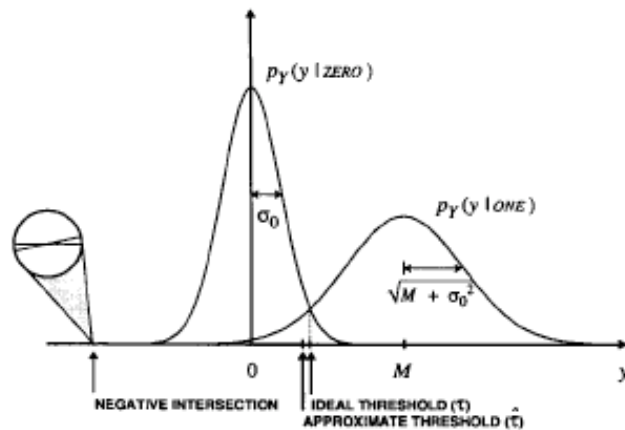


Coherent Binary Modulation

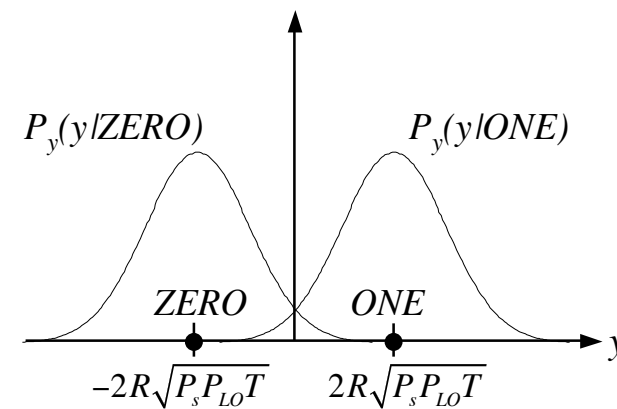


Binary Signal Constellations

Binary Intensity Modulation/Direct Detect (IM/DD)



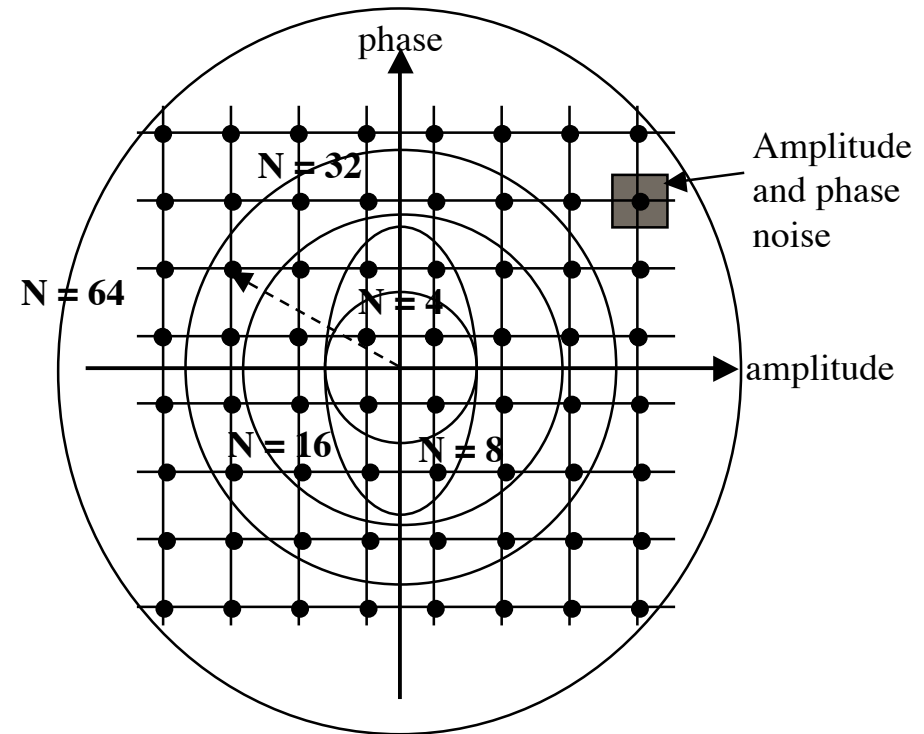
Two-Level PSK



M = average power in 1 bit
 σ_0 = variance of signal independent noise
 P_s = average signal power
 P_{LO} = average local oscillator power
 T = bit period

Quadrature Multi-Level Modulation

- ⇒ Both optical phase and amplitude can be used to code symbols per bit
- ⇒ N-ASK is N-level amplitude shift keying (generalization of ASK): along amplitude axis
- ⇒ N-PSK is N-level phase shift keying (PSK): along phase axis
- ⇒ N-QAM is quadrature amplitude modulation: 2D in amplitude and phase
- ⇒ Receiver must isolate one point in constellation per bit
- ⇒ Noise makes more difficult to isolate symbol (SNR)
- ⇒ 2-D space can be increased to 3 and 4-D by allowing temporal modulation of phase and amplitude





Photodetection

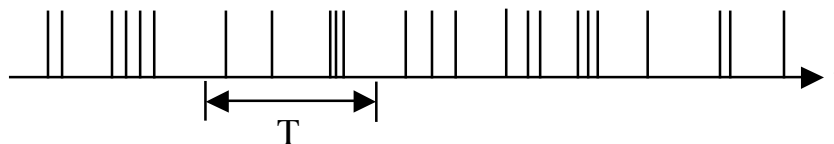
Detection of Optical Signals



- ⇒ Thermal: Temperature change with photon absorption
 - ⇒ Thermoelectric
 - ⇒ Pyromagnetic
 - ⇒ Pyroelectric
 - ⇒ Liquid crystals
 - ⇒ Bolometers
- ⇒ Wave Interaction: Exchange energy between waves at different frequencies
 - ⇒ Parametric down-conversion
 - ⇒ Parametric up-conversion
 - ⇒ Parametric amplification
- ⇒ Photon Effects: Generation of photocarriers from photon absorption
 - ⇒ Photoconductors
 - ⇒ Photoemissive
 - ⇒ Photovoltaics

Photon Statistics

- ⇒ Photon sources can in general be characterized as coherent or incoherent[†]
 - ⇒ Coherent: Probability that a photon is generated at time t_0 is mutually independent of probability of photons generated at other times (Markov Process)
 - ⇒ Poisson Process: Probability of finding n photons in time interval T
 - ⇒ Bunching is a trait of the Poisson process
 - ⇒ Interarrival time is decaying exponentially distributed



$$P(n | T) = \frac{(rT)^n e^{-rT}}{n!}$$

[†] Can also be a combination of these two types -> partially coherent

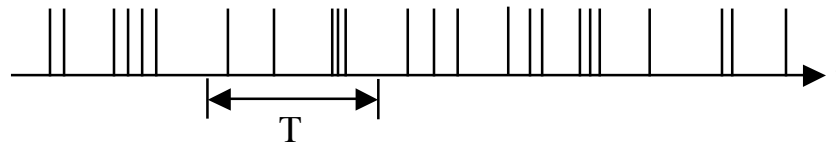
Where :

$P(n|T)$ is probability of finding n photons in time interval T
 R is mean photon arrival rate (photons/second)

Photon Statistics (II)

⇒ Narrowband Thermal (Gaussian):

⇒ Bose-Einstein Process: Probability of finding n photons in time interval T



$$P(n) = \left(\frac{1}{1 + n_b} \right) \left(\frac{n_b}{1 + n_b} \right)^n$$

Where :

$P(n)$ = probability of finding n photons given

n_b = mean number photons from incoherent source = $N_0/h\nu_0$

N_0 = spectral density of source = P_{opt}/B_0

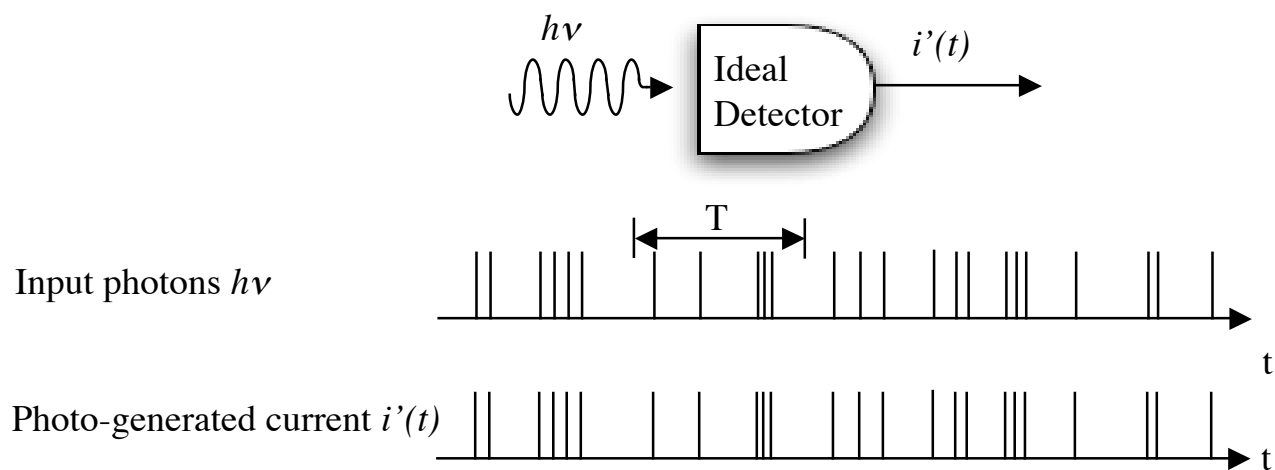
P_{opt} = total optical power from source

B_0 = source optical bandwidth

T = observation time $\leq 1/B_0$

Detecting Photons (1)

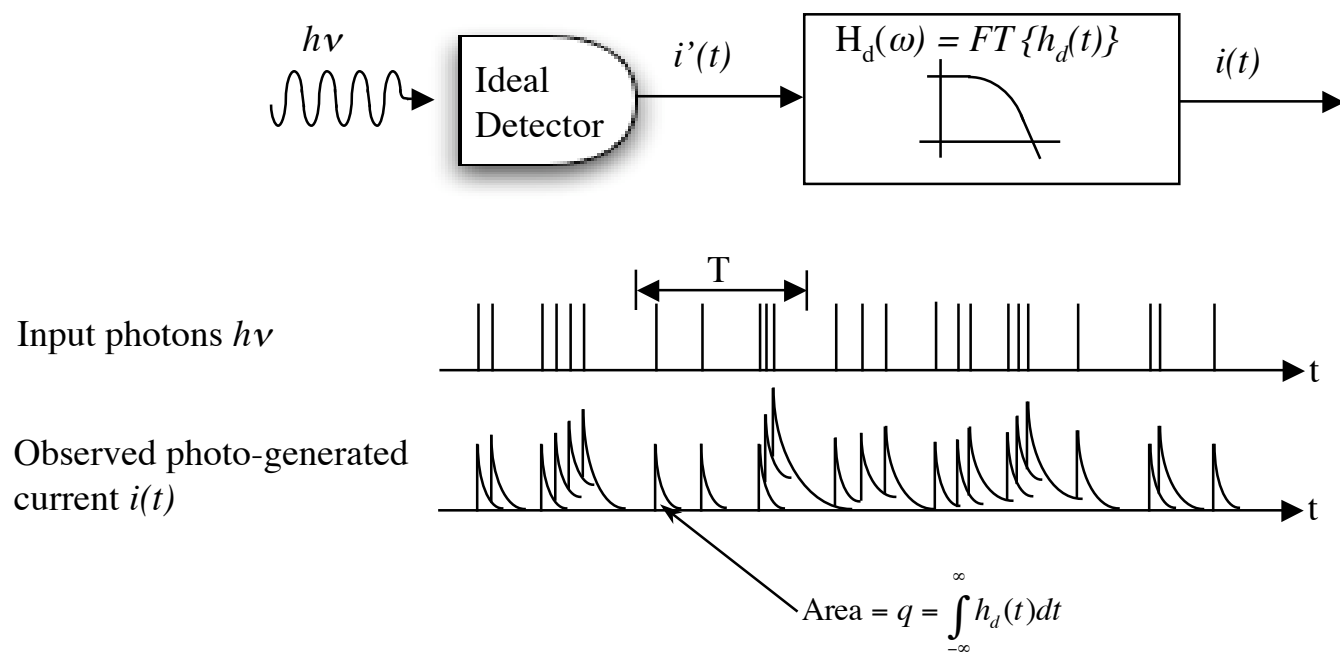
- ⇒ Any material that can respond to single photons can be used to count photons
- ⇒ Ideal Detector
 - ⇒ Generation of a electron-hole pair per absorbed photon results in an instantaneous current pulse



Detecting Photons (2)

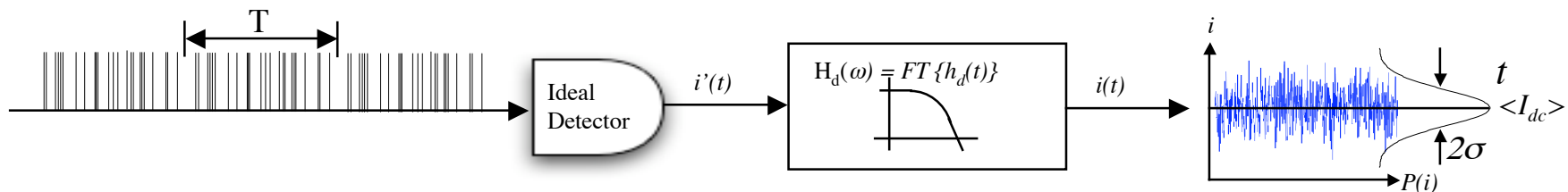
⇒ Real Detector

- ⇒ Has an inherent “impulse response,” $h_d(t)$, due to built in resistance and/or capacitance.
- ⇒ Can be modeled as an RC filter with low pass response



Detecting Photons (3)

- ⇒ As the average photon rate increases, the observed photo-current starts smoothing out, with a variance around the mean (average) count that is based on the statistics (which tends to Gaussian for large photon arrival rate)
- ⇒ $P(i)$ is the probability function of measuring the current at a certain value at time t .



Detecting Photons (4)

⇒ The detector output current $i(t)$ can be modeled as a discrete “filtered Poisson” process

$$i(t) = \sum_{j=1}^N h_d(t - \tau_j)$$

⇒ Where $h_d(t)$ is PD impulse response, N is total number e-h pairs generated, τ_j is the random time the j^{th} photocarrier is generated.

⇒ Define: Quantum Efficiency (QE), unitless, as

$$\eta = \frac{\text{number of photocarriers produced}}{\text{number of incident photons}}, 0 \leq \eta \leq 1$$

⇒ Define: Time varying photon rate parameter ($\lambda(t)$) in units of photocarriers/second as

$$\lambda(t) = \frac{\eta}{h\nu} P_{\text{recvd}}(t)$$

Detecting Photons (5)

⇒ The power incident on a photodetector of area A , in units of Watts, is

$$P(t) = \int_A I(\mathbf{p}, t) dA$$

⇒ where the instantaneous optical intensity at an observation point \mathbf{p} is given by

$$I(\mathbf{p}, t) = \frac{1}{Z_0} |E(\mathbf{p}, t)|^2$$

⇒ The time varying photon rate parameter $\lambda(t)$ can then be written in terms of $P(t)$

$$\lambda(t) = \frac{\eta}{h\nu} \frac{|E(t)|^2}{Z_0}$$

Detecting Photons (6)

- ⇒ If we consider an observation interval, over which we are going to average our photon count over
 - ⇒ This can be due either to the inherent bandwidth of the detector or (as we will see later) on purpose to match the receiver bandwidth to the data bit rate
- ⇒ Then the number of photocarriers generated over the interval T counted at the j^{th} observation interval

$$N_j = \int_0^T \lambda_j(\tau) d\tau$$

- ⇒ Assuming a coherent source, the *conditional inhomogeneous Poisson process* describes this photon count during the j^{th} observation interval

$$P(N_j = N) = \frac{\left(\int_0^T \lambda_j(\tau) d\tau \right)^N}{N!} e^{-\left(\int_0^T \lambda_j(\tau) d\tau \right)}$$

Detecting Photons (7)

⇒ If we assume a constant rate parameter over the time interval T (independent of j), then the photo-generated current can be written as

$$i(t) = \lambda(t)q$$

$$\lambda(t) = \frac{N}{T}$$

⇒ Then the photocurrent produced by the photodetector can be written in Amperes, assuming the observation time is normalized to one second

$$\begin{aligned} i(t) &= \lambda(t)q = \frac{\eta q}{h\nu} P_{rcvd}(t) \\ &= \mathfrak{R}P_{rcvd}(t) \end{aligned}$$

⇒ Where we have defined the detector responsivity as

$$\mathfrak{R} = \frac{\eta q}{h\nu}$$