Lecture 2: Photodetection and Photodetectors



Photodetection (Continued)

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Electrical Signal-to-Noise Ratio (SNR)

► At the receiver, there is noise on the signal arriving at the input and and after detection added to that is noise that is injected at various stages of the receiver

- The current output of the receiver $i_n(t)$ has current contributions from
 - Electrical shot noise
 - Thermal noise
 - ➡ APD detectors have additional multiplication noise



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Modeling Detector SNR

⇒ When observing the detector current output, it is difficult to tell which noise was present at the optical input and which noise was generated internal to the detector. So we tend to use several different models and combine them



Noise Current

- ⇒ To quantify the statistical nature of noise, we can't determine random events ahead of time, but we can use their "spectral" characteristics to quantify statistical behavior
 - ⇒ Define an Average (mean) value to quantify the amount of power (energy) in the nontime varying part of the signal
 - ⇒ Define a Variance to quantify the amount of power (energy) in the noisy part of the signal
- \Rightarrow Define the "noise" current as

$$i(t) = I_{DC} + i_{noise}(t)$$

Shot Noise Mean and Variance

- \Rightarrow For constant power illumination, the rate parameter is constant, and the signal is the mean
- \Rightarrow The noise corresponds to the photocurrent variance
- \Rightarrow For a filter, homogeneous Poisson process

Mean (Amps)

$$i_{s}(t) = \overline{i(t)} = \frac{\eta q}{hv} P_{recvd} \int_{0}^{t} h_{d}(\tau) d\tau$$
• Both mean and variance are linear with P_{revd}
• As P_{revd} is increased, both signal and noise increase
Power Spectrum

$$i_{n}^{2}(0) = 2qI_{DC}$$
Total Shot Noise =

$$i_{n}^{2}(0) = 2qI_{DC}$$
• Both mean and variance are linear with P_{revd}
• As P_{revd} is increased, both signal and noise increase

Photodetector Shot Noise

- ⇒ The shot noise generated in the photodetection process is physically due to the "quantum granularity" of the received (and photo converted) optical signal
- \Rightarrow Shot noise sets the ultimate limit of an optical receiver
- ⇒ Shot noise is a Poisson noise, but it is usually approximated as a Gaussian noise
- \Rightarrow Hallmark of shot noise is dependence on q, the electron charge



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Shot Noise with Data Modulation

- \Rightarrow Consider how the picture changes when we have information modulated on the optical carrier
- \Rightarrow Let m(t) be the information transmitted
 - \Rightarrow Then P_{revd} (t) and λ (t) are functions of m(t)
 - Assuming the photodetector filter impulse function can change in amplitude from time period to time period, let G_i be a time varying parameter

$$i(t) = \sum_{j=1}^{N} G_j h_d(t - \tau_j)$$



Ideal Direct Detection (1)



Ideal Direct Detection (2)

Electrical SNR is found using the ratio between the signal power (DC) generated in the load resistor and the noise power (shot noise) generated in the load resistor

$$SNR_{dd} = \frac{P_{signal}}{P_{noise}} = \frac{i_{signal}^2 R_L}{i_{noise}^2 R_L} = \frac{\left(\frac{\eta q}{hv} P_{signal}\right)^2}{2qhv P_{signal}B} = \frac{1}{2} \frac{\eta P_{signal}}{hv B}$$

- ⇒ This equation shows the fundamental, *quantum shot noise limit*, where the SNR is limited only by the shot noise itself -> *Shot Noise Limited Direct (Incoherent) Detection*
- \Rightarrow SNR improves linearly with input signal strength
- \Rightarrow We will discuss other noise contributions that exist that make it difficult to reach this limit

Ideal Coherent Detection (1)

⇒ Consider the following ideal Heterodyne Coherent Receiver

 \Rightarrow Heterodyne implies that a non-zero intermediate frequency ($\omega_{\rm IF}$) is generated prior to data recovery



$$i(t) = \frac{\eta q}{h\nu} 2\sqrt{P_{lo}P_{rcvd}\varepsilon(1-\varepsilon)} \cos\left[\omega_{IF}t + \phi\right]$$

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Ideal Coherent Detection (2)

 \Rightarrow Using the same approach as in direct detection to obtain the SNR

$$SNR_{het} = \frac{P_{signal}}{P_{noise}} = \frac{i_{signal}^2 R_L}{i_{noise}^2 R_L} = \frac{\left(i_{rms}\right)^2}{2qI_{DC}BR_L} = \frac{\left(\frac{i_{peak}}{\sqrt{2}}\right)^2}{2qI_{DC}BR_L}$$
$$= \frac{\left(\frac{\eta q}{hv} 2\sqrt{P_{lo}P_{rcvd}}\varepsilon(1-\varepsilon)}{\sqrt{2}}\right)^2}{2q\left(\frac{\eta q}{hv}P_{lo}\varepsilon\right)BR_L} = \frac{\eta(1-\varepsilon)P_{rcvd}}{hvB}; \frac{\eta P_{rcvd}}{hvB}\Big|_{limit P_{lo} \to \infty, \varepsilon \to 0}$$

⇒ Note that *shot noise limited heterodyne coherent detection*, in the limit where the local oscillator is much stronger than the received signal,

 \Rightarrow Is a factor of 2 (3dB) better than the *shot noise limited incoherent detection*

Ideal Coherent Detection (3)

⇒ The other coherent approach is *Homodyne Coherent Detection*

⇒ The intermediate frequency (ω_{IF}) is driven to zero (ω_{IF} =0) at phase is driven to ϕ =0 bringing the data immediately to baseband



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$$i(t) = \frac{\eta q}{hv} 2\sqrt{P_{lo}P_{rcvd}\varepsilon(1-\varepsilon)}$$
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Ideal Coherent Detection (4)

 \Rightarrow Using the same approach as in direct detection to obtain the SNR

$$SNR_{het} = \frac{P_{signal}}{P_{noise}} = \frac{i_{signal}^2 R_L}{i_{noise}^2 R_L} = \frac{(i_{rms})^2}{2qI_{DC}B}$$
$$= \frac{\left(\frac{\eta q}{hv} 2\sqrt{P_{lo}P_{rcvd}\varepsilon(1-\varepsilon)}\right)^2}{2q\left(\frac{\eta q}{hv}P_{lo}\varepsilon\right)B} = \frac{\eta 2(1-\varepsilon)P_{rcvd}}{hvB}; 2\frac{\eta P_{rcvd}}{hvB}\Big|_{\lim t P_{lo} \to \infty, \varepsilon \to 0}$$

- ⇒ Note that *shot noise limited homodyne coherent detection*, in the limit where the local oscillator is much stronger than the received signal,
 - ⇒ Is a factor of 2 (3dB) better than the *shot noise limited heterodyne receiver* and factor of 4 (6dB) better than the *shot noise limited incoherent detection*



Photodetectors

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Photoconductors (1)

 \Rightarrow Photon absorption in semiconductor materials.

⇒ Three main absorption mechanisms: Intrinsic (band-to-band), Free-Carrier Absorption and Band-and-Impurity Absorption

⇒ Intrinsic (band-to-band) is the dominant effect in most SC photoconductors



•Incident photon $E_{photon} = hv = E_c - E_v$

Photoconductors (2)

 \Rightarrow For intrinsic absorption, photons can be absorbed if

$$\begin{split} \lambda(\mu m) &> \frac{hc}{E_c - E_V} = \frac{1.24}{E_g(eV)} \\ \lambda(nm) &> \frac{1240}{E_g(eV)} \end{split}$$

Material	Bandgap (eV)	Maximum λ (nm)	Typical Operating Range (nm)
Si	1.12	1110	500-900
Ge	0.67	1850	900-1300
GaAs	1.43	870	750-850
In _x Ga _{1-x} As _y P _{1-y}	0.38-2.25	550-3260	1000-1600

Photoconductors (3)



 \Rightarrow Power absorbed by the semiconductor is

$$P_{abs}(x) = P_i(1 - R)(1 - e^{-\alpha(\lambda)x})$$
$$= \eta(\lambda, x)P_i$$

 \Rightarrow defining the efficiency

 $\eta(\lambda, x) = \frac{\text{number of photocarriers produced}}{\text{number of incident photons}}$ $= (1 - R)(1 - e^{-\alpha(\lambda)x})$ $0 \le \eta(\lambda, x) \le 1$



- \Rightarrow P_i = incident optical power
- \Rightarrow R(λ) power reflectivity from input
- medium to semiconductor
- $\Rightarrow \alpha(\lambda) = 1/e$ absorption length

 \Rightarrow 1/ $\alpha(\lambda)$ = penetration depth



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Photoconductive Photodetectors (1)

⇒ Photogenerated current will have time and wavelength dependence

$$i_{photo}(t) = \frac{\eta q}{h\nu} GP_{rcvd}(t) + i_{dark}$$

 $\tau_{carrier}$ = mean free carrier lifetime

 $\tau_{transit}$ = transit time between eletrical contacts

$$G = \left(\frac{\tau_{carrier}}{\tau_{transit}}\right) = \text{ photoconductive gain}$$

$$i_{dark}$$
 = dark current

The transit time for electrons and holes can be different and in many SCs the eletron mobility is greater than that of the hole

$$v_e = \mu_e E > \mu_h E = v_h$$

⇒ The SC must remain charge neutral, for every electron generated, multiple holes will get pulled in until the photogenerated electron reaches the other contact. The carrier and transit times are limited by the slower carrier and the photoconductive gain is given by the ratio of the transit times

$$\tau_{carrier} = \frac{L_a}{\upsilon_h}$$
$$\tau_{transit} = \frac{L_a}{\upsilon_e}$$

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Photoconductive Photodetectors (2)

- ⇒ The carrier velocity is a linear function of electric field strength up to a saturation velocity (which is the same for both electrons and holes)
 - \Rightarrow Field strength of about 10⁵ V/cm result in velocities in range of 6x10⁶ to 10⁷ cm/s
 - \Rightarrow Some materials have an electron drift velocity that peaks at 2x10⁷ cm/s at 10⁴ V/cm
- \Rightarrow When photoconductive gain is desirable, detector is operated at low voltages
- ⇒ Carrier lifetime also impacts the frequency response of the photoconductive photodetector

$$i_{photo}(\omega) = \Re G \frac{P_{rcvd}(\omega)}{\sqrt{1 + \left(\frac{\omega}{\omega_c}\right)^2}}$$
$$\omega_c = \frac{1}{\tau_{carrier}} = \text{cutoff frequency}$$