

## ECE137B Final Exam

There are 5 problems on this exam and you have 3 hours  
 There are pages 1-19 in the exam: please make sure all are there.

Do not open this exam until told to do so

Show all work:

Credit will not be given for correct answers if supporting work is not shown.

Class Crib sheets and 2 pages (front and back → 4 surfaces) of your own notes permitted.

Don't panic.

| Time function                               | LaPlace Transform   |
|---|---|
| $\delta(t)$                                 | 1   |
| $U(t)$                                      | $1/s$   |
| $e^{-\alpha t} \cdot U(t)$                  | $\frac{1}{s + \alpha}$ or $\frac{1/\alpha}{1 + s/\alpha}$ |
| $e^{-\alpha t} \cos(\omega_d t) \cdot U(t)$ | $\frac{s + \alpha}{(s + \alpha)^2 + \omega_d^2}$          |
| $e^{-\alpha t} \sin(\omega_d t) \cdot U(t)$ | $\frac{\omega_d}{(s + \alpha)^2 + \omega_d^2}$            |

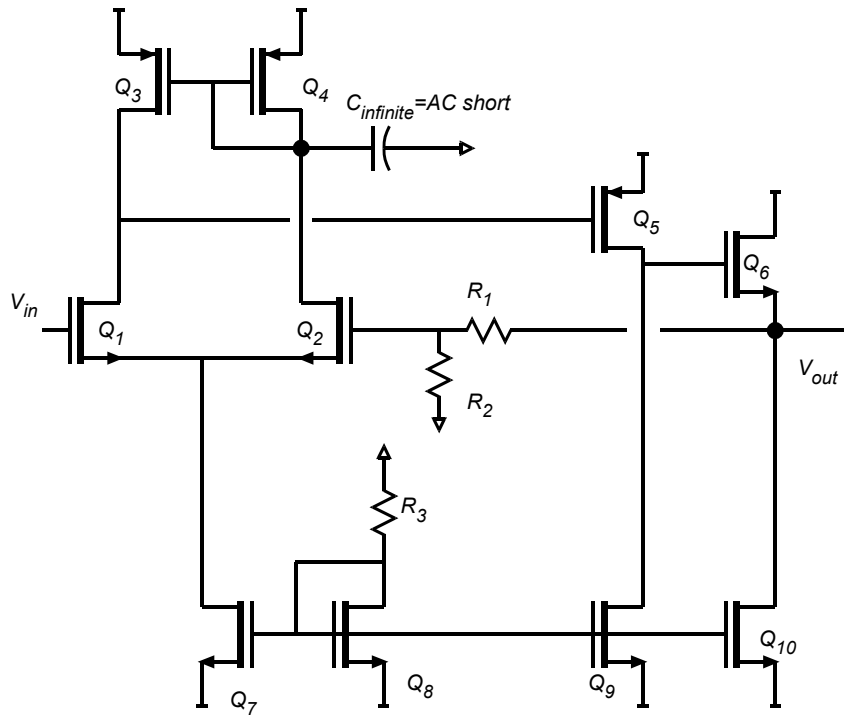
Name: \_\_\_\_\_

| Problem | points | possible | Problem | points | possible |
|---------|--------|----------|---------|--------|----------|
| 1a      |        | 3        | 2       |        | 10       |
| 1b      |        | 8        | 3a      |        | 7        |
| 1c      |        | 5        | 3b      |        | 13       |
| 1d      |        | 12       | 4a      |        | 10       |
| 1e      |        | 7        | 4b      |        | 5        |
| 1f      |        | 5        | 5a      |        | 5        |
|         |        |          | 5b      |        | 5        |
|         |        |          | 5c      |        | 5        |

**Problem 1, 40 points**

method of first-order and second-order time constants, some feedback theory

The circuit below is an op-amp



Part a, 3 points

DC analysis

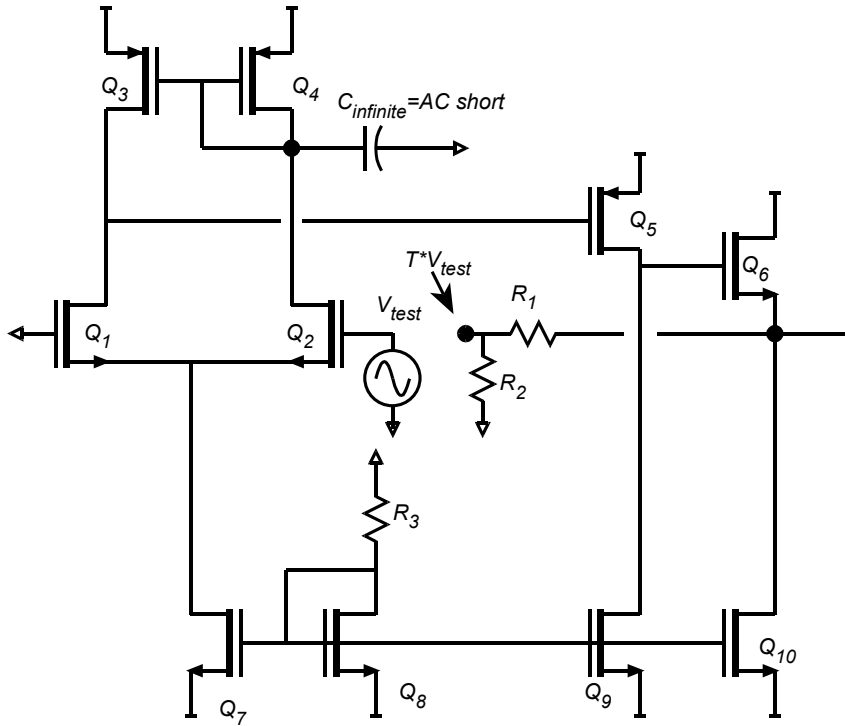
Find all transistor DC emitter currents, find all node voltages. Make these on the circuit diagram.

|   |  |
|---|--|
| $\lambda = 1/50$ V for Q3 and Q9.   | $\lambda = 0$ for all other transistors  |
| $ V_{th}  = 0.3$ V for all transistors, $g_m = 2$ mS for all transistors. |  |
| Q5 : $C_{gs} = 5$ fF, $C_{gd} = 0.5$ fF.                                  | Q6 : $C_{gs} = 0$ fF, $C_{gd} = 0.5$ fF. |
| All other transistors: $C_{gs} = C_{gd} = 0$ fF.                          |  |
| The DC component of $V_{in}$ is zero volts                                |  |
| The supplies are +/- 2 Volts.   |  |
| Pick R3 so that the DC drain current of Q8 is 0.5 mA                      |  |
| R1=1 MegOhm R2=100 kOhm   |  |

Part b. 8 points  
*mid-band analysis*

Find the low-frequency loop transmission:  
 $T(f=0 \text{ Hz}) = \underline{\hspace{2cm}}$

To do this, you need to cut the feedback loop, thus, to find the loop transmission









Part c, 5 points  
*feedback theory*

At low frequencies, what is the closed-loop gain  $V_{out}/V_{in}$  ?

***Treat  $C_{infinite}$  as an AC short (not a capacitor) in the MOTC analysis.***

$V_{out}/V_{in} =$  \_\_\_\_\_

Part d, 12 points

*motc*

Using MOTC, you will find the frequency, in Hz (not rad/sec), of the **two** major poles in the transfer function.

| capacitor 1: Cgs of Q5 | capacitor 2: Cgd of Q5 | capacitor 3: Cgd of Q6 |
|------------------------|------------------------|------------------------|
| $R_{11}^0 =$           | $R_{22}^0 =$           | $R_{33}^0 =$           |
| $R_{22}^1 =$           | $R_{33}^1 =$           | $R_{33}^2 =$           |
| $f_{p1} =$             | $f_{p2} =$             |                        |

***Remember to treat  $C_{infinite}$  as an AC short (not a capacitor) in the MOTC analysis.***



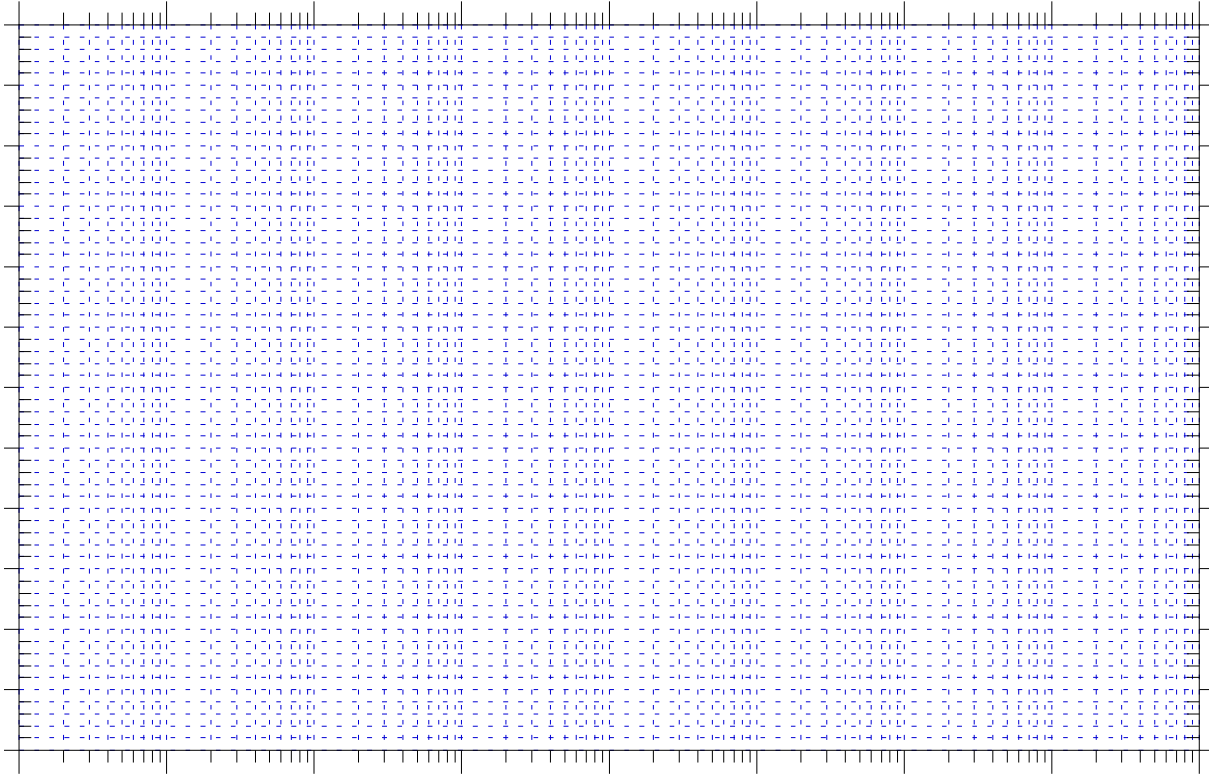


Part e, 7 points

Make accurate asymptotic plots of  $T$ . Find the phase margin and the loop bandwidth.

Phase margin = \_\_\_\_\_ Loop bandwidth = \_\_\_\_\_

**Draw the magnitude of  $T$  on this plot**



Frequency, Hz

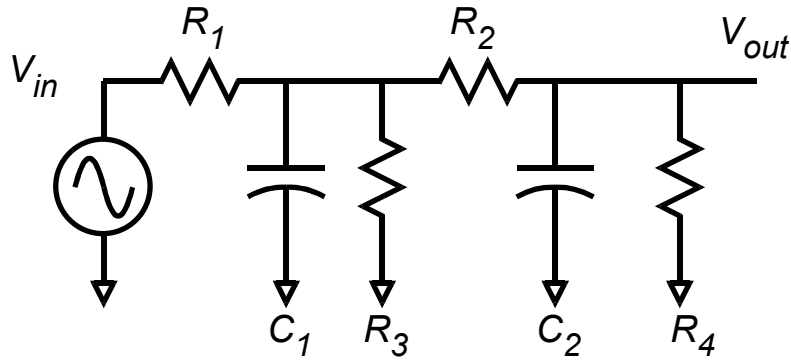
Part f, 5 points

What is the gain and bandwidth of the closed-loop amplifier ?

low frequency  $V_{out}/V_{gen} =$  \_\_\_\_\_ bandwidth of  $V_{out}/V_{gen} =$  \_\_\_\_\_

**Problem 2: 10 points**

*method of time constants analysis*



$R_1=1 \text{ KOhm}$ ,  $R_2=2\text{kOhm}$ ,  $R_3=3\text{kOhm}$ ,  $R_4=4 \text{ kOhm}$ ,  $C_1= 1 \text{ fF}$   $C_2=2 \text{ fF}$

Using MOTC, find the coefficients  $a_1$  and  $a_2$  of transfer function  $V_{out}(s)/V_{gen}(s)$ , given a

transfer function in the standard form  $\frac{V_{out}(s)}{V_{gen}(s)} = \frac{V_{out}}{V_{gen}} \Big|_{DC} \frac{1 + b_1s + b_2s^2 + \dots}{1 + a_1s + a_2s^2 + \dots}$

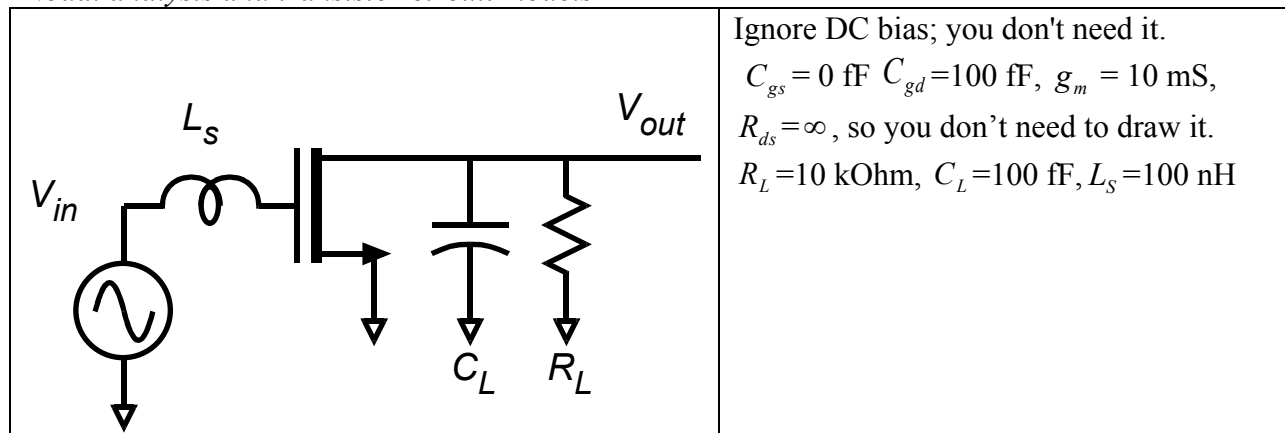
$R_{11}^0 =$  \_\_\_\_\_       $R_{22}^0 =$  \_\_\_\_\_       $R_{22}^1 =$  \_\_\_\_\_  
 $\frac{V_{out}}{V_{gen}} \Big|_{DC} =$  \_\_\_\_\_       $a_1 =$  \_\_\_\_\_       $a_2 =$  \_\_\_\_\_





**Problem 3: 20 points**

*Nodal analysis and transistor circuit models*



Part a, 7 points

Draw an accurate small-signal equivalent circuit model of the circuit above.

Part b, 13 points

**Using NODAL ANALYSIS**, find the transfer function  $V_{out}(s)/V_{in}(s)$

The answer must be in standard form  $\frac{V_{out}(s)}{V_{in}(s)} = \frac{V_{out}}{V_{in}} \Big|_{midband} \times \frac{1 + b_1s + b_2s^2 + \dots}{1 + a_1s + a_2s^2 + \dots}$ ,

$V_{out}(s)/V_{in}(s) =$  \_\_\_\_\_

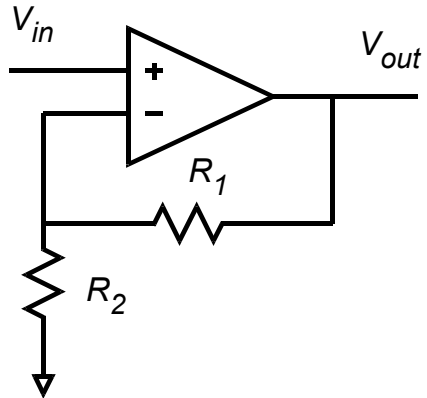




**Problem 4, 15 points**

*negative feedback*

part a, 10 points



The amplifier has a differential gain of  $10^5$ .  
 $R_1=99 \text{ k}\Omega$ ,  $R_2=1 \text{ k}\Omega$ . The op-amp has infinite differential input impedance and zero differential output impedance.

The differential amplifier has 2 poles in its open-loop transfer function.

One, the dominant pole, is at a low frequency, and can be adjusted by appropriately adjusting a compensation capacitor internal to the op-amp. The second one is at 500 MHz

To repeat:

$f_{p1}$  = dominant pole frequency= you must find the required value

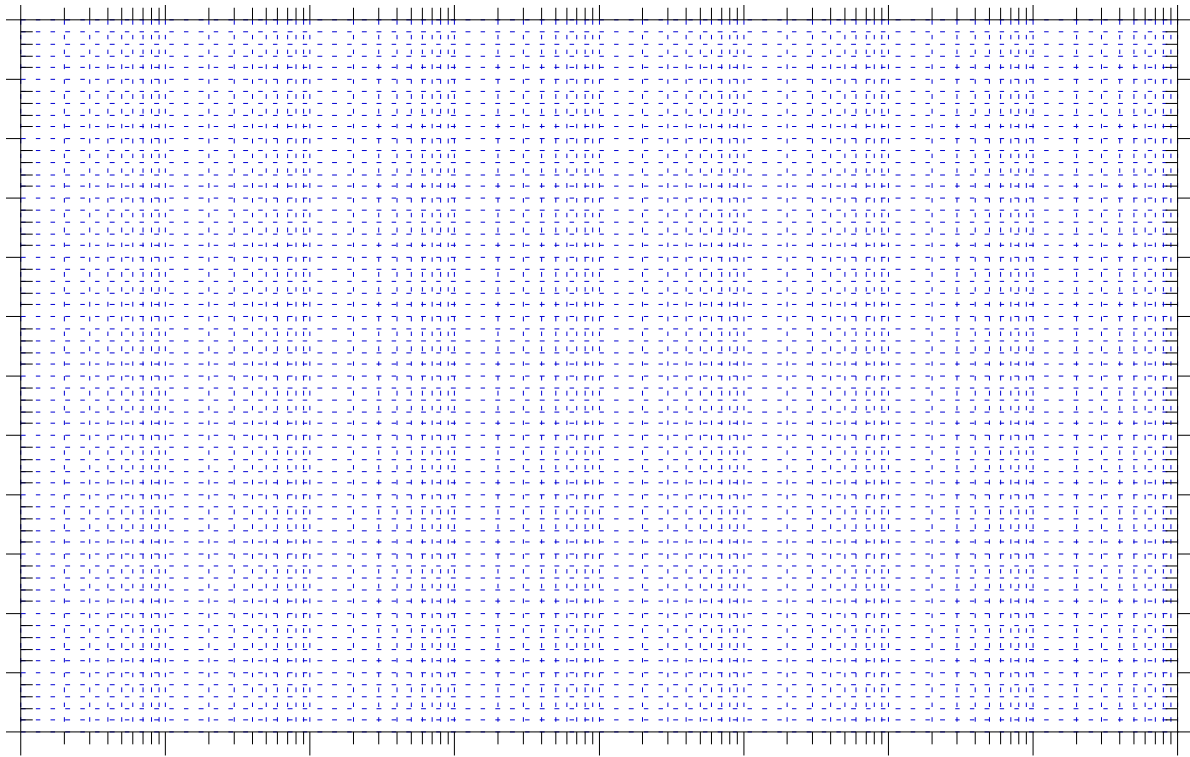
$f_{p2}$  = second pole frequency= 500 MHz

**PICK  $f_{p1}$  so that the phase margin is 168.7 degrees.**

Using the Bode plot on the next page, plot the open-loop gain ( $A_d$  or  $A_{ol}$ ), the inverse of the feedback factor ( $1/\beta$ ), closed loop gain ( $A_{CL}$ ). **Label all axes, slopes, pole/zero frequencies, etc.** Determine the following:

$f_{p1}$  = \_\_\_\_\_ Loop bandwidth= \_\_\_\_\_

$V_{out}/V_{in}$  at DC= \_\_\_\_\_



Frequency, Hz

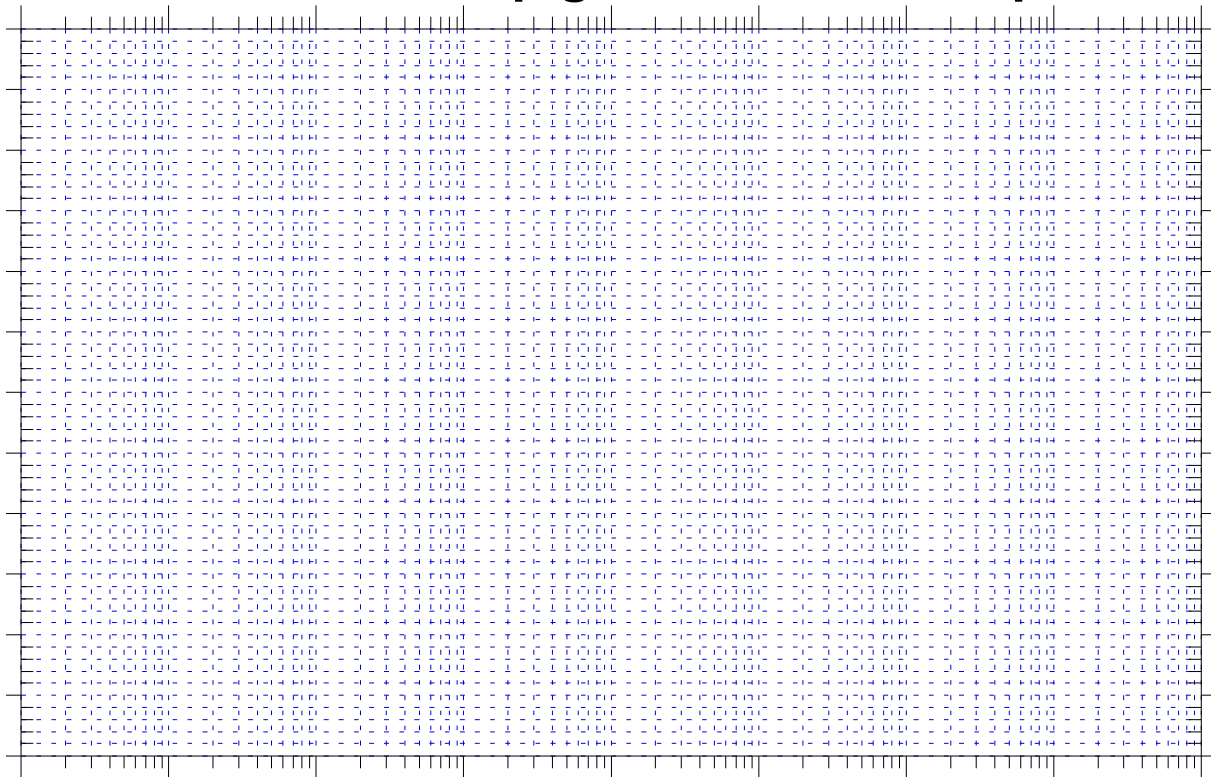
part b, 5 points

What is the gain and bandwidth of the closed-loop amplifier ?

low frequency  $V_{out}/V_{gen} = \underline{\hspace{2cm}}$  bandwidth of  $V_{out}/V_{gen} = \underline{\hspace{2cm}}$

*Draw a plot of the closed loop gain, labeling all axes, slopes, pole/zero frequencies, etc.*

**draw closed loop gain on this bode plot**

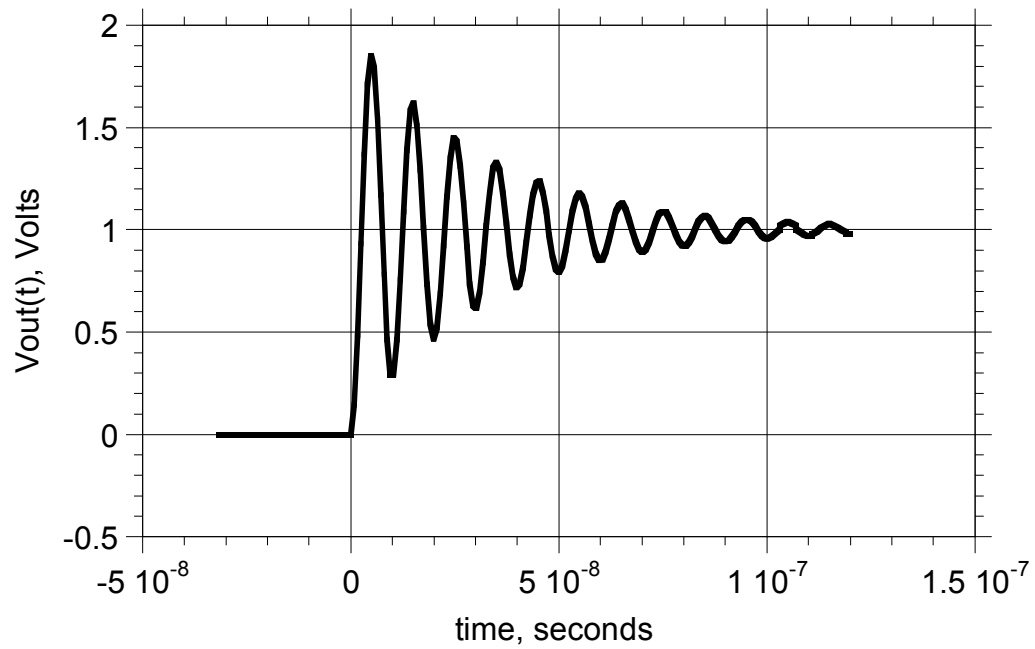


Frequency, Hz

**Problem 5: 15 points**  
*transfer functions*

Part a, 5 points

A transistor circuit has a step response (input is a 1-V step function) as shown.



Determine the frequency and damping factor of the dominant poles of the transfer function.

Part b, 5 points

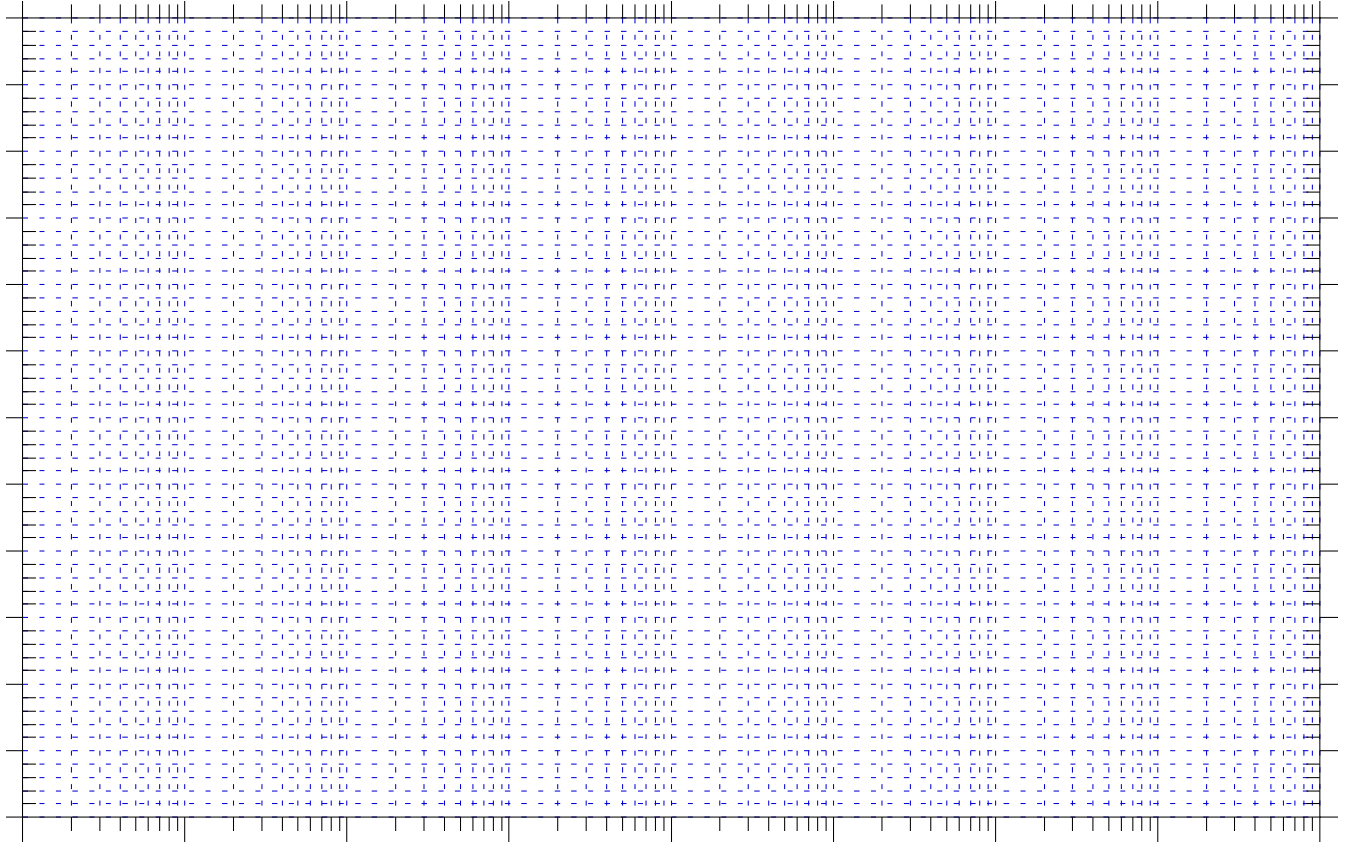
Give the transfer function

Vout(s)/Vgen(s). Give the answer in standard form  $\frac{V_{out}(s)}{V_{gen}(s)} = \frac{V_{out}}{V_{gen}} \Big|_{DC} \frac{1 + b_1s + b_2s^2 + \dots}{1 + a_1s + a_2s^2 + \dots}$

Vout(s)/Vgen(s)= \_\_\_\_\_

Part c, 5 points

Draw an *accurate* Bode plot of the transfer function. LABEL AXES precisely



Frequency, Hz