

## ECE137B Final Exam

There are 6 problems on this exam and you have 3 hours

***Do not open this exam until told to do so***

***Show all work:***

***Credit will not be given for correct answers if supporting work is not shown.***

***Class Crib sheets and 4 pages of your own notes permitted.***

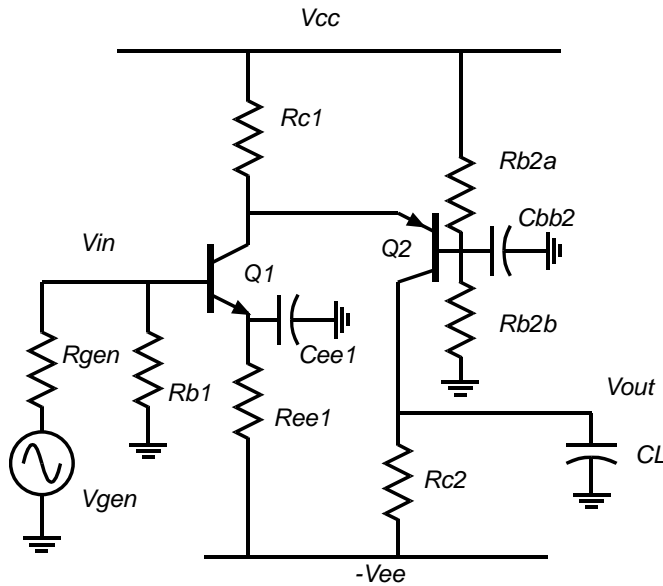
***Don't panic.***

Time function	LaPlace Transform
$\delta(t)$	1
$U(t)$	$1/s$
$e^{-\alpha t}U(t)$	$\frac{1}{s + \alpha}$
$e^{-\alpha t} \cos(\omega_d t)U(t)$	$\frac{s + \alpha}{(s + \alpha)^2 + \omega_d^2}$
$e^{-\alpha t} \sin(\omega_d t)U(t)$	$\frac{\omega_d}{(s + \alpha)^2 + \omega_d^2}$

Name: \_\_\_\_\_

**Problem 1, 20 points**  
*transistor circuit analysis*

part a, 5 points



In the circuit, the power supplies are +/- 10 volts. The transistors have  $\beta=1000$ ,  $f_t=1$  GHz, and  $C_{cb}=0.5$  pF.  $C_L=1$  pF.  $V_a=\infty$ .

$C_{ee1}$  and  $C_{bb2}$  are very large (AC short-circuits)

$R_{gen}=1$  kOhm,  $R_{b1}=10$  kOhm

$R_{b2a}$  and  $R_{b2b}$  are chosen to bias the base of Q2 at +4.3 volts.

Q1 and Q2 are each biased at 1 mA emitter current.

$R_{c2}$  is chosen to set the DC output voltage to zero volts.

Find  $R_{ee1}$ ,  $R_{c1}$ ,  $R_{c2}$

$R_{ee1}=\underline{\hspace{2cm}}$   $R_{c1}=\underline{\hspace{2cm}}$   $R_{c2}=\underline{\hspace{2cm}}$

Part b, 5 points

Find the mid-band value of  $V_{out}/V_{gen}$ .

$V_{out}/V_{gen} = \underline{\hspace{10em}}$



Part c, 10 points

Find  $C_{pi}$  of transistors Q1 and Q2. Give the frequency, in Hz (not rad/sec), of the 3 major poles in the transfer function.

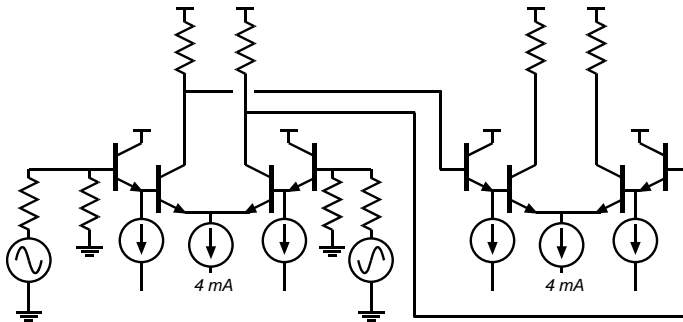
$C_{pi1} =$  \_\_\_\_\_  $C_{pi2} =$  \_\_\_\_\_

$f_{p1} =$  \_\_\_\_\_  $f_{p2} =$  \_\_\_\_\_  $f_{p3} =$  \_\_\_\_\_

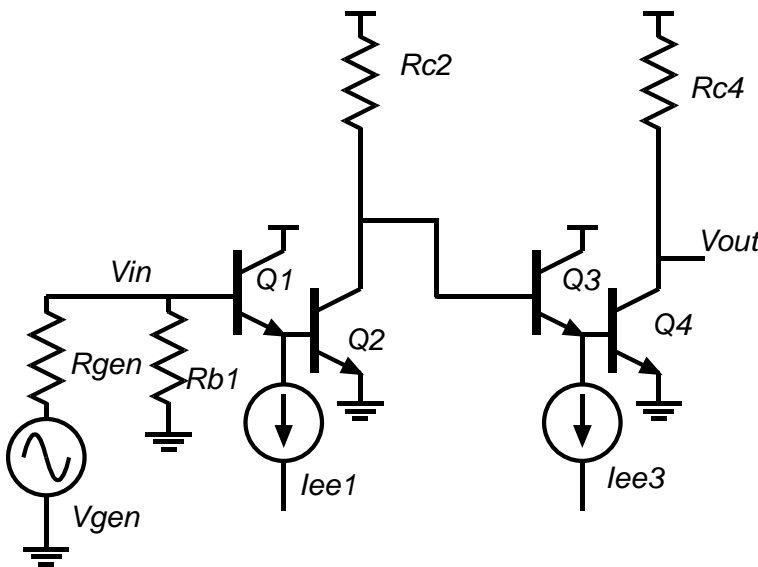


**Problem 2, 20 points**

*method of first-order time constants*



A basic differential video amplifier is shown on the left. This circuit is fully differential, and so can be analyzed by the half-circuit method, where the connected emitters of the differential pairs become virtual grounds.



*The circuit we therefore analyze is to the left. This is an AC equivalent circuit: It does not represent the DC.*

All transistors have  $f_t=500$  MHz and  $C_{cb}=1$  pF.  
Beta=infinity,  $V_a=infinity$

$R_{gen}=R_{b1}=50$  Ohms.

Q1 and Q3 are each biased at 1 mA. Q2 and Q4 are each biased at 2 mA.

$R_{c2}$  and  $R_{c4}$  are 100 Ohms

Part a, 5 points

Find  $C_{pi}$  of Q1-Q4.

$C_{pi1} = \underline{\hspace{2cm}}$        $C_{pi2} = \underline{\hspace{2cm}}$   
 $C_{pi3} = \underline{\hspace{2cm}}$        $C_{pi4} = \underline{\hspace{2cm}}$

Part b, 15 points

Using the method of time constants, find the dominant time constant  $a_1$  of the transfer function  $V_{out}(s)/V_{gen}(s)$ . Give the components of  $a_1$  due to each transistor capacitance.

$a_1 =$  \_\_\_\_\_ seconds

component of  $a_1$  due to Ccb1= \_\_\_\_\_ seconds

component of  $a_1$  due to Ccb2= \_\_\_\_\_ seconds

component of  $a_1$  due to Ccb3= \_\_\_\_\_ seconds

component of  $a_1$  due to Ccb4= \_\_\_\_\_ seconds

component of  $a_1$  due to Cpi1= \_\_\_\_\_ seconds

component of  $a_1$  due to Cpi2= \_\_\_\_\_ seconds

component of  $a_1$  due to Cpi3= \_\_\_\_\_ seconds

component of  $a_1$  due to Cpi4= \_\_\_\_\_ seconds



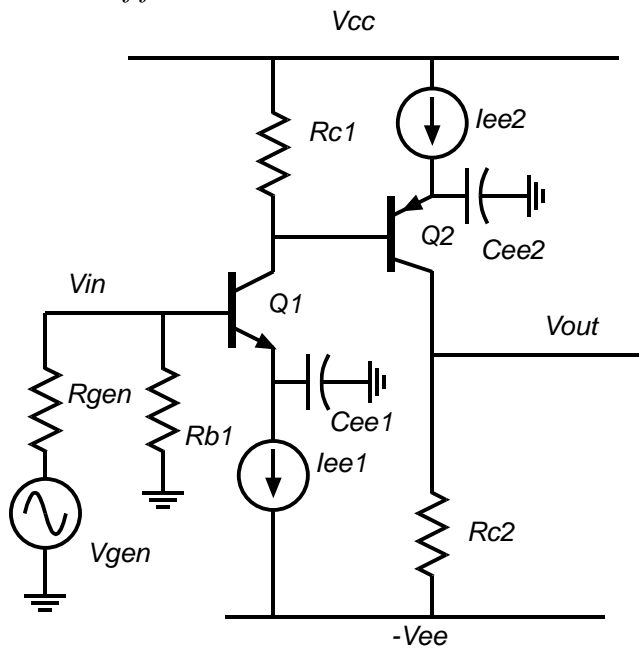






**Problem 3, 20 points**

*method of first-order and second-order time constants*



Q1 has  $C_{be}=10\text{ pF}$ ,  $C_{cb}=1\text{ pF}$ .  
Beta=infinity,  $V_a=\text{infinity}$ .

Q2 has  $C_{be}=0\text{ pF}$ ,  $C_{cb}=1\text{ pF}$ .  
Beta=infinity,  $V_a=\text{infinity}$ .

$C_{ee1}$  and  $C_{ee2}$  are very large (AC short-circuits)

The supplies ( $V_{cc}$  and  $-V_{ee}$ ) are  $\pm 10$  volts.

$I_{ee1}=1\text{ mA}$ .  $I_{ee2}=2\text{ mA}$ .

$R_{gen}=R_{b1}=50\text{ Ohms}$ .

$R_{c1}=100\text{ Ohms}$ .  $R_{c2}=400\text{ Ohms}$ .

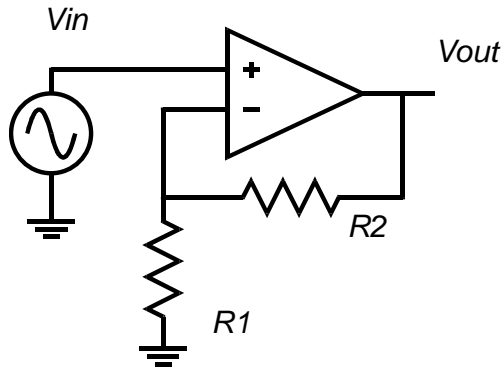
Use the method of time constants to find the frequencies of the first two poles of the transfer function  $V_{out}(s)/V_{gen}(s)$ .





**Problem 4 10 points**

*negative feedback*



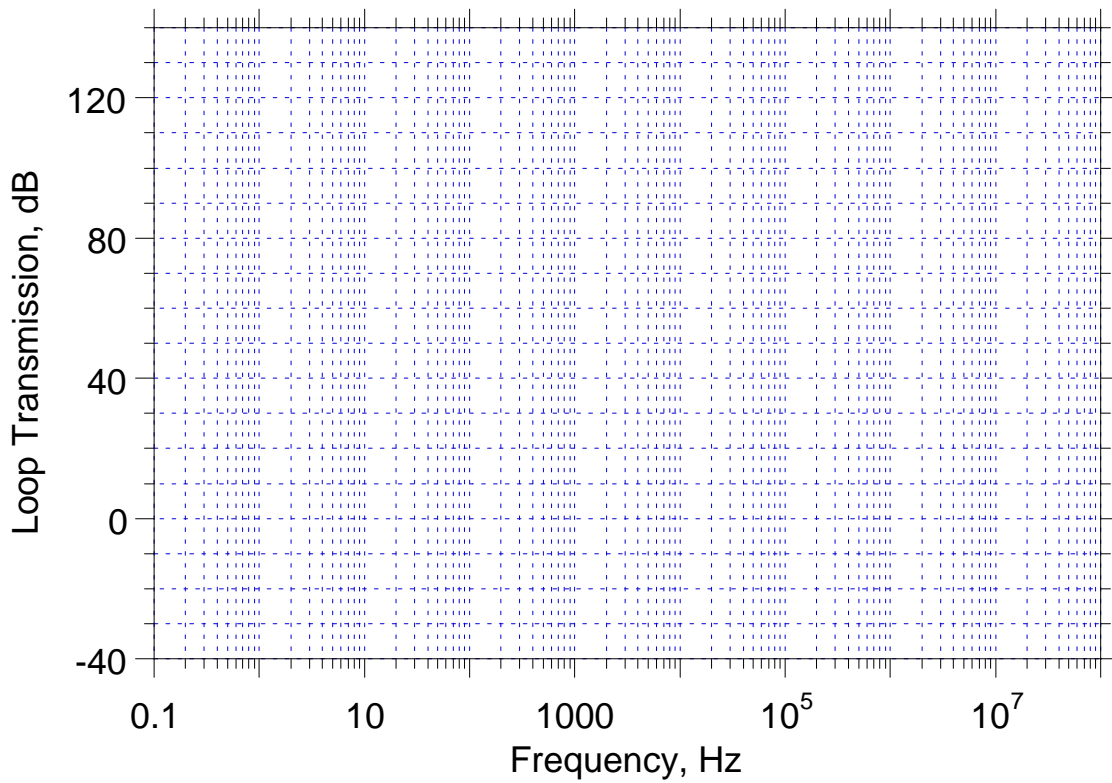
The amplifier has a differential gain of  $10^7$ .  $R1=1\text{ k}\Omega$ ,  $R2=19\text{ k}\Omega$ . The op-amp has infinite differential input impedance and zero differential output impedance.

The differential amplifier has poles in its open-loop transfer function at 20 Hz and 100 kHz. .

Using the Bode plot below, determine the following

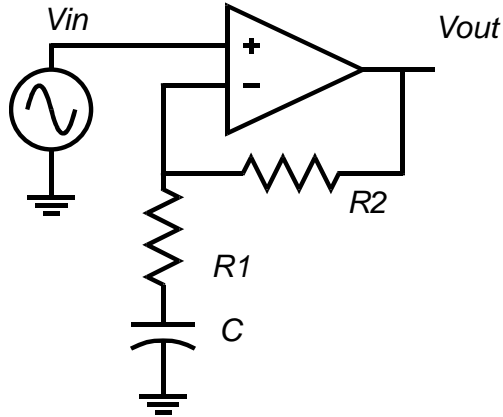
Loop bandwidth=\_\_\_\_\_ phase margin=\_\_\_\_\_

$V_{out}/V_{gen}$  at DC=\_\_\_\_\_



**Problem 5 15 points**

*negative feedback, again*



The differential amplifier has infinite differential input impedance and zero output impedance. Its low-frequency gain is  $10^6$ , and it has a single pole in its transfer function at 2 Hz.

$R_1=100$  Ohms.  $R_2=9.9$  kOhm.

$C=1.59$  microfarads.

Part a, 5 points

Find the feedback factor  $\beta(s)$ , using standard form  $\beta(s) = \beta_{dc} \frac{1 + b_1s + b_2s^2 + \dots}{1 + a_1s + a_2s^2 + \dots}$

$\beta(s) =$  \_\_\_\_\_

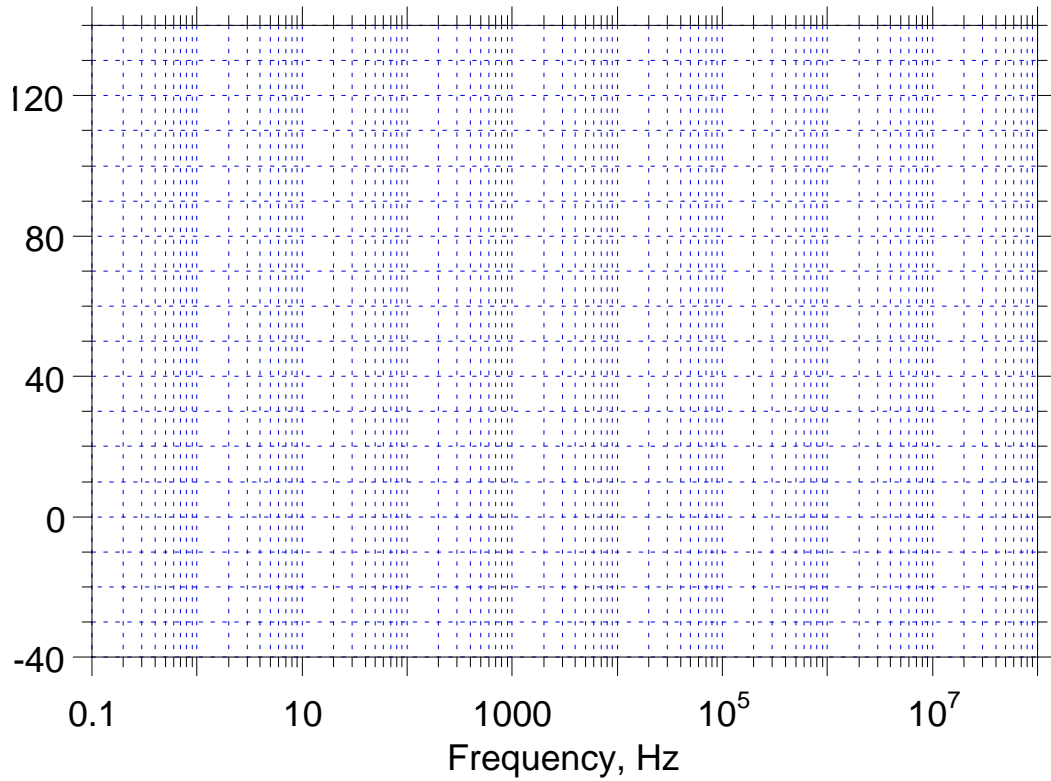


Part b, 10 points

Use the Bode plot below to plot the **closed loop transfer function**  $A_{CL}$ , the differential gain  $A_d$ , and the inverse of the feedback factor  $1/\beta$ . List all the poles and zero frequencies of  $A_{CL}$ .

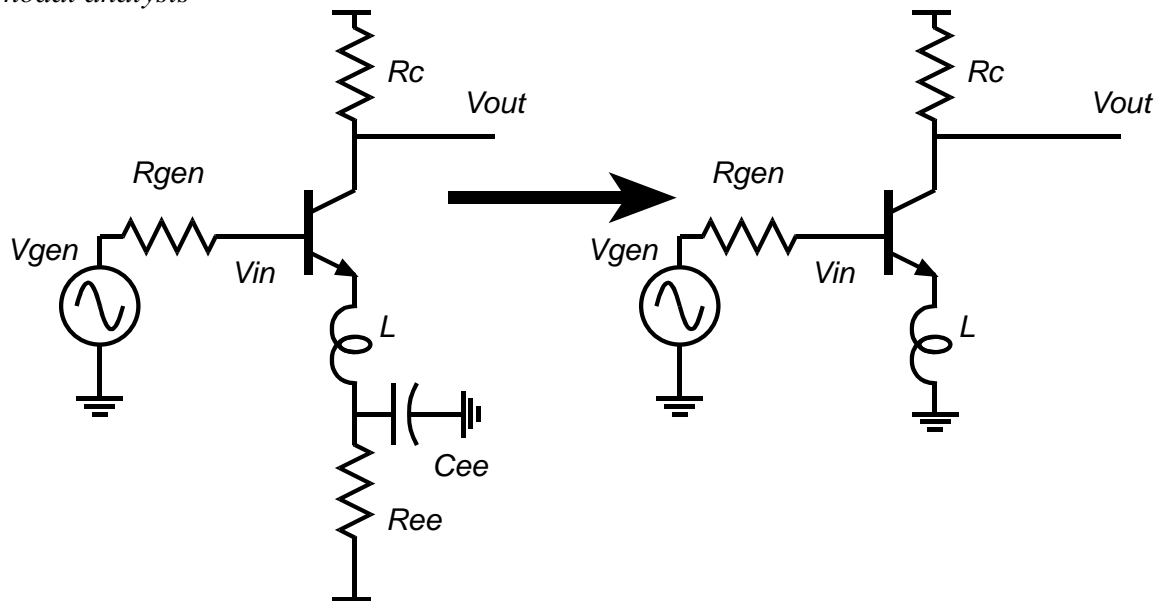
Poles in  $A_{CL}$  at frequencies \_\_\_\_\_ Hz

Zeros in  $A_{CL}$  at frequencies \_\_\_\_\_ Hz



**Problem 6 15 points**

*nodal analysis*



Inductance, often present in the emitter lead of a common-emitter amplifier, can have a serious effect on high frequency response. Working from the small-signal equivalent ***circuit on the right***, with  $R_{gen} = \text{zero}$  Ohms,  $R_c = 100$  Ohms,  $L = 1$  nH,  $r_e = 26$  Ohms,  $C_{be} = 1$  pF,  $C_{cb} = \mathbf{0pF}$ ,  $\beta = \text{infinity}$ ,  $V_a = \text{infinity}$ , find  $V_{out}/V_{gen}$  by nodal analysis. Give

the answer in standard form  $\frac{V_{out}(s)}{V_{gen}(s)} = \frac{V_{out}}{V_{gen}} \bigg|_{DC} \frac{1 + b_1s + b_2s^2 + \dots}{1 + a_1s + a_2s^2 + \dots}$

$V_{out}(s)/V_{gen}(s) = \underline{\hspace{10cm}}$



