

## ECE137B Final Exam

There are 5 problems on this exam and you have 3 hours  
There are pages 1-19 in the exam: please make sure all are there.

Do not open this exam until told to do so

Show all work:

Credit will not be given for correct answers if supporting work is not shown.

Class Crib sheets and 4 pages of your own notes permitted.

Don't panic.

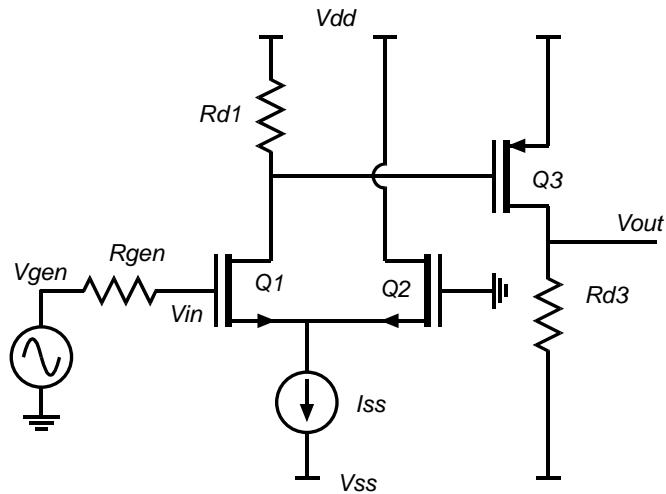
Time function	LaPlace Transform
$\delta(t)$	1
$U(t)$	$1/s$
$e^{-\alpha t} \cdot U(t)$	$\frac{1}{s + \alpha}$ or $\frac{1/\alpha}{1 + s/\alpha}$
$e^{-\alpha t} \cos(\omega_d t) \cdot U(t)$	$\frac{s + \alpha}{(s + \alpha)^2 + \omega_d^2}$
$e^{-\alpha t} \sin(\omega_d t) \cdot U(t)$	$\frac{\omega_d}{(s + \alpha)^2 + \omega_d^2}$

Name: \_\_\_\_\_

Problem	points	possible	Problem	points	possible
1a			3a		
1b			3b		
1c			4		
1d			5a		
2a			5b		
2b					

### Problem 1, 25 points

method of first-order and second-order time constants



Q1, Q2, and Q3 have  $v_{sat}c_{ox}W_g = 10 \text{ mS}$ ,  $|V_t| = 0.5 \text{ volts}$ , and  $\lambda = 0 \text{ V}^{-1}$ .

Vdd and Vss are  $\pm 3.3 \text{ Volts}$ .

Rgen=50 kOhm and Iss=2 mA.

Q1 has

$$C_{gs} = 10C_{gd} = 15.9 \text{ fF}$$

Q2 has

$$C_{gs} = 10C_{gd} = 15.9 \text{ fF}$$

Q3 has

$$C_{gs} = 0, C_{gd} = 31.8 \text{ fF}$$

#### Part 1, 4 points

Q1 and Q2 are to be biased at 1 mA drain current, Q3 is to be biased at 2mA drain current and Vout is to be at zero volts DC.

Find Rd1 and Rd3

Rd1=\_\_\_\_\_ Rd3=\_\_\_\_\_

**Part b, 5 points**

Find the mid-band value of  $V_{out}/V_{gen}$ .

$V_{out}/V_{gen} = \underline{\hspace{2cm}}$



Part c, 4 points

Find the  $f_\tau$  of transistors Q1 and Q3.

Q1:  $f_\tau$  = \_\_\_\_\_ Q3:  $f_\tau$  = \_\_\_\_\_

Part d, 12 points

Using MOTC, you will find the frequency, in Hz (not rad/sec), of the *two* major poles in the transfer function. The degeneration approximation may help.

capacitor 1: Cgs of transistor 1 (possibly the degenerated Cgs)	capacitor 2: Cgd of transistor 1	capacitor 3: Cgd of transistor 3
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$$R_{11}^0 = \underline{\hspace{10em}} \quad R_{22}^0 = \underline{\hspace{10em}} \quad R_{33}^0 = \underline{\hspace{10em}}$$

$$R_{22}^1 = \underline{\hspace{10em}} \quad R_{33}^1 = \underline{\hspace{10em}} \quad R_{33}^2 = \underline{\hspace{10em}}$$

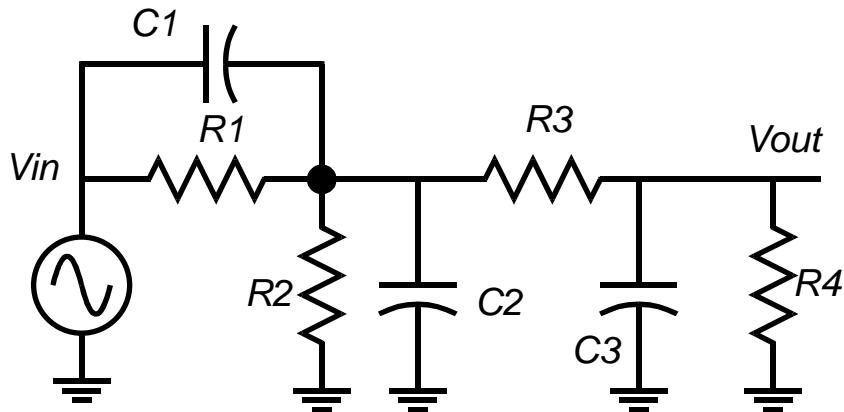
$$\bar{f}_{p1} = \underline{\hspace{10em}} \quad f_{p2} = \underline{\hspace{10em}}$$

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**Problem 2: 20 points**

*method of time constants analysis*



R1=1 KOhm R2=2 KOhm R3=3 KOhm R4=4 KOhm

C1= 1 nF      C2=2nF    C3=3 nF

Part a, 15 points

Using MOTC, find the transfer function  $V_{out}(s)/V_{gen}(s)$ . Give the answer in standard

$$\text{form } \frac{V_{out}(s)}{V_{gen}(s)} = \left. \frac{V_{out}}{V_{gen}} \right|_{DC} \frac{1 + b_1 s + b_2 s^2 + \dots}{1 + a_1 s + a_2 s^2 + \dots}$$

**HINT:**  $b_1 = R_1 C_1$  and  $0 = b_2 = b_3 = \dots$

$$R_{11}^0 = \underline{\hspace{10em}}$$

$$R_{22}^0 = \underline{\hspace{10em}}$$

$$R_{33}^0 = \underline{\hspace{10em}}$$

$$R_{22}^1 = \underline{\hspace{10em}}$$

$$R_{33}^1 = \underline{\hspace{10em}}$$

$$R_{33}^2 = \underline{\hspace{10em}}$$

$$\left. \frac{V_{out}}{V_{gen}} \right|_{DC} = \underline{\hspace{10em}}$$

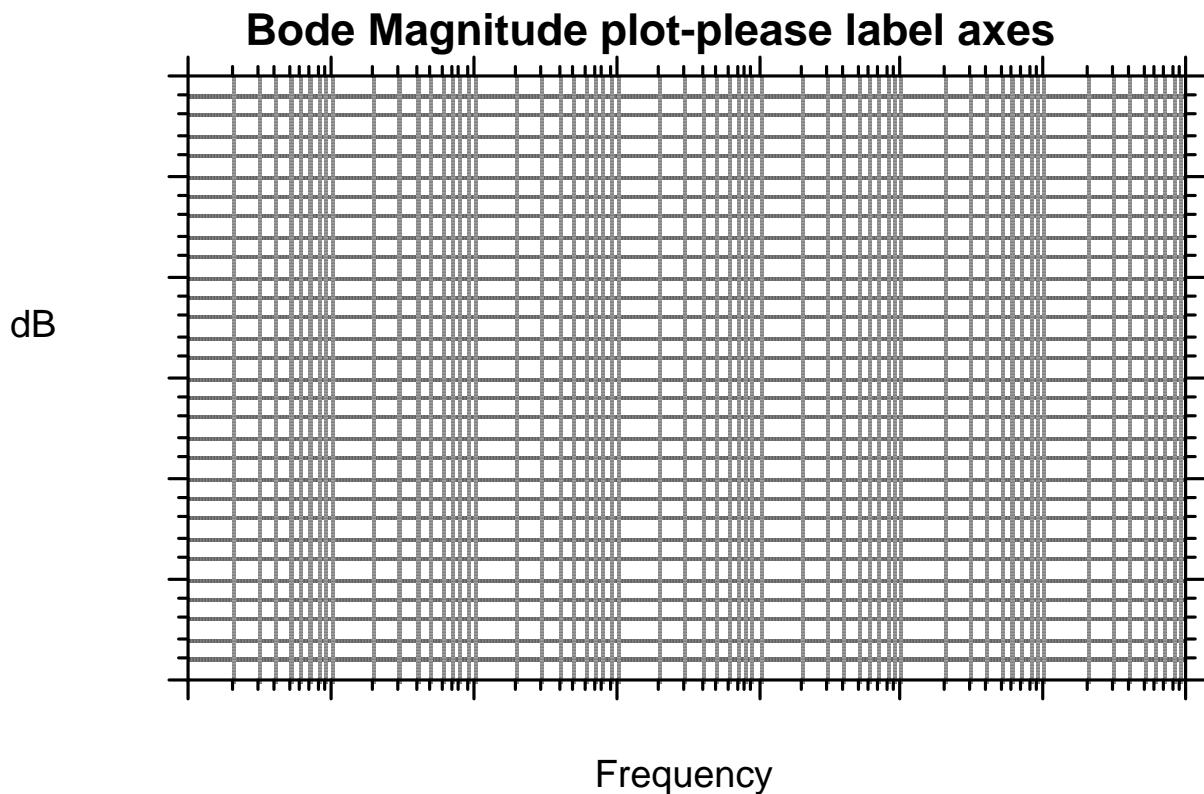
$$a_1 = \underline{\hspace{10em}}$$

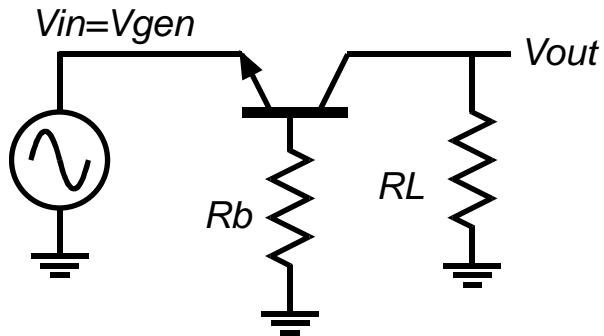
$$a_2 = \underline{\hspace{10em}}$$



Part b, 5 points

Draw a Bode Plot (Straight-line asymptotes) of the circuit transfer function  $V_{out}/V_{gen}$ , labeling all pole and zero frequencies and labeling the slopes of all asymptotes.



**Problem 3 20 points***Nodal analysis and transistor circuit models*

Above is the AC small signal representation of transistor circuit.

$R_b = 2000$  Ohms.  $R_L = 10,000$  Ohms. The transistor is biased at 2 mA DC emitter current, so that  $r_e = 13$  Ohms.

$\tau_f = 0$  ps,  $C_{be,dep} = 0$  fF,  $C_{cb} = 20$  fF.  $\beta = \infty$ ,  $V_A = \infty$  volts.

**Part a, 7 points**

Draw an accurate small-signal equivalent circuit model of the circuit above, with the transistor represented by the common-base T model

Part b, 13 points

**Using NODAL ANALYSIS,** find the transfer function  $V_{out}(s)/V_{gen}(s)$ .

The answer must be in standard form  $\frac{V_{out}(s)}{V_{gen}(s)} = \frac{V_{out}}{V_{gen}} \Big|_{DC} \frac{1+b_1s+b_2s^2+\dots}{1+a_1s+a_2s^2+\dots}$

**HINT:** Think carefully; how many nodal equations are really needed here

$$\frac{V_{out}}{V_{gen}} \Big|_{DC} = \text{_____}, \quad a_1 = \text{_____}, \quad a_2 = \text{_____}$$

$$b_1 = \text{_____}, \quad b_2 = \text{_____}$$

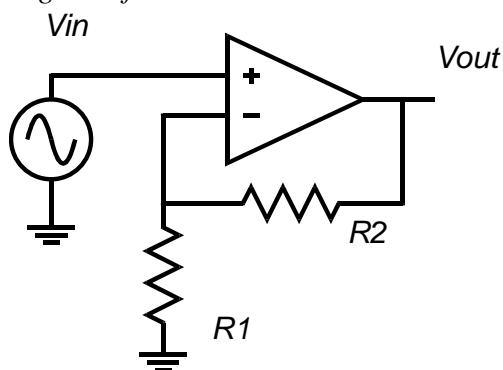
(note that  $a_3, a_4, \dots, b_3, b_4, \dots$  are all zero)





**Problem 4, 20 points**

negative feedback



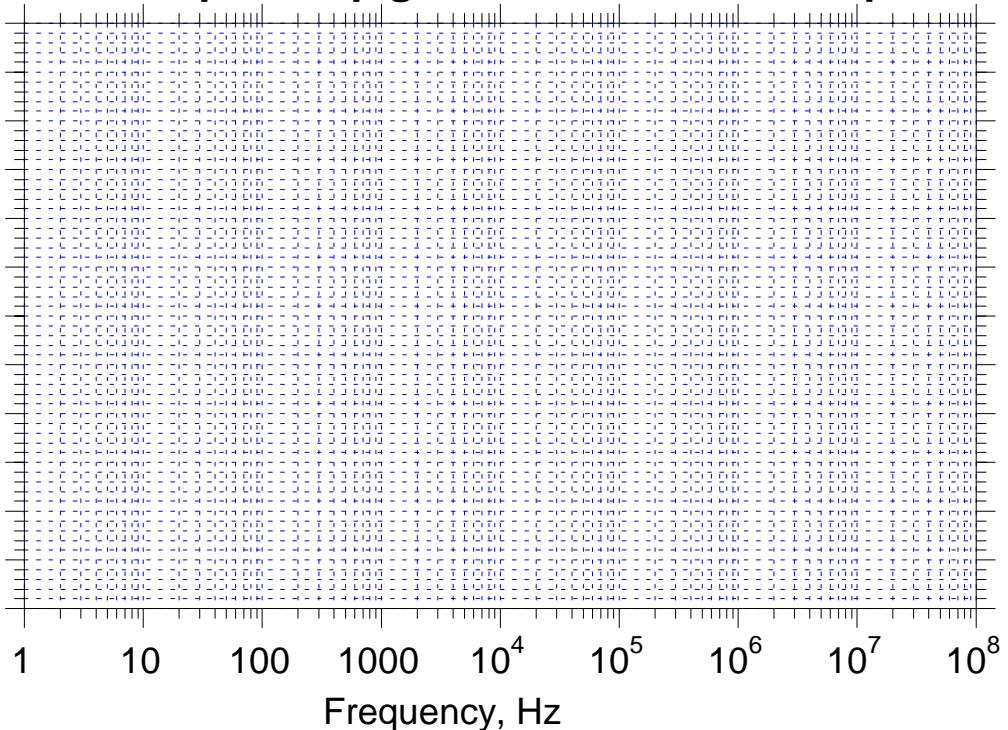
The amplifier has a differential gain of  $2 \cdot 10^7$ .  $R_1=1\text{ kOhm}$ ,  $R_2=19\text{ kOhm}$ . The op-amp has infinite differential input impedance and zero differential output impedance.

The differential amplifier has 2 poles in its open-loop transfer function at 1 kHz, and one pole at 10 MHz. It has a single zero in its transfer function at 10 MHz.

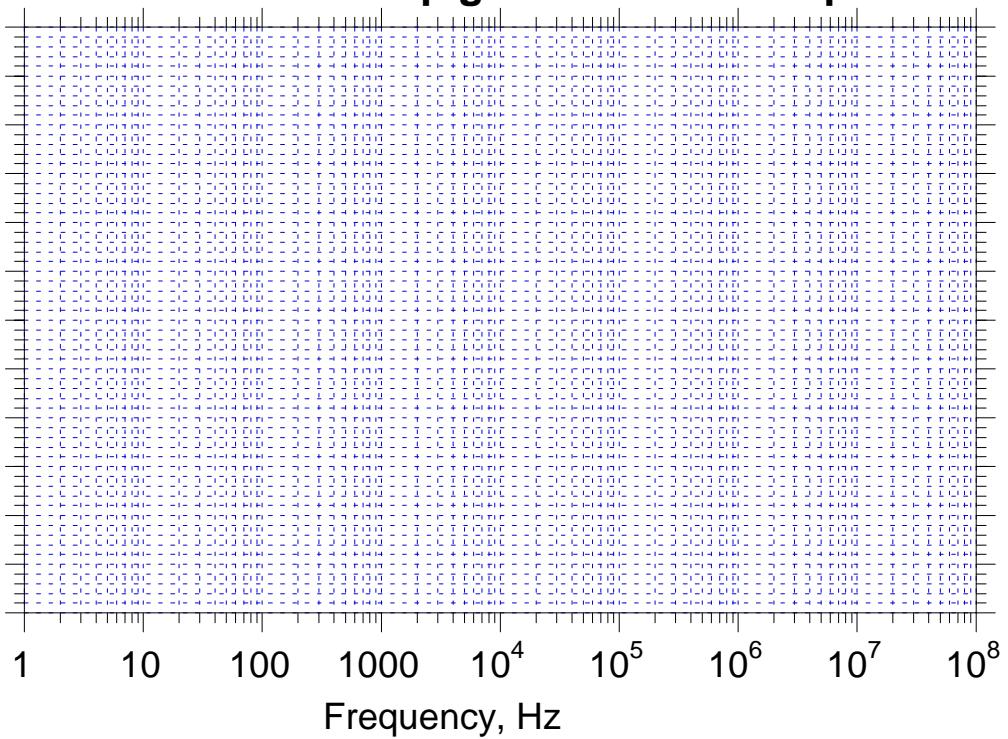
Using the Bode plot on the next page, plot the open-loop gain ( $A_d$  or  $A_{ol}$ ), the inverse of the feedback factor ( $1/\beta$ ), closed loop gain ( $A_{CL}$ ), and determine the following:

Loop bandwidth=\_\_\_\_\_ phase margin=\_\_\_\_\_  
 Vout/Vgen at DC=\_\_\_\_\_

**Draw open loop gain and 1/beta on this plot**



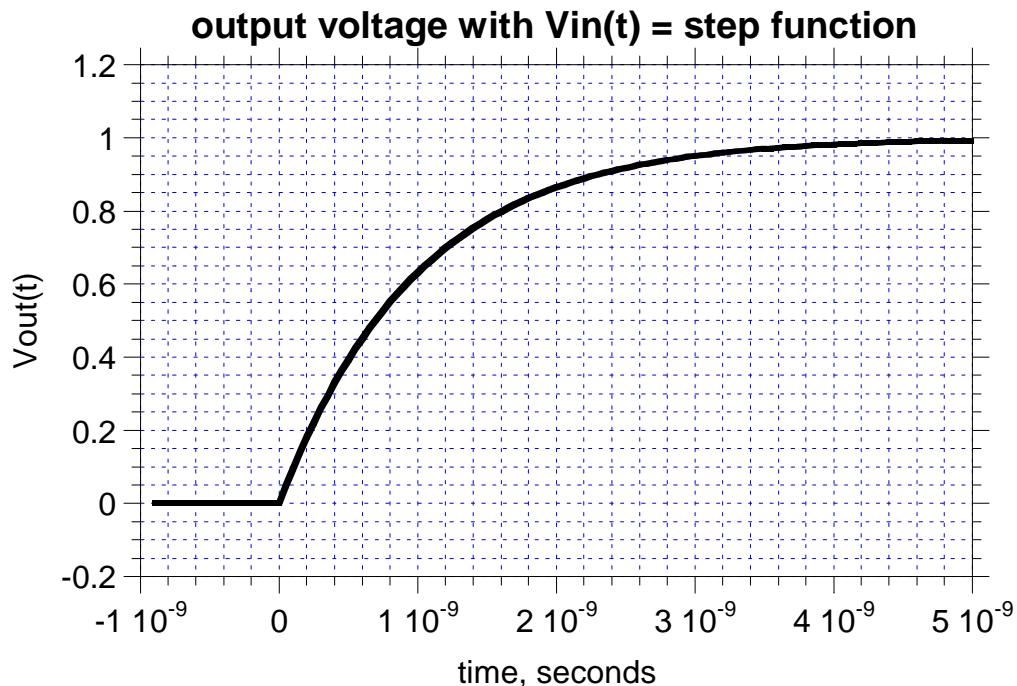
**draw closed loop gain on this bode plot**



**Problem 5: 15 points**  
*transfer functions*

Part a, 5 points

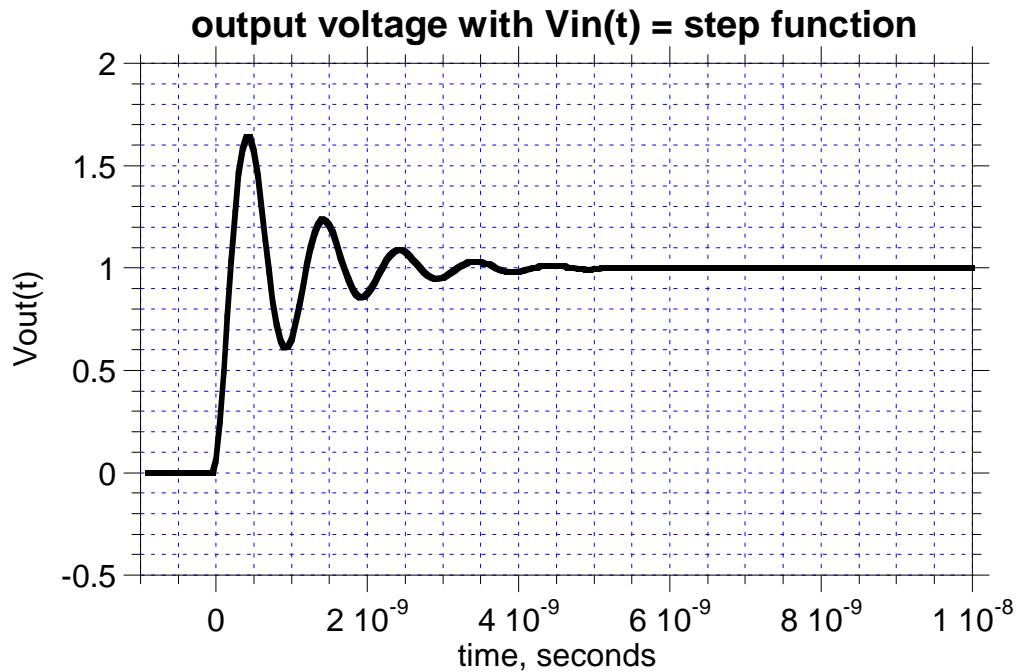
A transistor circuit has a step response (input is a 1-V step function) as shown.



What is the circuits' 3-dB bandwidth ?  $f_{3dB} = \underline{\hspace{10cm}}$

Part b, 10 points

Another transistor circuit has a step response (input is a 1-V step function) as shown.



This is clearly a second-order response.

Approximately what is the damped resonant frequency ?  $f_n = \underline{\hspace{2cm}}$

Estimate the damping factor ?  $\zeta = \underline{\hspace{2cm}}$  (35% accuracy is fine here)

Sketch the transfer function below, labeling both axes, key slopes, and key frequencies.

### Bode Magnitude plot-please label axes

