# Switching circuits: basics and switching speed 

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## Amplifiers vs. switching circuits

Some transistor circuit might have $V_{\text {in }}$ vs. $V_{\text {out }}$ characteristics like this:


The characteristics have a nearly linear amplification region:

## Trivial example: CS stage with resistive load





Here, the lower limit on $V_{\text {out }}$ is set by saturation, and the upper limit by cutoff

## Amplifiers vs. switching circuits

Biased in the linear region, and with a sufficiently small input, the circuit is an *amplifier*


But, if the input is large, then the output switches between the clipping values. This is a *switching circuit*


## Switching circuits vs. logic gates

Logic gates are a particular *type* of switching circuit

A general switching cicuit might have a different range for $V_{\text {out }}$ and $V_{\text {in }}$. ...and might not perform *logic*


## Switching circuits vs. logic gates

Logic gates are a particular *type* of switching circuit

A logic gate will have the same range for $V_{\text {out }}$ and $V_{\text {in }}$. ...and usually has multiple inputs to perform Boolean operations


CMOS NAND gate:


## Switching circuits vs. logic gates

Our focus here is on switching circuits, and on calculating
DC $V_{\text {in }}-V_{\text {out }}$ transfer characteristics switching risetimes and falltimes

You should have, by now, studied basic logic gates in other classes

## Noise margins

"Noise" margins: tolerance for component variation, EMI

Input low level can vary over a considerable range, yet always produce nearly the same output "high" level


Input high level can vary over a considerable range, yet always produce nearly the same output "low" level

Defining margins precisely is difficult for general switching circuits. ....easier for logic

## Another switching circuit: CMOS

$$
V_{D D}=1 \mathrm{~V}
$$




$I_{D, N F E T}=I_{D, P F E T}$ and $V_{D S, P F E T}=V_{D D}-V_{D S, N F E T}$
From these relationships, we obtain the loadline constructions above
Both the positive and negative clipping limits, hence switched output voltage levels, are set by transistor saturation.

## Another switch: emitter-coupled pair



One example of this: the digital $50 \Omega$ coaxial cable interface between the PRBS pulse generator and the LED/laser driver in lab project choice \#2.

## Another switch: emitter-coupled pair



There are also logic families using bipolar differential pairs, current mode logic, left, and emitter coupled logic, right

## emitter-coupled pair transfer characteristics



The stated levels on the diagram are easily found.
But, how do we find $\Delta V_{i n}$ ?

## emitter-coupled pair transfer characteristics




DC bias $V_{\text {in }}$ at zero Volts, then apply a small signal: what is the gain?
$g_{m}=g_{m 1}=g_{m 2}=I_{o} / 2 V_{T}, A_{v}=\partial V_{\text {out }} / \partial V_{\text {in }}=g_{m} R_{L} / 2=I_{o} R_{L} / 4 V_{T}$

## emitter-coupled pair transfer characteristics



so, the slope of the switching region is $I_{o} R_{L} / 4 V_{T}$,
while the output voltage swing is $I_{o} R_{L}$,
so the input voltage range must be the ratio of these:

$$
\Delta V_{i n}=\left(I_{o} R_{L}\right) /\left(I_{o} R_{L} / 4 V_{T}\right)=4 V_{T}=4 \mathrm{kT} / q
$$

## emitter-coupled pair: comments



You can repeat this calculation for a differential input $\rightarrow$ different $\Delta V_{\text {in }}$

We have assume that $Q_{1}, Q_{2}$ don't saturate over the logic swing. if they do, then this will change the $V_{\text {in }}-V_{\text {out }}$ characteristics

## Limiting mechanisms: current-steering




We can design differential current-steering circuits such that both $V_{\text {out,high }}$ and $V_{\text {out,low }}$ are set by cutoff.

## Limiting mechanisms: CS or CE



In these common-source-like and common-emitter-like circuits either or both $V_{\text {out , high }}$ and $V_{\text {out }, \text { low }}$ are set by saturation.

## Limiting mechanisms: CS or CE



When BJT's saturate, they usually store large amounts of minority carrier change.

Switching speed is then very slow.

With a few exceptions, saturation is avoided in bipolar switching circuits

## Computing risetimes: charge control method

Charge control method: hand estimate switching circuit delay, risetime -Compute total charge on all capacitors at high $Q_{\text {high }}$ and low levels $Q_{\text {low }}$ -Compute voltage on node at high level $V_{\text {high }}$ and low level $V_{\text {low }}$ -Compute change in charge $\Delta Q=Q_{\text {high }}-Q_{\text {low }}$ and voltage $\Delta V=V_{\text {high }}-V_{\text {low }}$ -If node is charged by constant current $I$, then charging is linear

$$
T_{\text {risel fall }}=\Delta Q / I \text { and } T_{\text {delay }}=T_{\text {risel fall }} / 2
$$

-If node is charged through resistance $R$, then charging is exponential
Equivalent capacitance $C=\Delta Q / \Delta V$, time constant $\tau=R C$

$$
T_{\text {risel fall }}=2.2 \tau \text { and } T_{\text {delay }}=\tau \ln (2)
$$

## Charging through a current source



The input voltage falls suddenly, turning the FET off.
Let's ignore, just for now,
the PFET knee voltage; treat as current source.
Now, constant current charges capacitance.
Charging is linear

$$
T_{\text {risel fall }}=\Delta Q / I_{0} \text { and } T_{\text {delay }}=T_{\text {risel fall }} / 2
$$

## Charging through a resistance



The input voltage falls suddenly, turning the FET off.
Node is charged through resistance $R$; charging is exponential
Equivalent capacitance $C=\Delta Q / \Delta V$, time constant $\tau=R C$

$$
T_{\text {risel fall }}=2.2 \tau \text { and } T_{\text {delay }}=\tau \ln (2)
$$

## Example: Waveform at Q1 drain


$V_{i n}$ switches at $t=0$.


We will estimate $V_{D 1}(t)$.

## Example: Waveform at Q1 drain



Note:



1) $V_{D 1}(t)$ initially swings negative: $V_{\text {in }}(t)$ couples to $V_{D 1}(t)$ though a capacitive voltage divider between $C_{g d 1}$ and $\left(C_{g d 2}, C_{g d 3}, C_{g s 3}\right)$ 2) $V_{D 1}(t)$ then charges towards +1 V .

Between $V_{D 1}=0 \mathrm{~V}$ and $0.8 \mathrm{~V}, Q_{2}$ is a constant-current source
Between $V_{D 2}=0.8 \mathrm{~V}$ and $1 \mathrm{~V}, Q_{2}$ acts as a resistance (saturation)

## Example: Waveform at Q1 drain



Switching time between A and C : 1 st part: charging to 0.8 V change in charge in:

$$
\begin{aligned}
& C_{g d 1}: @ \mathrm{~A}: Q=-1 \mathrm{~V} \cdot C_{g d 1}, @ \mathrm{C}: Q=0.8 \mathrm{~V} \cdot C_{g d 1}, \Delta Q=1.8 \mathrm{~V} \cdot C_{g d 1} \\
& C_{g d 2}: @ \mathrm{~A}: Q=-0.8 \mathrm{~V} \cdot C_{g d 2}, @ \mathrm{C}: Q=0 \mathrm{~V} \cdot C_{g d 2}, \Delta Q=0.8 \mathrm{~V} \cdot C_{g d 2} \\
& C_{g d 3}: @ \mathrm{~A}: Q=-1 \mathrm{~V} \cdot C_{g d 3}, @ \mathrm{C} Q=0.8 \mathrm{~V} \cdot C_{g d 3}, \Delta Q=1.8 \mathrm{~V} \cdot C_{g d 3} \\
& C_{g s 3}: @ \mathrm{~A}: Q=0 \mathrm{~V} \cdot C_{g s 3}, @ \mathrm{C}: Q=0.8 \mathrm{~V} \cdot C_{g s 3}, \Delta Q=0.8 \mathrm{~V} \cdot C_{g d 3}
\end{aligned}
$$

Time for drain of Q 1 to charge to 0.8 V :

$$
T_{1}=\left(1.8 \mathrm{~V} \cdot C_{g d 1}+0.8 \mathrm{~V} \cdot C_{g d 2}+1.8 \mathrm{~V} \cdot C_{g d 3}+0.8 \mathrm{~V} \cdot C_{g d 3}\right) / 1 \mathrm{~mA}
$$

## Example: Waveform at Q1 drain




Switching time between C and $\mathrm{D}: 2$ nd part: charging from 0.8 V towards 1 V

$$
\begin{aligned}
& C_{g d 1}: @ \mathrm{C}: Q=0.8 \cdot C_{g d 1}, @ \mathrm{D}: Q=1 \mathrm{~V} \cdot C_{g d 1}, \Delta Q=0.2 \mathrm{~V} \cdot C_{g d 1} \\
& C_{g d 2}: @ \mathrm{C}: Q=0 \mathrm{~V} \cdot C_{g d 2}, @ \mathrm{D}: Q=0.2 \mathrm{~V} \cdot C_{g d 2}, \Delta Q=0.2 \mathrm{~V} \cdot C_{g d 2} \\
& C_{g d 3}: @ \mathrm{C}: Q=0.8 \mathrm{~V} \cdot C_{g d 3}, @ \mathrm{D}: Q=1 \mathrm{~V} \cdot C_{g d 3}, \Delta Q=0.2 \mathrm{~V} \cdot C_{g d 3} \\
& C_{g 33}: @ \mathrm{C}: Q=0.8 \mathrm{~V} \cdot C_{g s 3}, @ \mathrm{D}: Q=1 \mathrm{~V} \cdot C_{g s 3}, \Delta Q=0.2 \mathrm{~V} \cdot C_{g d 3}
\end{aligned}
$$

Effective capacitance :
$C_{e f f}=\left(0.2 \mathrm{~V} \cdot C_{g d 1}+0.2 \mathrm{~V} \cdot C_{g d 2}+0.2 \mathrm{~V} \cdot C_{g d 3}+0.2 \mathrm{~V} \cdot C_{g d 3}\right) / 0.2 \mathrm{~V}=\ldots$
Time constant $\tau=R_{D S, s a t} C_{e f f}=R_{D S, s a t}\left(C_{g d 1}+C_{g d 2}+C_{g d 3}+C_{g d 3}\right)$
Exponential charging: $V_{D 1}(t)=0.8 \mathrm{~V}+(1 \mathrm{~V}-0.8 \mathrm{~V})\left(1-\exp \left(\left(t-T_{1}\right) / \tau\right)\right)$

## Example: bipolar differential switch



Let us calculate the risetime at the base of Q3

## Example: bipolar differential switch



Let us calculate the risetime at the base of Q3
Times are relative to the time at which the collector current of Q2 switches to zero.


## Example: bipolar differential switch



Switching time between A and B:
change in charge in:

$$
\begin{aligned}
& C_{c b 2}: @ \mathrm{~A}: Q=V_{l o w} \cdot C_{c b 2}, \text { @ B: } Q=V_{\text {high }} \cdot C_{c b 2}, \Delta Q=\left(V_{\text {high }}-V_{l o w}\right) \cdot C_{c b 2} \\
& C_{c b 3}: @ \mathrm{~A}: Q=\left(V_{l o w}-V_{c C}\right) \cdot C_{c b 3}, @ \mathrm{~B}: Q=\left(V_{\text {high }}-V_{C C}\right) \cdot C_{c b 3}, \Delta Q=\left(V_{\text {high }}-V_{l o w}\right) \cdot C_{c b 3} \\
& C_{\text {je2 }}: @ \mathrm{~A}: Q=\left(V_{l o w}-V_{0}+\phi\right) \cdot C_{\text {je2 }}, @ \mathrm{~B}: Q=\left(V_{\text {high }}-V_{\text {high }}+\phi\right) \cdot C_{j e 2}, \Delta Q=\left(V_{0}-V_{l o w}\right) \cdot C_{\text {je2 }} \\
& C_{d i f f 2}: @ \mathrm{~A}: Q=0 \mathrm{~mA} \cdot \tau_{f 2}, @ \mathrm{~B}: Q=I_{0} \cdot \tau_{f 2}, \Delta Q=I_{0} \cdot \tau_{f 2}
\end{aligned}
$$

Effective capacitance:

$$
\begin{aligned}
C_{\text {eff }} & =\Delta Q /\left(V_{\text {high }}-V_{\text {low }}\right) \\
& =\left(\left(V_{\text {high }}-V_{\text {low }}\right) \cdot C_{c b 2}+\left(V_{\text {high }}-V_{\text {low }}\right) \cdot C_{c b 3}+\left(V_{0}-V_{\text {low }}\right) \cdot C_{\text {je2 }}+I_{0} \cdot \tau_{f 2}\right) /\left(V_{\text {high }}-V_{\text {low }}\right)
\end{aligned}
$$

## Example: bipolar differential switch



Effective capacitance:
$C_{e f f}=C_{c b 2}+C_{c b 3}+C_{j e 2} \frac{V_{0}-V_{\text {low }}}{V_{\text {high }}-V_{\text {low }}}+\frac{I_{0} \cdot \tau_{f 2}}{V_{\text {high }}-V_{\text {low }}}$ but $V_{\text {high }}-V_{\text {low }}=I_{0} R_{L}$
Charging time constant:
$\tau_{\text {charge }}=R_{L} C_{e f f}=R_{L} C_{c b 2}+R_{L} C_{c b 3}+R_{L} C_{\text {je2 }} \frac{V_{0}-V_{\text {low }}}{V_{\text {high }}-V_{\text {low }}}+\tau_{f 2}$
Voltage waveform:
$V_{b 3}(t)=V_{\text {low }}+\left(V_{\text {high }}-V_{\text {low }}\right)\left(1-\exp \left(-t / \tau_{\text {charge }}\right)\right)$

## Limitations of charge control

1) the method is very approximate
2) We do not predict the detailed shape of the switching waveform More detailed analysis can find secondary switching transients at one or move points within the overall waveform. In some cases, spikes are produced. This is more advanced material
