

**ECE ECE145B (undergrad) and ECE218B (graduate)**

**Final Exam. March 24, 2012**

Do not open exam until instructed to.

Open notes, open books, etc

You have 3 hrs.

Use all reasonable approximations (5% accuracy is fine. ), ***AFTER STATING THEM.***

***Hint: Stop and think before doing complicated calculations. For some problems, there is an easier way.***

Problem	Points Received	Points Possible
1a		5
1b		5
1c		10
1d		5
2		30
3a		10
3b		10
4a		10
4b		10
4c		10

**Name:** \_\_\_\_\_

**Problem 1, 20 points**

receiver calculations.

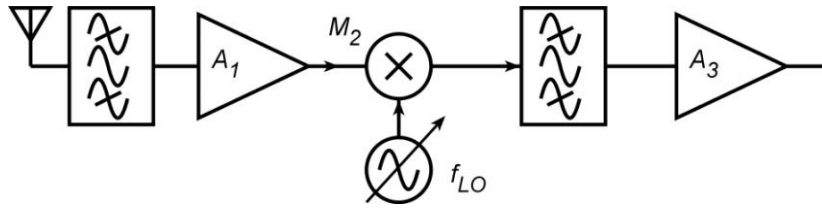
Amplifier  $A_1$  has gain  $G_1=10$  dB gain, noise figure  $F_1=1.0$  dB and input-referred third-order intercept

$IIP3_1=0$  dBm

Mixer  $M_2$  has gain  $G_2=0$  dB gain, noise figure  $F_2=3.0$  dB.

Amplifier  $A_3$  has gain  $G_3=30$  dB gain, noise figure  $F_3=3.0$  dB.

Neither  $M_2$  nor  $A_3$  produce and third-order distortion.



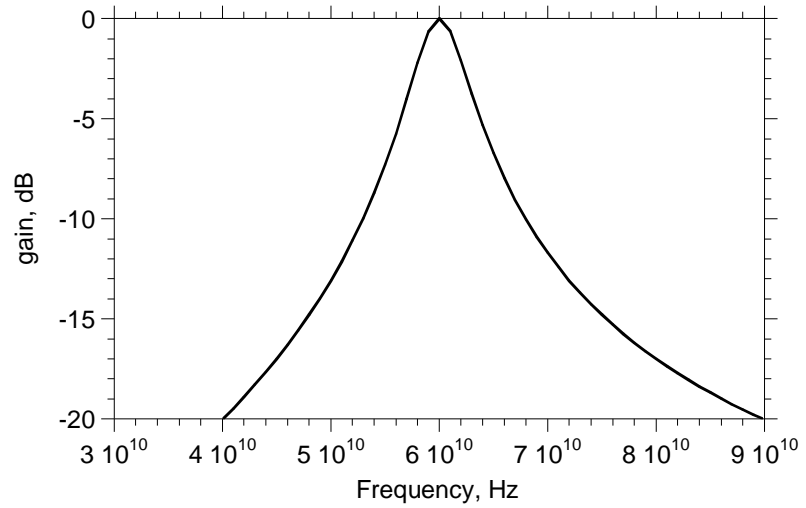
part a, 5 points

The receiver is operating with 1 Gb/s ( $10^9$  bits/sec) digital radio on a 60 GHz carrier using *uncoded* QPSK modulation. Since we have not studied this, it is stated without proof that for a digital bit error rate of  $10^{-9}$ , the signal (power)/noise(power) ratio in a 1 GHz bandwidth must be 36:1. Find the minimum received power.



part b, 5 points

The local oscillator is \*above\* the RF frequency. The IF is at 10 GHz. The attenuation-frequency characteristics of the RF pre-select filter are as shown to the right.



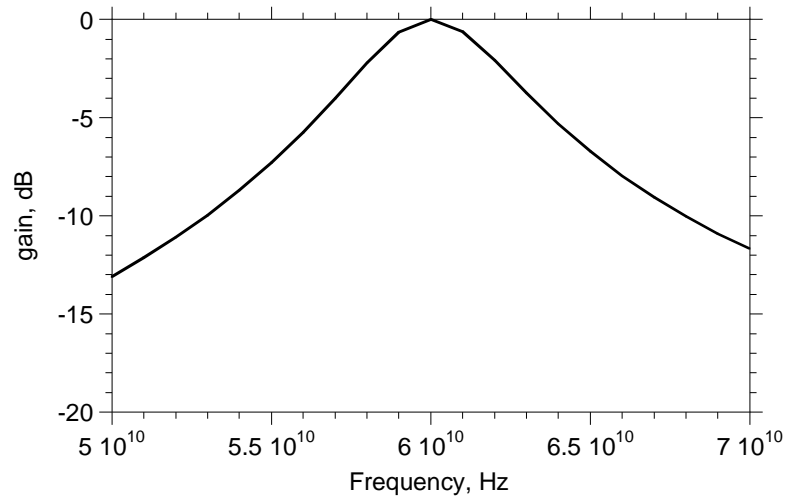
If the received signal power is -40 dBm, what interfering power at the receiver image frequency would result in a 20 dB signal/interference ratio ?



part c, 10 points

The transfer function of the RF pre-select filter is shown in more detail to the right.

Interfering signals are present, both of power -30 dBm *at the antenna* terminals, at frequencies of 50 GHz and 55 GHz.



The IF filter is a brick-wall filter of 1 GHz bandwidth centered at 10 GHz, i.e. has 0 dB gain between 9.5 and 10.5 GHz, and infinite attenuation outside this bandwidth. If we require a 20 dB signal/ interference ratio, what must the 60 GHz RF signal power be ?



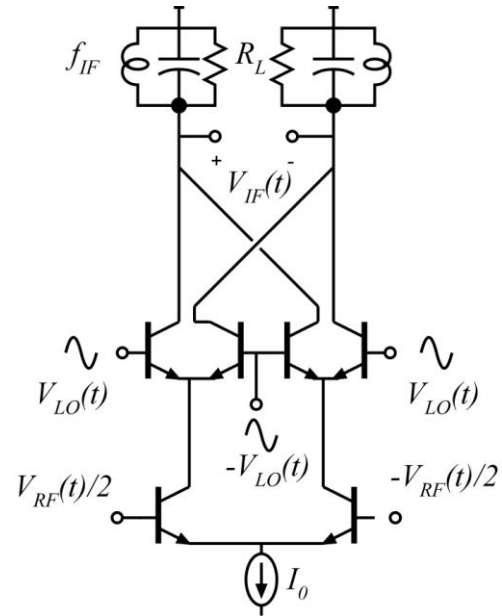
part d, 5 points

We instead use a fundamental mixer, as shown.

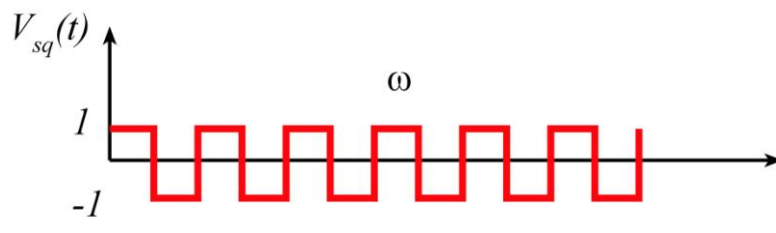
The bipolar transistors are ideal (zero parasitic resistance, infinite current gain, no capacitances),  $I_0 = 2 \text{ mA}$ ,  $R_L = 50 \text{ Ohms}$ .

The LO is large and switches the upper transistor quad completely.

In units of voltage gain, not power gain, what is the conversion gain of the mixer?



Hint: the Fourier series of a squarewave is given to the right.



$$V_{sq}(t) = \frac{4}{\pi} \left[ \cos(\omega t) + \frac{\cos(3\omega t)}{3} + \frac{\cos(5\omega t)}{5} + \dots \right]$$







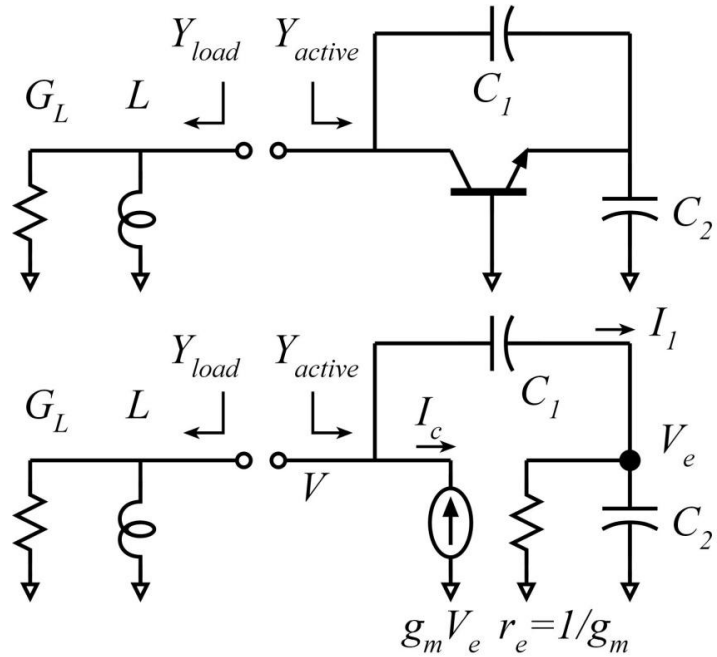
**Problem 2, 30 points**

The bipolar transistor is ideal (zero parasitic resistance, infinite current gain, no capacitances), and is biased at 1 mA emitter current.

You wish to design a 50 GHz oscillator (LO for problem 1).

Pick  $C_2$  so that its capacitive reactance is 1/10 that of  $1/g_m$ .

Pick  $C_1$  so that the negative conductance presented to the resonator is maximized.



Find  $L$ ,  $C_1$ , and  $C_2$ . Find the maximum tolerable value of load conductance.







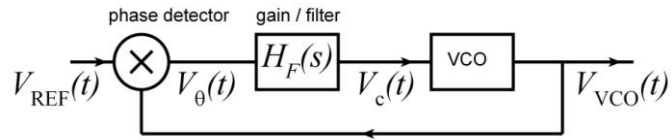
**Problem 3, 20 points**

In the 50 GHz PLL at right,

$$V_{\theta}(t) = V_0 \sin(\Delta\theta)$$

where  $V_0 = 1.0$  V,  $\Delta\theta$  is the phase difference between the reference and VCO signals.

$A_{mixer} = 1.0$  and  $V_{RF}(t) = V_{RF} \cos(\omega_{RF}t + \theta_{RF})$ .



For zero control voltage, the VCO oscillates at 50 GHz, and it tunes at a rate of 1 GHz/Volt.

The loop filter has  $H_F(s) = (1 + s\tau_z) / s\tau_i$ .

part a, 10 points

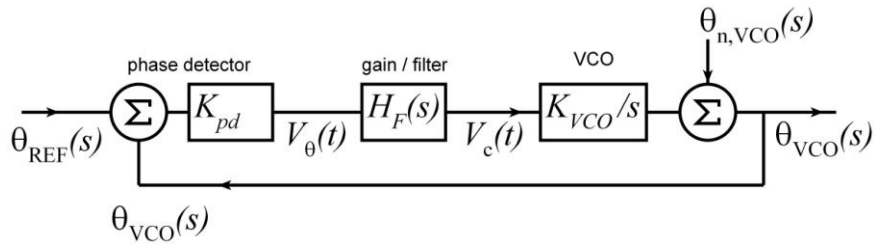
The loop filter has  $H_F(s) = (1 + s\tau_z) / s\tau_i$ . We want a 1.0 MHz PLL loop bandwidth.

The zero frequency  $f_{zero} = 1 / 2\pi\tau_z$  is to be 1/5 of this. Find the integrator time constant  $\tau_i$  and the zero frequency. Find the loop phase margin.





part b, 10 points

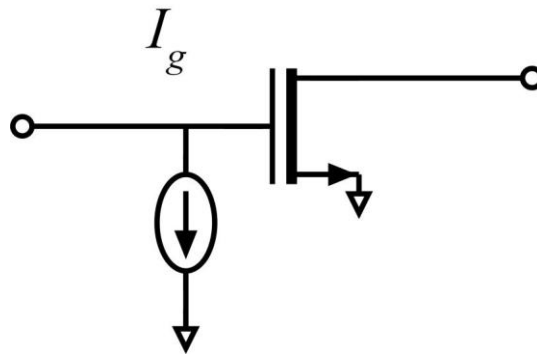


If the reference has phase noise of -120 dBc (1Hz) at 10 MHz offset from carrier, what would this contribute to the phase noise of the PLL output ? If the VCO has phase noise of -50 dBc (1Hz) at 100 Hz offset from carrier, what would this contribute to the phase noise of the PLL output ?



**Problem 4, 30 points**

The FET has  $g_m = 100$  mS and no other parasitic elements----except a 100 nA gate leakage current  $I_g$  which has shot noise associated with it



part a, 10 points

Find the spectral densities of the short-circuit input noise voltage and the open-circuit input noise current.



part b, 10 points

Find the optimum generator impedance and the minimum noise figure.

part c, 10 points

Given the optimum generator impedance, find the generator available signal power that would give you 0 dB signal/noise ratio in a 1 Hz bandwidth.

Please compare this to  $kT \cdot (1\text{ Hz})$ .

1 Hz receiver bandwidth is roughly equivalent to making a 1-second measurement. The answer may be quite surprising.