
***ECE 2C, notes set 2:
Active Devices***

Mark Rodwell

University of California, Santa Barbara

Goals of this note set:

Rough physical sense of FET operation

FET current - voltage characteristics.

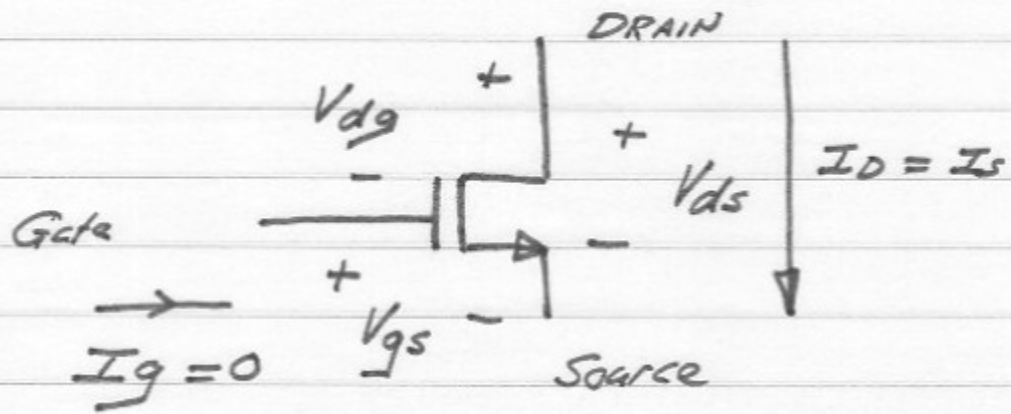
Rough mathematical models of MOSFETs

old - fashioned mobility - limited model.

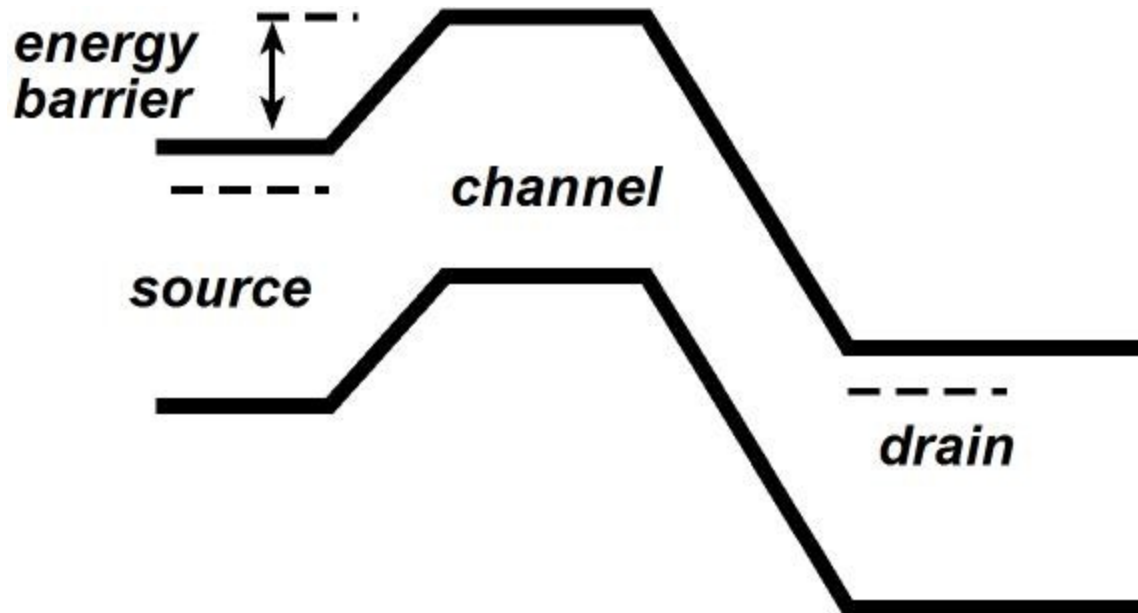
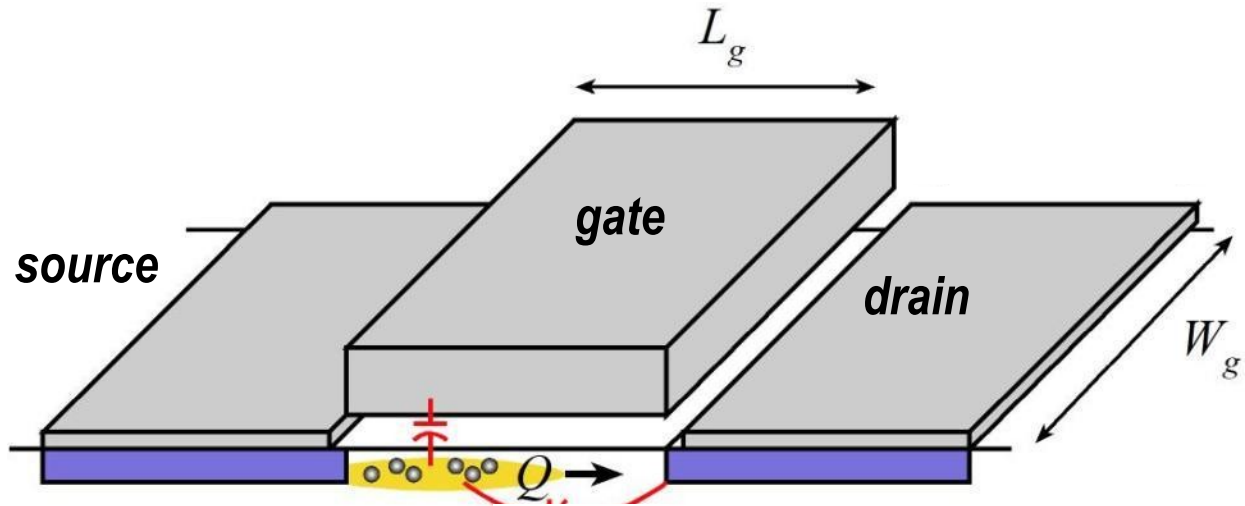
slightly less - old - fashioned velocity - limited model

N-Channel MOSFET

N-channel MOSFET:

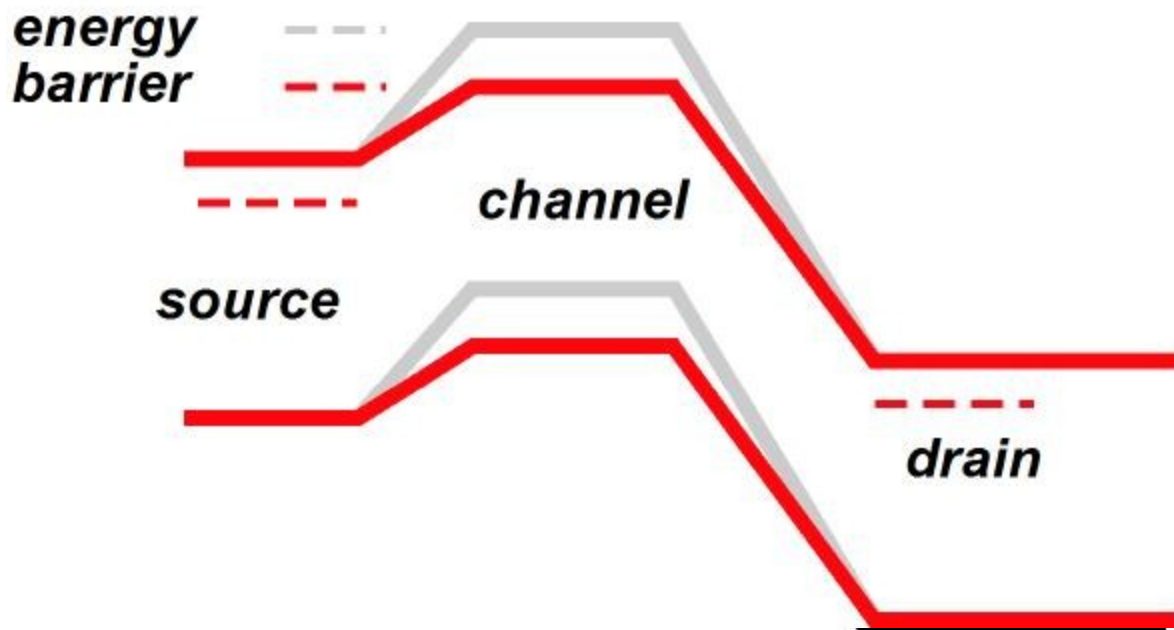
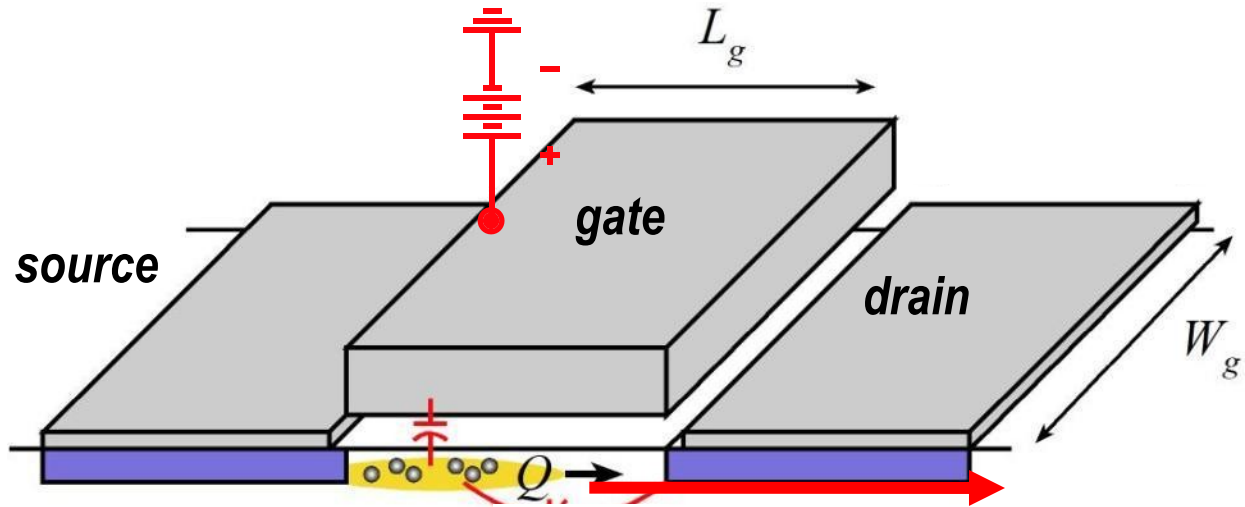


Field-Effect Transistor Operation



Positive Gate Voltage
→ reduced energy barrier
→ increased drain current

Field-Effect Transistor Operation



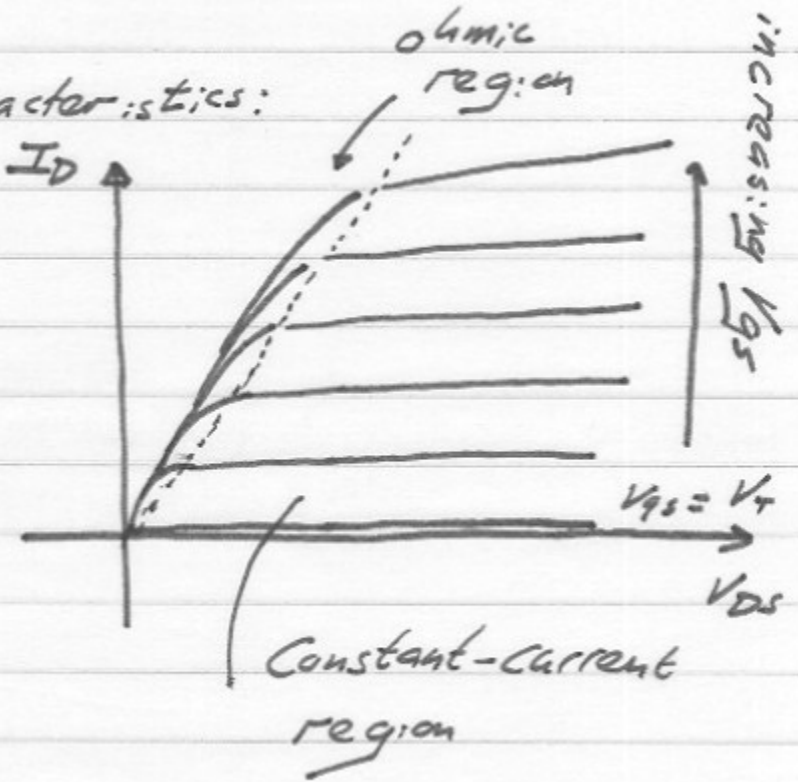
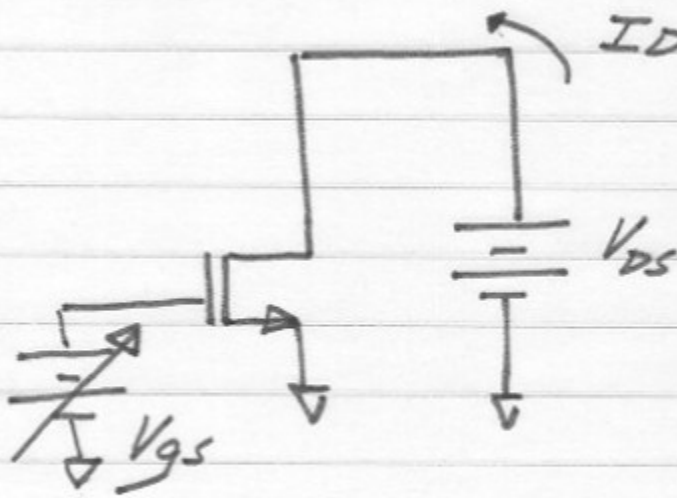
Positive Gate Voltage

→ reduced energy barrier

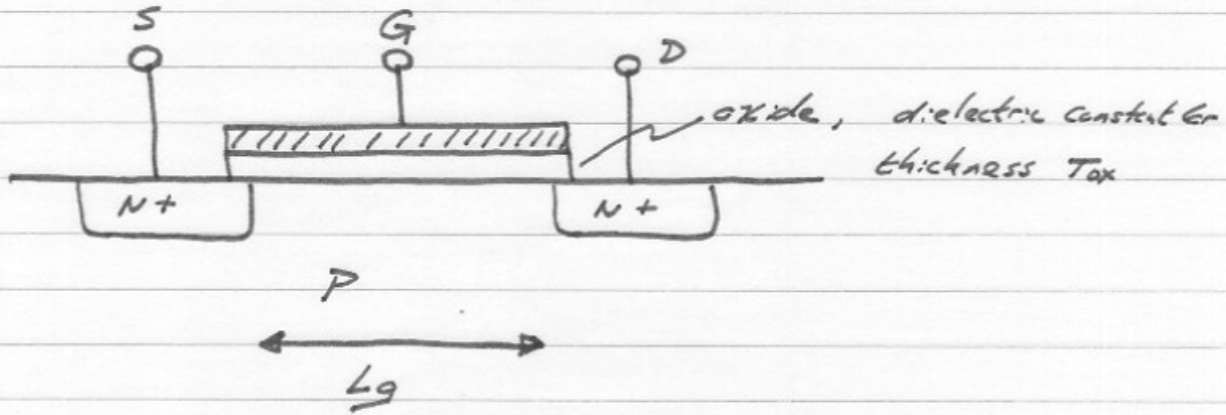
→ increased drain current

N-Channel MOSFET

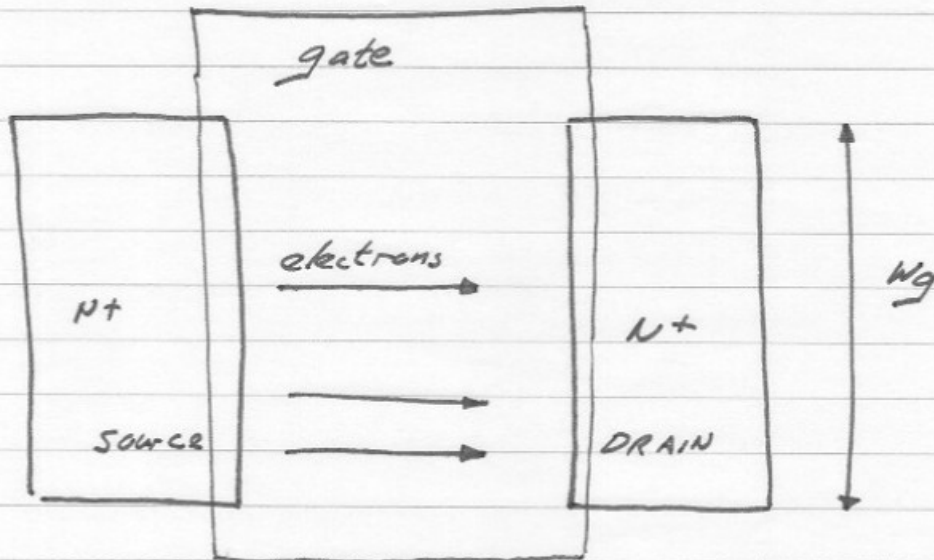
Plot common-source characteristics:



Physical Sketch

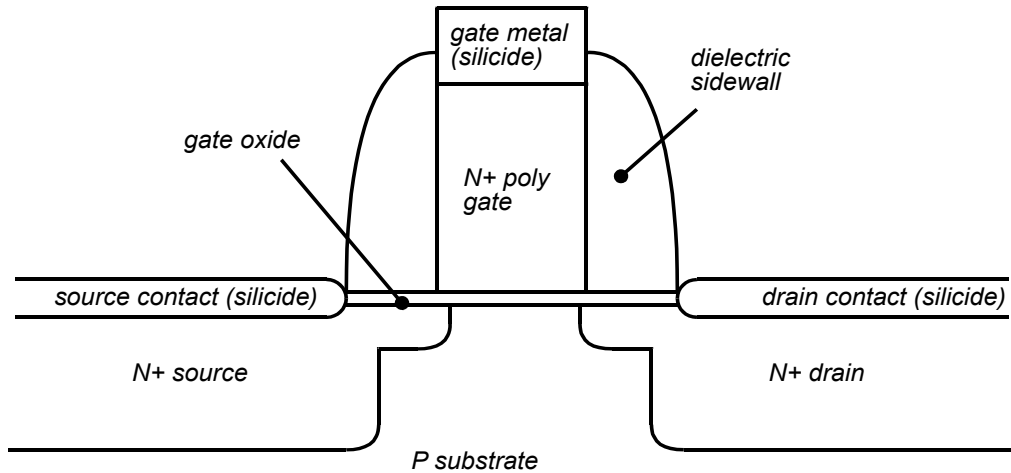


top view:

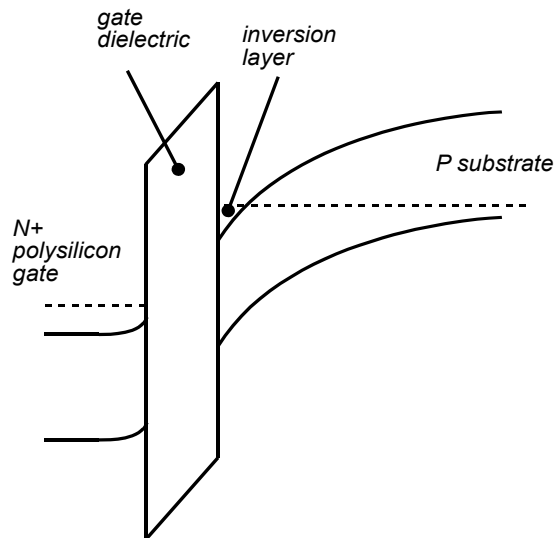
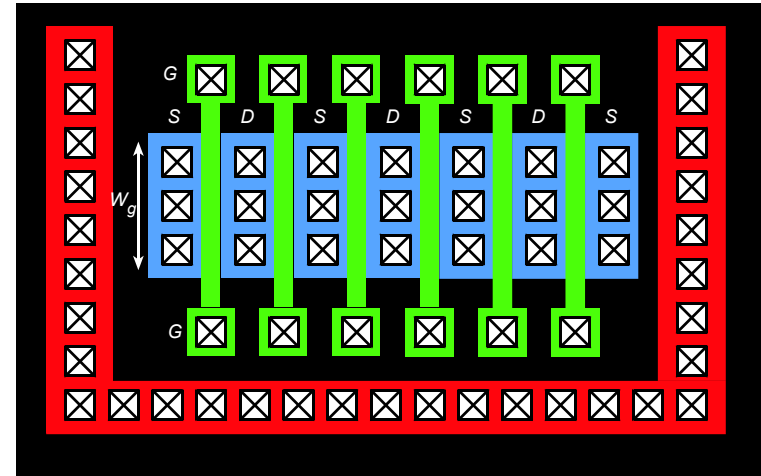


MOSFET Physical Structure

Cross-Section

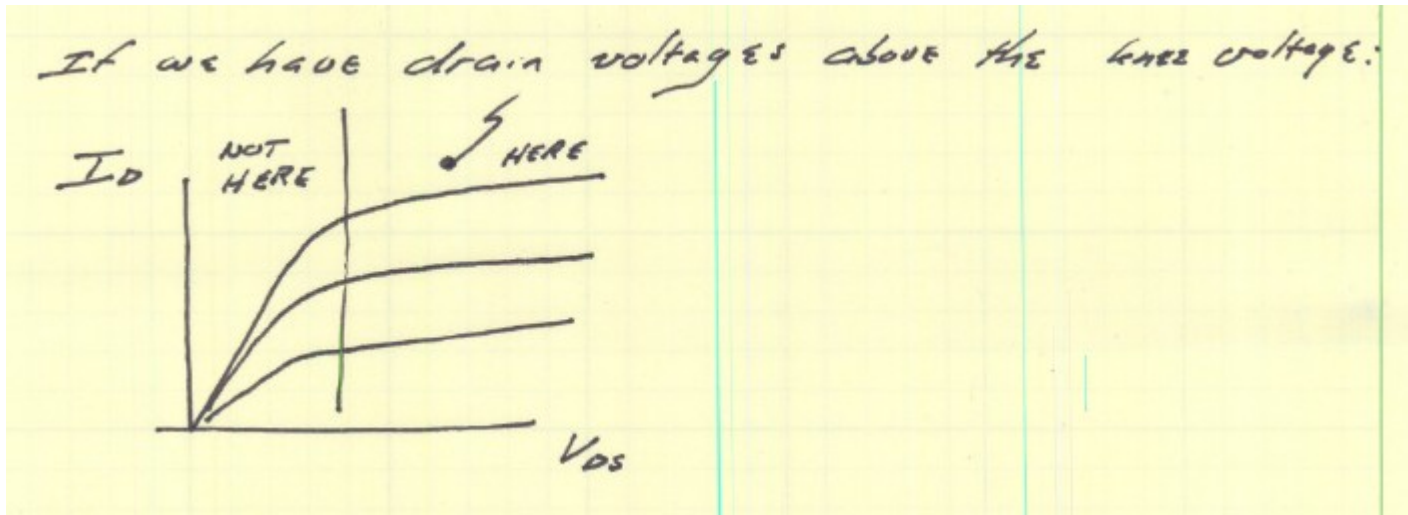


Layout



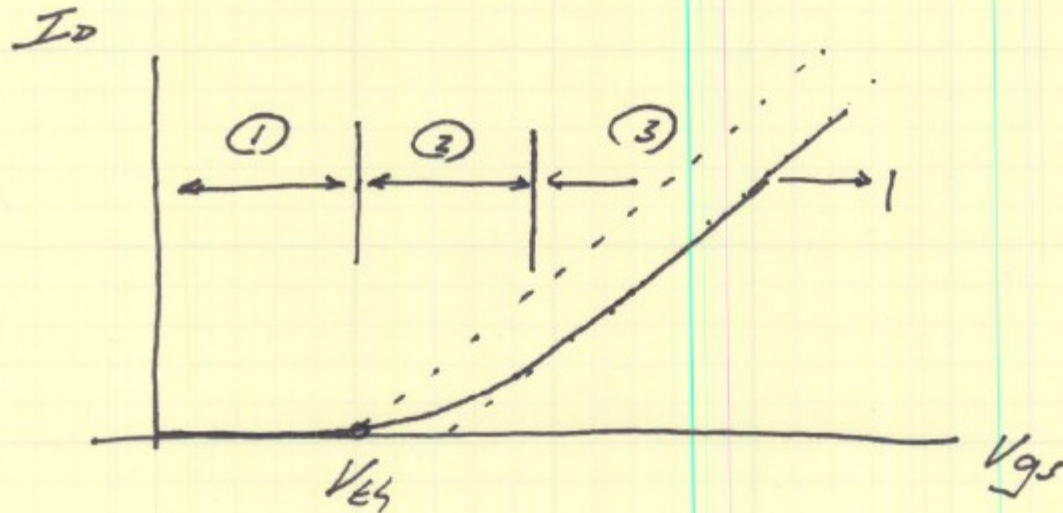
(6 FETs, each of gate width W_g ,
connected in parallel)

MOSFET I-V characteristics



MOSFET I-V characteristics

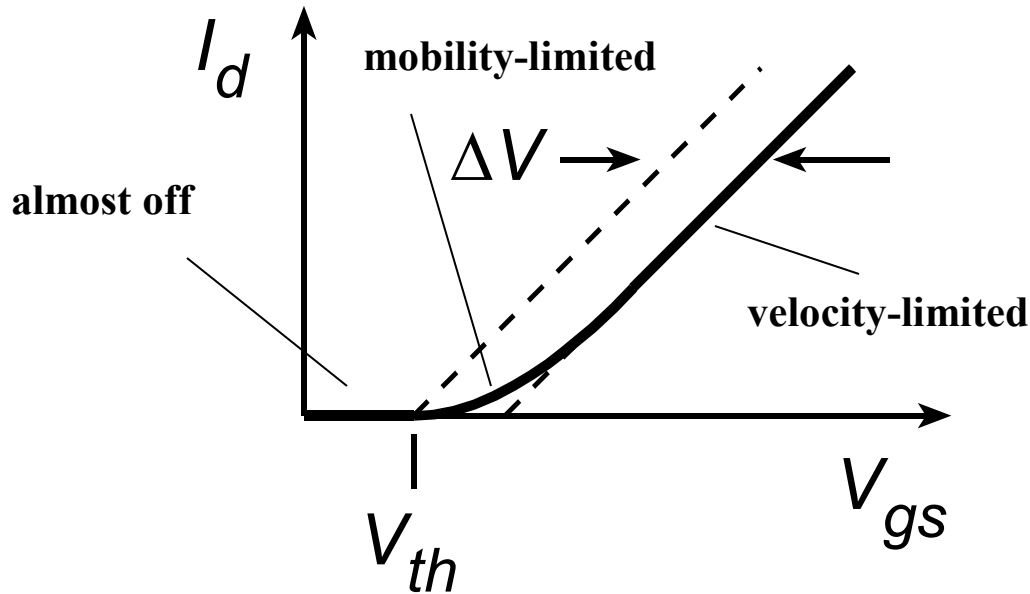
Then we can plot I_D vs V_{GS} :



There are 3 regions in the $I_D - V_{GS}$ curve:

- 1) subthreshold = almost off
- 2) mobility-limited: $I_D \sim (V_{GS} - V_{Th})^2 (1 + \lambda V_{DS})$
- 3) velocity-limited: $I_D \sim (V_{GS} - V_{Th})^1 (1 + \lambda V_{DS})$

MOSFETs: Three Regions of Gate Voltage



$$\Delta V = v_{sat} L_g / \mu$$

When V_{gs} is less than threshold, transistor is (almost) off : "subthreshold"

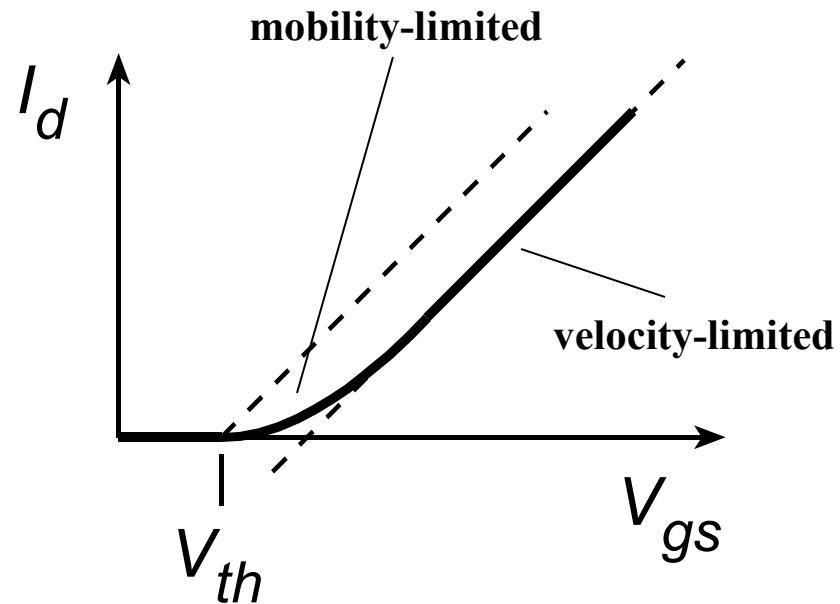
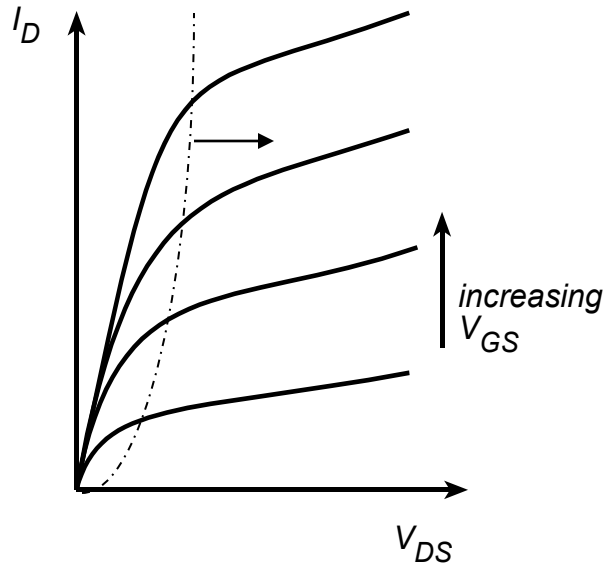
When V_{gs} is a little above threshold, current is mobility – limited

$$I_{D,\mu} \propto (V_{gs} - V_{th})^2$$

When V_{gs} is far above threshold, current is velocity – limited

$$I_{D,v} \propto (V_{gs} - V_{th} - \Delta V)$$

MOSFET DC Characteristics: Mobility-Limited Case

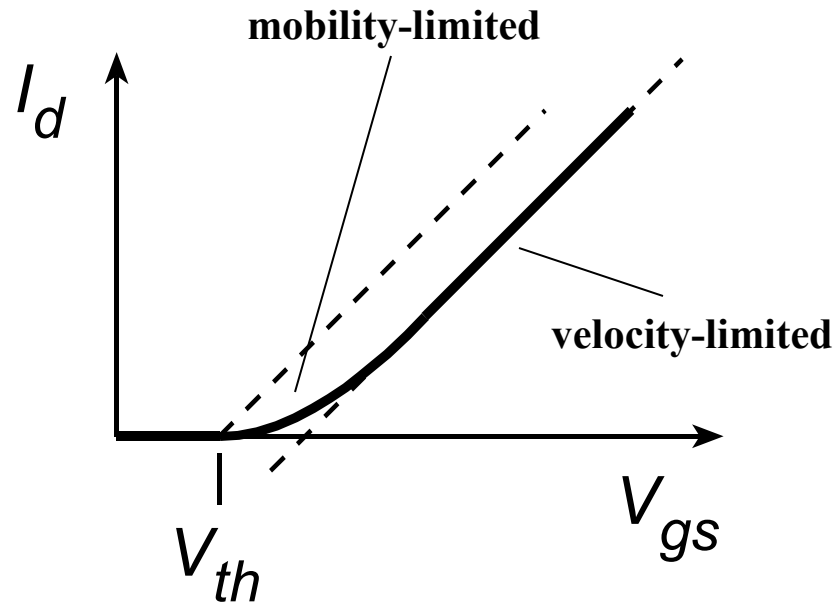
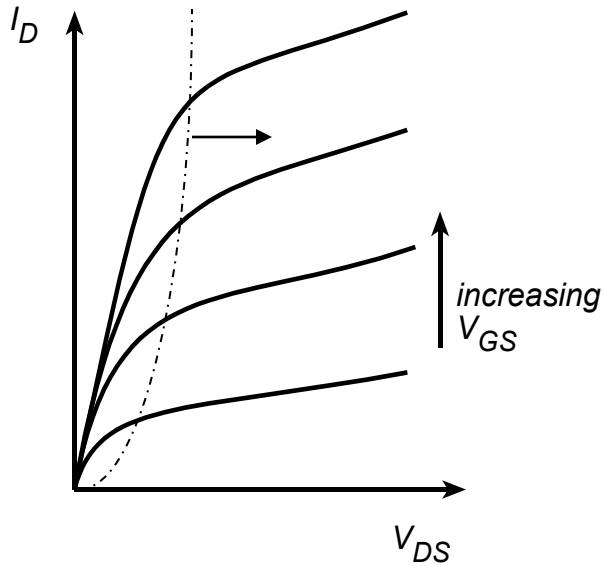


mobility – limited current :

$$I_{D,\mu} = (\mu c_{ox} W_g / 2L_g)(V_{gs} - V_{th})^2 (1 + \lambda V_{DS})$$

Applies for drain voltages larger than the knee voltage,

MOSFET DC Characteristics: Velocity-Limited Case



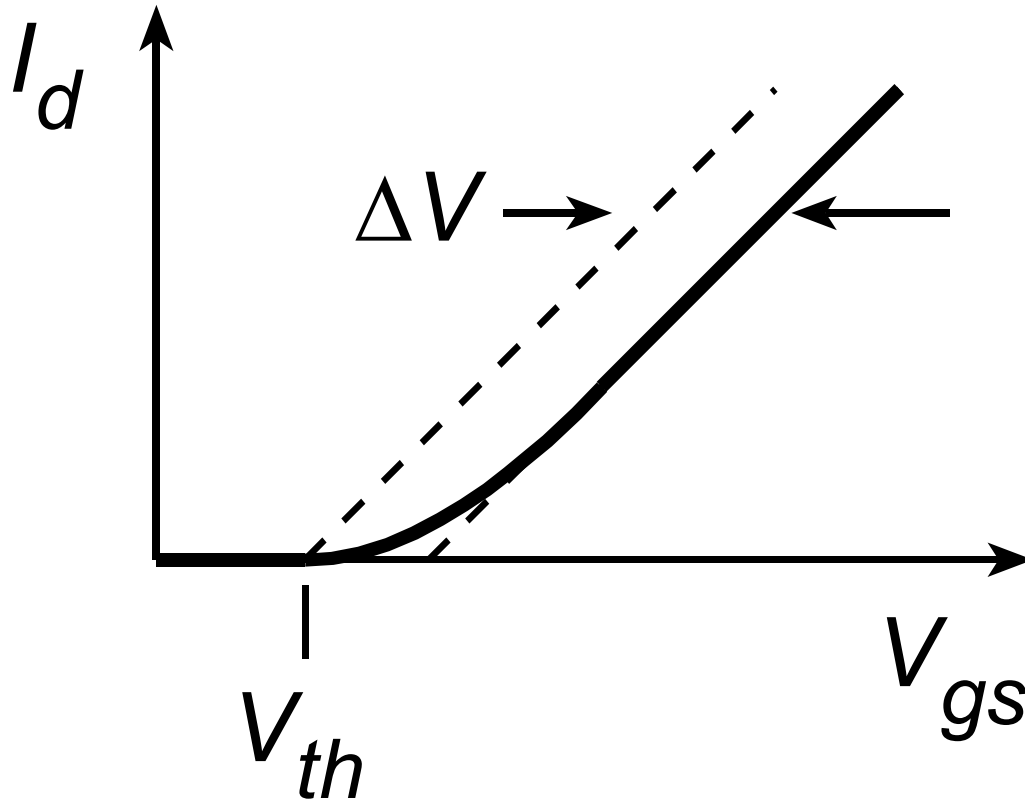
velocity – limited current

$$I_{D,v} = c_{ox} W_g v_{sat} (1 + \lambda V_{DS}) (V_{gs} - V_{th} - \Delta V)$$

$$\Delta V = v_{sat} L_g / \mu$$

Applies for drain voltages larger than the knee voltage,

DC Characteristics---Far Above Threshold



$$I_D \approx c_{ox} W_g v_{sat} (V_{gs} - V_{th} - \Delta V) \text{ for } (V_{gs} - V_{th}) / \Delta V \gg 1$$

$$\text{where } \Delta V = v_{sat} L_g / \mu$$

We will ignore the ΔV term in ece2C, but please use it in your more advanced classes.

Parameters and Typical #s

v_{sat} = saturation drift velocity $\sim 10^7$ cm/s for N - MOSFETs

μ = carrier mobility at surface $\sim 300 - 400$ cm²/(V - s) for N - MOSFET

For P - channel FETs, both v_{sat} and μ are about half that of N - FETs

c_{ox} = gate capacitance per unit area = $\epsilon_r \epsilon_0 / T_{ox}$ ($\epsilon_r = 3.8$ for SiO₂)

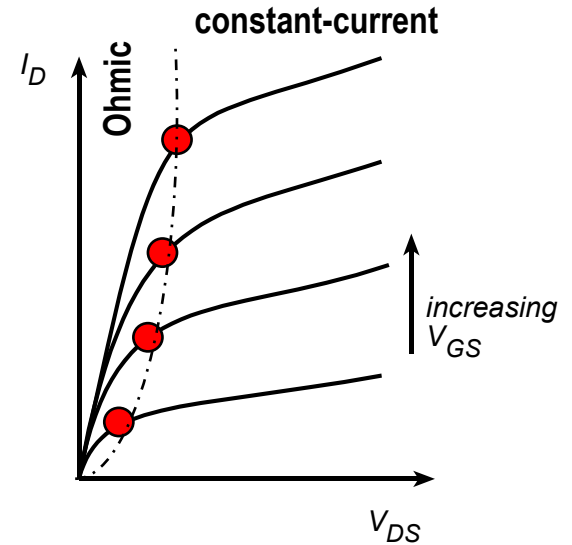
T_{ox} = equivalent oxide thickness - about 1 nm = 10^{-9} m

V_{th} threshold voltage - - - usually 0.2 - 0.4 V for modern N - FETs

λ gives slope of output characteristics : $1/\lambda$ typically 3 - 20 V

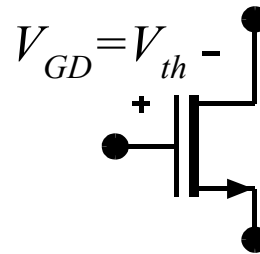
Knee Voltage: Mobility-Limited Case

The knee voltage defines the boundary between the Ohmic and constant-current regions

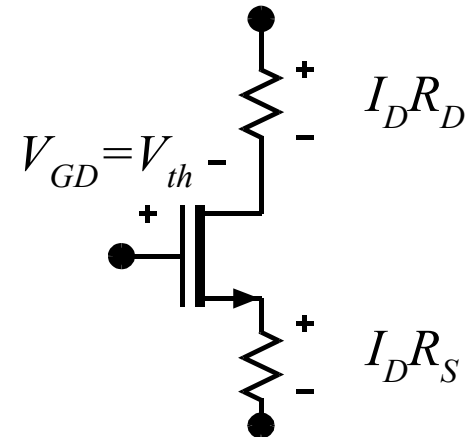


In the mobility-limited regime, the knee in curve occurs when

$$V_{dg} = V_{ds} - V_{gs} = -V_{th}$$

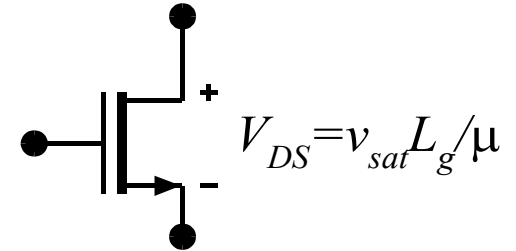


The Knee Voltage is further increased by voltage drops across the parasitic source & drain resistances.

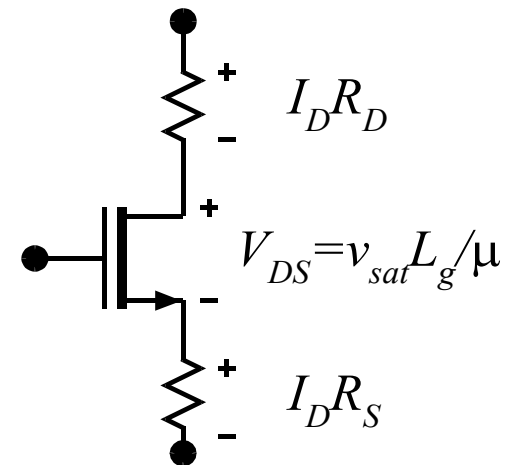


Knee Voltage: Velocity-Limited Case

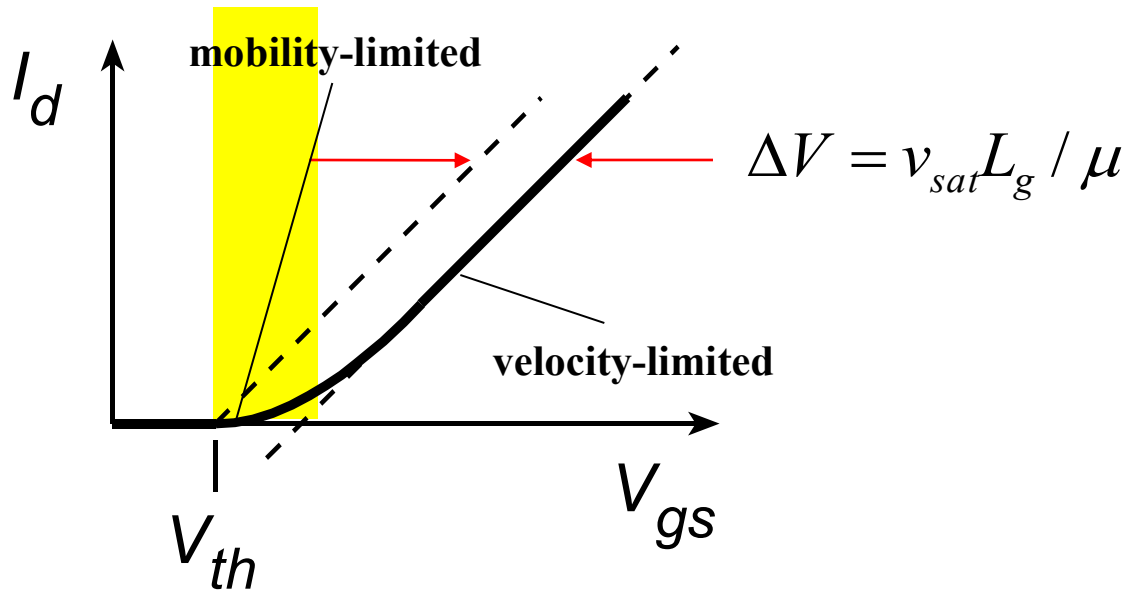
In the velocity - limited regime, the knee in curve occurs when $V_{ds} = v_{sat}L_g / \mu$



Again, the Knee Voltage is further increased by voltage drops across the parasitic source & drain resistances.



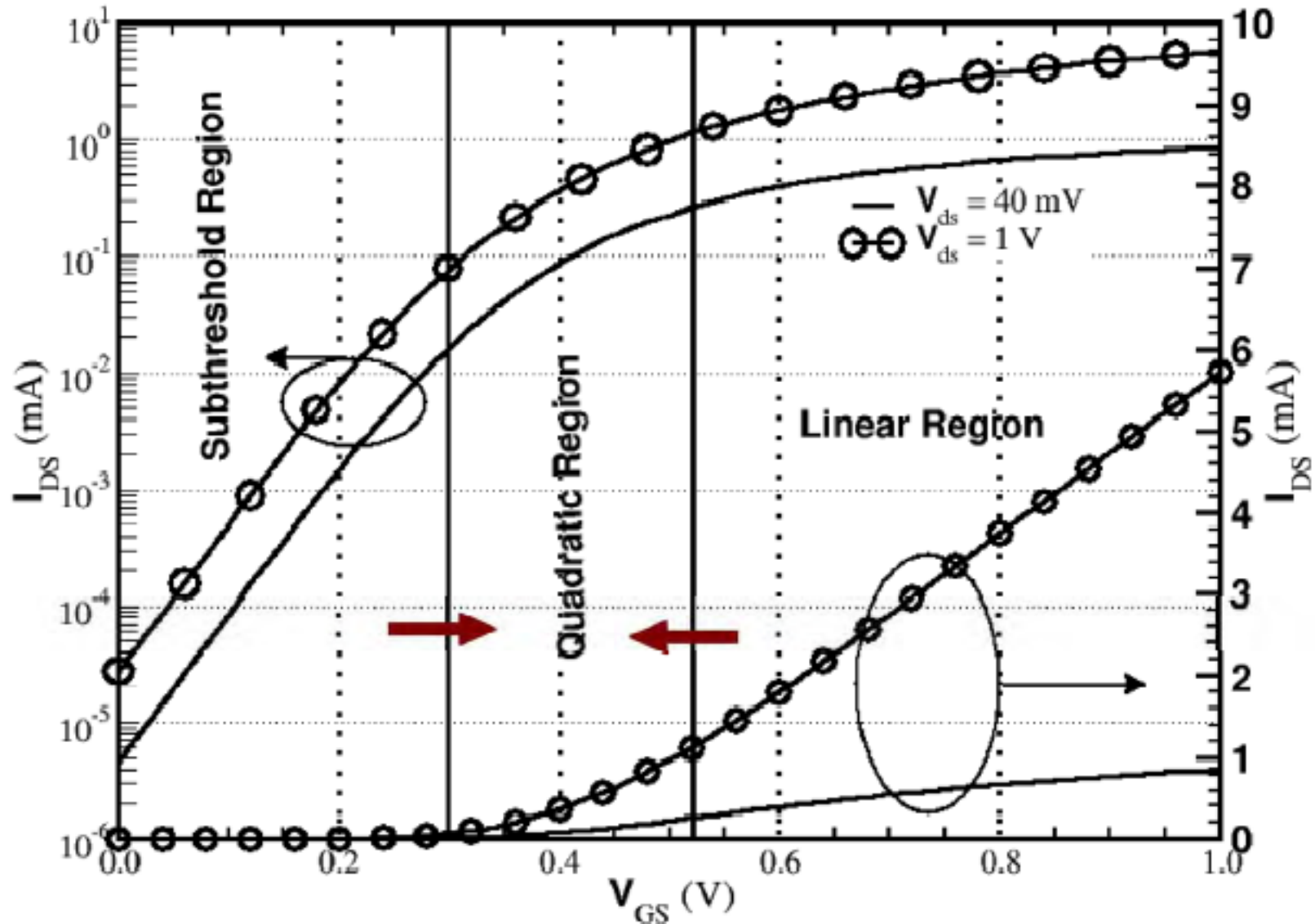
Which Model to use When ?



If $V_{gs} - V_{th} < \Delta V$ where $\Delta V = v_{sat} L_g / \mu$, use the constant - mobility model

If $V_{gs} - V_{th} > \Delta V$, use the constant - velocity model

Linear vs. Square-Law Characteristics: 90 nm



Which Model to use When ?

for 90nm CMOS, ΔV is about 0.2-0.3V

for 45nm CMOS, ΔV is about 0.15V

short gate length devices obey the velocity model.

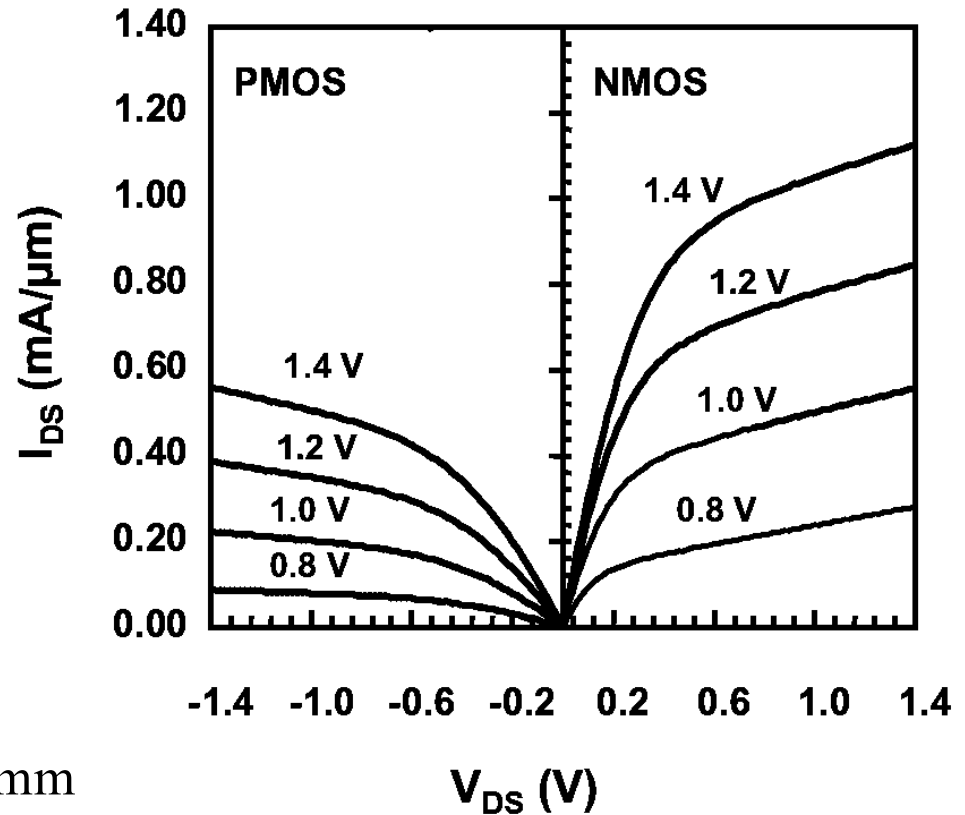
- but -

short gate length devices have very low
breakdown voltage.

- so -

analog circuit design is very hard with
short-gate-length devices.

90 nm MOSFET DC Characteristics



N - channel

$$g_m / W_g = c_{ox} v_{sat} = 1.4 \text{ mS}/\mu\text{m} = 1.4 \text{ S}/\text{mm}$$

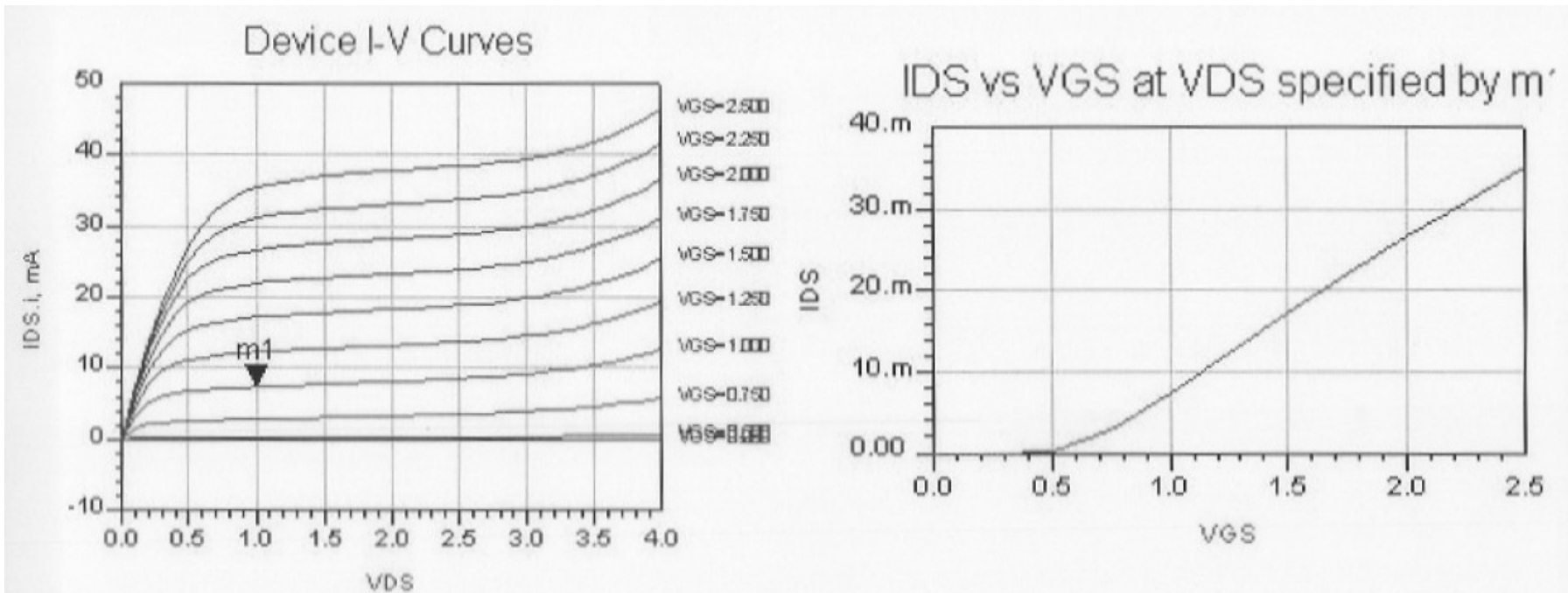
$$V_{th} = 0.6 \text{ V} \quad 1/\lambda \sim 3\text{V}$$

P - channel

$$g_m / W_g = c_{ox} v_{sat} = 0.7 \text{ mS}/\mu\text{m} = 0.7 \text{ S}/\text{mm}$$

$$|V_{th}| = 0.6 \text{ V} \quad 1/\lambda \sim 3\text{V}$$

180 nm MOSFET DC Characteristics



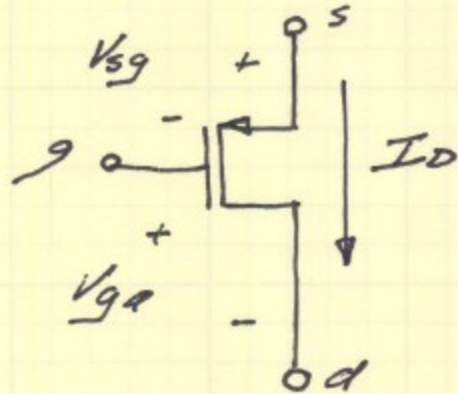
$$g_m / W_g = c_{ox} v_{sat} = 35\text{mA} / (2\text{V} \cdot 80\ \mu\text{m})$$
$$= 0.22\text{mS} / \mu\text{m} = 0.22\ \text{S} / \text{mm}$$

This is lower than typical of a 180 nm device

$$V_{th} = 0.5\ \text{V}$$

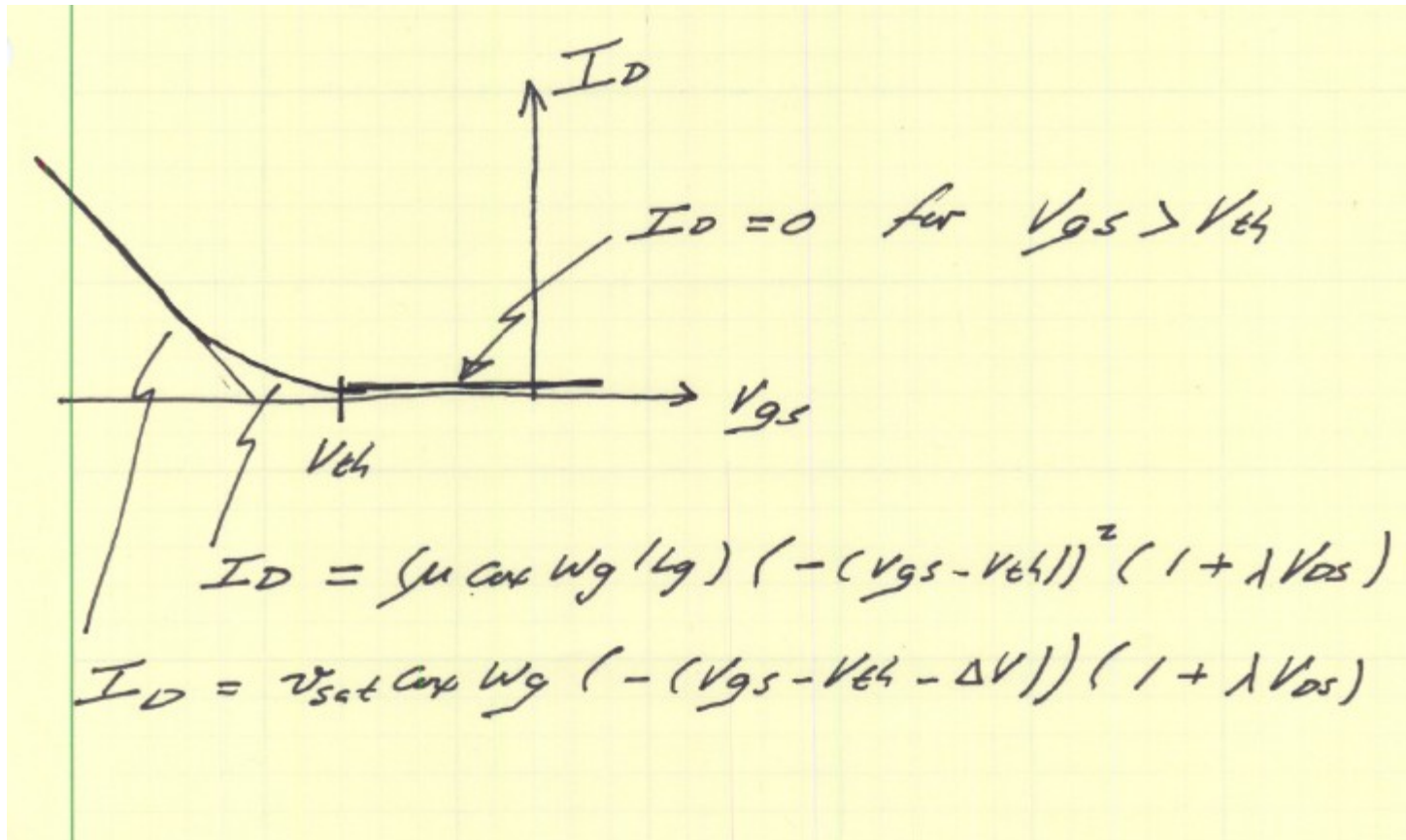
P-Channel MOSFET

P-channel MOSFET



To turn the device on
the gate must be more negative than the
source, by an amount exceeding the threshold
voltage V_{th}

P-Channel MOSFET



P-Channel MOSFET

This device is in the constant current region if V_{ds} above the knee voltage.

Example: constant mobility model:

knee @ $V_{DQ} < -V_{th}$

Example: Suppose the threshold voltage is $-1V$.

Then the P-MOSFET is in the constant-current region if the drain is at most $1V$ more positive than the gate.

