## ECE 2C Final Exam

## June 8, 2010

Do not open exam until instructed to.
Closed book: Crib sheet and 2 pages personal notes permitted
There are 4 problems on this exam, and you have 3 hours.
Use any and all reasonable approximations (5\% accuracy is fine.), AFTER STATING and approximately Justifying them.

Name:

| Problem | Points Received | Points Possible |
| :--- | :--- | :--- |
| 1a |  | 5 |
| 1b |  | 5 |
| 1c |  | 5 |
| 1d |  | 5 |
| 1e |  | 5 |
| 1f |  | 10 |
| 2a |  | 10 |
| 2b |  | 10 |
| 2c |  | 10 |
| 2d |  | 10 |
| 3a |  | 10 |
| 3b |  | 10 |
| 3c | 5 |  |
| 3d |  | 5 |
| 3e |  | 5 |
| 4a |  | 5 |
| 4b |  | 5 |
| 4c |  | 5 |
| 4d |  | 5 |
| 4e |  | 5 |
| 4f |  | 10 |
| total | 155 |  |

Problem 1, 40 points
You will be working on the circuit below:


Q1 is a mobility-limited FET, i.e. $I_{d}=\left(\mu C_{o x} W_{g} / 2 L_{g}\right)\left(V_{g s}-V_{t h}\right)^{2}\left(1+\lambda V_{d s}\right)$ where $\left(\mu C_{o x} W_{g} / 2 L_{g}\right)=4 \mathrm{~mA} / \mathrm{V}^{2}, \lambda=0.1 \mathrm{~V}^{-1}$, and $V_{t h}=0.2 \mathrm{~V}$.
$+\mathrm{Vcc}=+2.0$ volts, $-\mathrm{Vss}=-2$ Volts
Cin1 and Cout are very big and have negligible AC impedance.
RL=10 kOhm
Rgen=1 MOhm, $\mathrm{Rg}=10 \mathrm{MOhm}$

## Part a, 5 points

DC bias.
Q1 is to be biased with 1 mA drain current.
Ignore $\lambda$ while solving this part.
Find: Rss=
The DC voltage at the source of Q1. =

## Part b, 5 points

DC bias


On the circuit diagram above, label the DC voltages at ALL nodes and the DC currents through ALL resistors

## Part c, 5 points

Find the small signal parameters of Q1. Use the constant-mobility model.
gm=
Rds=

## Part d, 5 points

Replacing the transistor with its small-signal model, draw a small-signal equivalent circuit diagram for the amplifier. Give values for all elements on the diagram.

## Part e, 5 points.

Find the small signal voltage gain (Vout/Vin) of Q1.
Vout/Vin=

## Part f, 5 points

Find the ${ }^{* * *}$ amplifier *** input resistance, Vin/Vgen, and Vout/Vgen
Rin,amplifier $=$ $\qquad$
Vin/Vgen= $\qquad$
$($ Vout $/ V g e n)=$ $\qquad$

## Part g, 10 points

Now you must find the maximum signal swings. Find the output voltage due to the knee voltage and due to cutoff in Q1.

Cutoff of Q 1 ; Maximum $\Delta$ Vout resulting $=$
Knee voltage of Q1; Maximum $\Delta$ Vout resulting $=$

## Problem 2, 40 points

Principles of small-signal analysis and active device modeling: To the right is a circuit diagram of a pentode vacuum tube. Current flows between cathode and plate under control of the voltage between the grid and the cathode. Don't worry about the suppressor and the screen.

The plate current is plotted below as a function of plate-to-cathode and grid-to-cathode voltage.

Important: the grid current is nearly zero (is negligible).



Part a, 10 points


You must now work with the circuit above.
Vpp=675 Volts, Rgen=100 kOhm, $\mathrm{Rgg}=1 \mathrm{MegOhm}, \mathrm{RL}=10 \mathrm{kOHm}$.
The Tube is to be biased at 150 mA plate current, and 375 Volts plate voltage. Find the grid bias voltage -Vgg and the plate bias resistance Rpp.
$-\mathrm{Vgg}=$ $\qquad$ $R p p=$ $\qquad$

## Part b, 10 points

Find the following:
The tube transconductance $\mathrm{gm}=$
The tube AC small signal output resistance Rout,tube=

## Part c, 10 points

Draw an AC small signal equivalent circuit of the amplifier.

## Part d, 10 points

Find the AC small signal voltage gain Vout/Vgen Vout/Vgen =

Problem 3: 35 points
Nodal analysis and transistor circuit models


Part a, 10 points
Draw an accurate small-signal equivalent circuit model of the circuit above.

Part b, 10 points
Using NODAL ANALYSIS, find the transfer function $\operatorname{Vo}(\mathrm{s}) / \mathrm{Vgen}(\mathrm{s})$
The answer must be in standard form $\frac{V_{o}(s)}{V_{g e n}(s)}=\left.\frac{V_{o}}{V_{\text {gen }}}\right|_{\text {low-frequency-value }} \times \frac{1+b_{1} s+b_{2} s^{2}+\ldots}{1+a_{1} s+a_{2} s^{2}+\ldots}$,
$\frac{V_{o}(s)}{V_{g e n}(s)}=$

## Part c, 5 points

$g_{m 1}=g_{m 2}=10 \mathrm{mS} . \quad R=200$ Ohms. $C=1 \mathrm{pF}$.
How many poles are there in the transfer function?
Give its frequency / their frequencies:

$$
f_{p 1}=\ldots, f_{p 2}=\ldots, f_{p 3}=\ldots
$$

Part d, 5 points
Make an accurate Bode plot of Vout/Vgen, labeling all slopes, and all key gain and frequency values.


## Part e, 5 points

If Vgen(t) is a 1 mV step-function, find and accurately plot Vout( t ). Be sure to label both axes and give units.
$\operatorname{Vout}(\mathrm{t})=$ $\qquad$


## Problem 4, 40 points

You will be working on the circuit below:


Q1 is a PNP transistor with $\beta=100$ and $V_{A}=\infty$ Volts.

+ Vee $=+10$ volts, - Vcc $=-10$ Volts
Cin1 and Cout are very big and have negligible AC impedance.
RL=20 kOhm
Rgen $=50$ Ohm,


## Part a, 5 points

DC bias.
Q1 is to be biased with 1 mA drain current. The collector is to be biased at -5 Volt and the emitter at +5 Volts. The DC current through Rb1 is to be 10 times the Q1 base DC current. Find Ree, Rb1, Rb2, and Rc

$$
\begin{array}{ll}
\text { Ree }=\ldots & \mathrm{Rb} 1= \\
\mathrm{Rb} 2= & \mathrm{Rc}=
\end{array}
$$

Part b, 5points
DC bias


On the circuit diagram above, label the DC voltages at ALL nodes and the DC currents through ALL resistors

## Part c, 5 points

Find the small signal parameters of Q1.
$\mathrm{gm}=$ $\qquad$ Rbe=
Rce $=$

## Part d, 5 points

Replacing the transistor with its small-signal model, draw a small-signal equivalent circuit diagram for the amplifier. Give values for all elements on the diagram.

## Part e, 5 points.

Find the small signal voltage gain (Vout/Vin) of Q1.
Vout/Vin=

## Part f, 5 points

Find the ${ }^{* * *}$ amplifier ${ }^{* * *}$ input resistance, Vin/Vgen, and Vout/Vgen
Rin,amplifier $=$ $\qquad$
Vin/Vgen= $\qquad$
$($ Vout $/ V g e n)=$ $\qquad$

## Part g, 10 points

Now you must find the maximum signal swings. Find the output voltage due to the knee voltage and due to cutoff in Q1.

Cutoff of Q 1 ; Maximum $\Delta$ Vout resulting $=$ $\qquad$
saturation of Q 1 ; Maximum $\Delta$ Vout resulting $=$ $\qquad$

