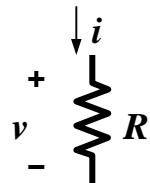


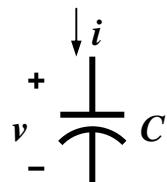
# Circuit Elements in the s-domain



## Time Domain

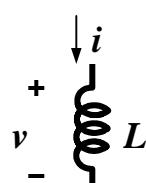


$$v = iR$$



$$i = C \frac{dv}{dt}$$

$$v(t) = \frac{1}{C} \int_0^t i dt + v(0^-)$$



$$v = L \frac{di}{dt}$$

$$i(t) = \frac{1}{L} \int_0^t v dt + i(0^-)$$

## s-Domain

$$V(s) = I(s)R$$

$$I(s) = sCV(s) - Cv(0^-)$$

$$V(s) = \frac{1}{sC} I(s) + \frac{v(0^-)}{s}$$

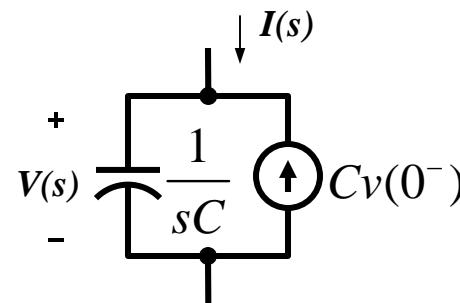
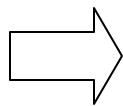
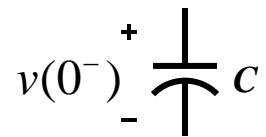
$$V(s) = sLI(s) - Li(0^-)$$

$$I(s) = \frac{1}{sL} V(s) + \frac{i(0^-)}{s}$$

Note how  
initial  
conditions  
are  
incorporated

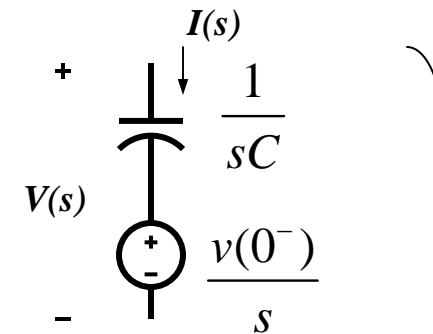
# Equivalent Circuits

Using the results of the previous slide we can draw equivalent s-domain circuits for capacitors and inductors to account for initial conditions:



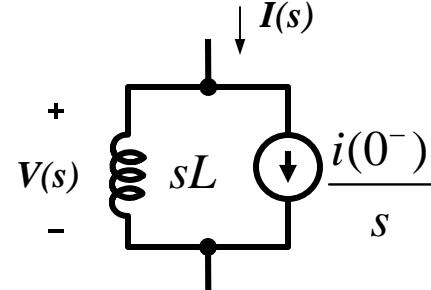
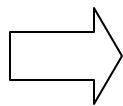
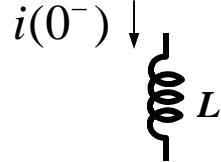
**Capacitor has an impedance:**  $\frac{1}{sC}$

$$I(s) = sCV(s) - Cv(0^-)$$



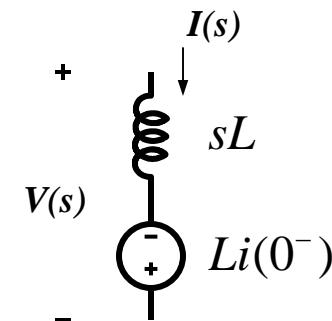
$$V(s) = \frac{1}{sC} I(s) + \frac{v(0^-)}{s}$$

Note polarity  
of sources  
representing  
initial  
conditions



**Inductor has an impedance:**  $sL$

$$I(s) = \frac{1}{sL} V(s) + \frac{i(0^-)}{s}$$



$$V(s) = sLI(s) - Li(0^-)$$