## ECE 178: Introduction (contd.)

Lecture Notes \#2: more basics
■ Section 2.4 -sampling and quantization
$\square$ Section 2.5 -relationship between pixels, connectivity analysis

## Light and the EM Spectrum



FIGURE 2.10 The electromagnetic spectrum. The visible spectrum is shown zoomed to facilitate explanation, but note that the visible spectrum is a rather narrow portion of the EM spectrum.

## Digial Image Acquisition



FIGURE 2.15 An example of the digital image acquisition process. (a) Energy ("illumination") source. (b) An el ement of a scene. (c) Imaging system. (d) Projection of the scene onto the image plane. (e) Digitized image.

Sampling and Quantization


a b
$c$
$c$
d
FIGURE 2.16 Generating a digital image. (a) Continuous image. (b) A scan line from $A$ to $B$ in the continuous image.
used to illustrate the concepts of sampling and quantization. (c) Sampling and quantization. (d) Digital scan line.

Sampling \& Quantization (contd.)


a b
FIGURE 2.17 (a) Continuos image projected onto a sensor array. (b) Result of image sampling and quantization.

Digital Image: Representation


FIGURE 2.18
Coordinate
convention used in this book to represent digital images.

## Storage Requirement

Image Dimension: $\mathrm{NxN} ; \mathrm{k}$ bits per pixel.

TABLE 2.1
Number of storage bits for various values of $N$ and $k$.

| $\boldsymbol{N} / \boldsymbol{k}$ | $\mathbf{1}(\boldsymbol{L}=\mathbf{2})$ | $\mathbf{2}(\boldsymbol{L}=\mathbf{4})$ | $\mathbf{3}(\boldsymbol{L}=\mathbf{8})$ | $\mathbf{4}(\boldsymbol{L}=\mathbf{1 6})$ | $\mathbf{5}(\boldsymbol{L}=\mathbf{3 2})$ | $\mathbf{6}(\boldsymbol{L}=\mathbf{6 4})$ | $\mathbf{7}(\boldsymbol{L}=\mathbf{1 2 8})$ | $\mathbf{8}(\boldsymbol{L}=\mathbf{2 5 6})$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 32 | 1,024 | 2,048 | 3,072 | 4,096 | 5,120 | 6,144 | 7,168 | 8,192 |
| 64 | 4,096 | 8,192 | 12,288 | 16,384 | 20,480 | 24,576 | 28,672 | 32,768 |
| 128 | 16,384 | 32,768 | 49,152 | 65,536 | 81,920 | 98,304 | 114,688 | 131,072 |
| 256 | 65,536 | 131,072 | 196,608 | 262,144 | 327,680 | 393,216 | 458,752 | 524,288 |
| 512 | 262,144 | 524,288 | 786,432 | $1,048,576$ | $1,310,720$ | $1,572,864$ | $1,835,008$ | $2,097,152$ |
| 1024 | $1,048,576$ | $2,097,152$ | $3,145,728$ | $4,194,304$ | $5,242,880$ | $6,291,456$ | $7,340,032$ | $8,388,608$ |
| 2048 | $4,194,304$ | $8,388,608$ | $12,582,912$ | $16,777,216$ | $20,971,520$ | $25,165,824$ | $29,369,128$ | $33,554,432$ |
| 4096 | $16,777,216$ | $33,554,432$ | $50,331,648$ | $67,108,864$ | $83,886,080$ | $100,663,296$ | $117,440,512$ | $134,217,728$ |
| 8192 | $67,108,864$ | $134,217,728$ | $201,326,592$ | $268,435,456$ | $335,544,320$ | $402,653,184$ | $469,762,048$ | $536,870,912$ |



Re-sampling...

$\begin{array}{lll}\text { a b } \\ \text { d } & \text { e f } \\ \text { l }\end{array}$
FIGURE 2.20 (a) $1024 \times 1024$, 8 -bit image. (b) $512 \times 512$ image resampled into $1024 \times 1024$ pixels by row and column duplication. (c) through (f) $256 \times 256,128 \times 128,64 \times 64$, and $32 \times 32$ images resampled into $1024 \times 1024$ pixels.

Quantization: Gray-scale resolution


FIGURE $\mathbf{2 . 2 1}$
(a) $452 \times 374$
256 -level image. (b)-(d) Image
displayed in 128, displayed in 128 ,
64, and 32 gray
levels, while
. 64, and 22 gra
levels. while
keeping the keeping the
spatial resolution
constant.
constant.

## ...false contouring



## Sampling and Aliasing



FIGURE 2.24 Illustration of the Moire pattern effect.

## Additional Reading

■ Chapter 1, Introduction

- Chapter 2, Sections 2.1-2.4
- We will discuss sampling and quantization in detail later
Next:
- some basic relationships between pixels (Section 2.5)


## Relationship between pixels

Neighbors of a pixel

- 4-neighbors (N,S,W,E pixels) $==N_{4}(p)$. A pixel $p$ at coordinates ( $\mathrm{x}, \mathrm{y}$ ) has four horizontal and four vertical neighbors:
- $(x+1, y),(x-1, y),(x, y+1),(x, y-1)$
- You can add the four diagonal neighbors to give the 8neighbor set. Diagonal neighbors $==N_{D}(p)$.
- 8-neighbors: include diagonal pixels $==N_{8}(p)$.


## Pixel Connectivity

Connectivity -> to trace contours, define object boundaries, segmentation.
In order for two pixels to be connected, they must be "neighbors" sharing a common property-satisfy some similarity criterion. For example, in a binary image with pixel values " 0 " and " 1 ", two neighboring pixels are said to be connected if they have the same value.

Let V: Set of gray level values used to define connectivity; e.g., $\mathrm{V}=\{1\}$.

## Connectivity-contd.

4-adjacency: Two pixels $p$ and $q$ with values in $V$ are 4-adjacent if $q$ is in the set $N_{4}(p)$.
8-adjacency: $q$ is in the set $\mathrm{N}_{8}(\mathrm{p})$.
■ m-adjacency: Modification of 8-A to eliminate multiple connections.
$-q$ is in $N_{4}(p)$ or
$-q$ in $N_{D}(p)$ and $N_{4}(p) \cap N_{4}(q)$ is empty.

## Connected components

- Let $S$ represent a subset of pixels in an image.
- If $p$ and $q$ are in $S, p$ is connected to $q$ in $S$ if there is a path from $p$ to $q$ entirely in $S$.
- Connected component: Set of pixels in $S$ that are connected; There can be more than one such set within a given S .


## 4-connected components


$\mathrm{p}=0$ : no action;
$\mathrm{p}=1$ : check r and t .

- both $r$ and $t=0$; assign new label to $p$;
- only one of $r$ and $t$ is a 1 . assign that label to $p$;
- both $r$ and $t$ are 1.
- same label => assign it to $p$;
- different label=> assign one of them to $p$ and establish equivalence between labels (they are the same.)

Second pass over the image to merge equivalent labels.

## Exercise

## Develop a similar algorithm for 8connectivity.

## Problems with 4- and 8-connectivity

Neither method is satisfactory.

- Why? A simple closed curve divides a plane into two simply connected regions.
- However, neither 4-connectivity nor 8-connectivity can achieve this for discrete labelled components.
- Give some examples..


## Related questions

■ Can you "tile" a plane with a pentagon?

## Distance Measures

- What is a Distance Metric?

For pixels $p, q$, and $z$, with coordinates $(x, y),(s, t)$, and ( $u, v$ ), respectively:
$D(p, q) \geq 0 \quad(D(p, q)=0$ iff $p=q)$
$D(p, q)=D(q, p)$
$D(p, z) \leq D(p, q)+D(q, z)$

## Distance Measures

- Euclidean

$$
D_{e}(p, q)=\sqrt{(x-s)^{2}+(y-t)^{2}}
$$

■ City Block

$$
D_{4}(p, q)=|x-s|+|y-t|
$$

- Chessboard

$$
D_{8}(p, q)=\max (|x-s|,|y-t|)
$$



