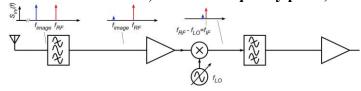
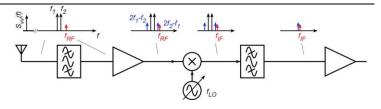
ECE 145b, 218B problem set (distortion mechanisms, receiver frequency plans)

Problem 1: Image response. Consider an FM radio receiver, where the signal frequency to be tuned is 88-108 MHz, and the IF frequency is 10.7 MHz. The local oscillator frequency



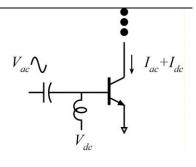
is *above* the intended RF signal frequency, not below it. (a) When the receiver is tuned to 88 MHz, what is the LO frequency? What is the RF image frequency? (b) When the receiver is tuned to 108 MHz, what is the LO frequency? What is the RF image frequency? (c) Based upon the above, can a fixed-tuned RF preselect filter be used for image rejection? What is the allowable frequency passband of this filter?

Problem 2: A receiver, designed to receive of problem (1abc) is now tuned to receive a station at 100 MHz RF frequency. The receiver has a -10 dBm input-referred third order intercept.



There are two interfering radio stations, each of -25 dBm amplitude, one 200 kHz below the RF signal of interest, the other 400 kHz below the RF signal of interest. (a) What RF signal power would result in a 20 dB carrier-to-interference ratio, i.e. the IM3 product from the 2 interferers is 20 dB below the desired RF signal? (b) Compare this to the noise-limited sensitivity of a high-quality FM stereo receiver at about -135 dBm.

Problem 3 **(218B only)**: Consider a bipolar transistor amplifier with $I_C = I_s \exp(qV_{be}/kT)$. The base emitter voltage is the sum of a DC bias voltage $V_{BE,DC}$ and of an AC signal $\delta V_{BE} = 2^{1/2}V_{RMS}\cos(\omega_1 t) + 2^{1/2}V_{RMS}\cos(\omega_2 t)$. As a result of this, the collector current has both an AC and a DC component and has 2-tone distortion products. If $V_{BE,DC}$ is such that the transistor is biased at $I_{E,DC} = 1 \text{ mA}$, $V_{BE} = V_{BE,DC} + \delta V_{be}$ and $I_C = I_{C,DC} + \delta I_C$, and if we truncate to 3rd order, then $\delta I_C = a_1 \delta V_{be} + a_2 (\delta V_{be})^2 + a_3 (\delta V_{be})^3 + \dots$



(a) Find the coefficients a_1 and a_3 . (b) Considering only the 1st and 3rd order terms, what value of V_{rms} gives equal response for the linear term $a_1 \delta V_{be}$ at frequency ω_1 and for the cubic term $a_3 (\delta V_{be})^3$ at frequency $2\omega_1 - \omega_2$? This is the input-referred third-order intercept in units of volts (RMS).

Problem 4: The FET has characteristics $I_d = K(V_{gs} - V_{th})^2$ where K = 20 mA/V² and $V_{th} = 0.3$ Volts. The FET is biased at 3 mA drain current. With $V_{ac} = V_0 \cos(\omega_1 t) + V_0 \cos(\omega_2 t)$ and $V_0 = 1$ mV, compute the amplitudes of all Fourier components of the drain AC current.

